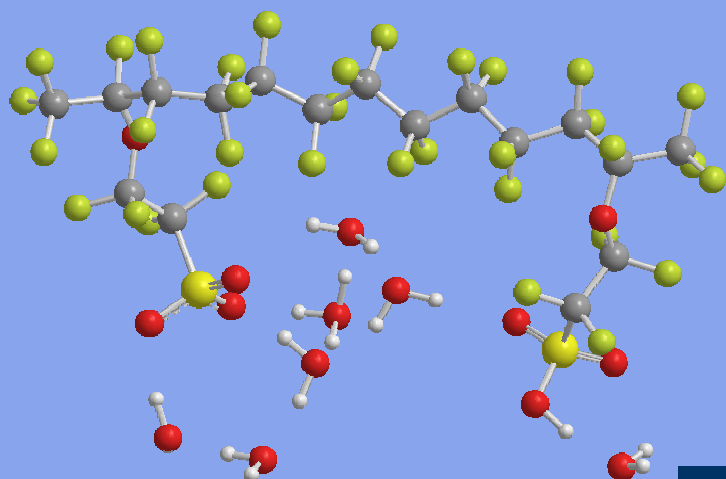


# Proton Conduction in Diverse Media

12/05/2005

## Mechanisms of Proton Conduction in the Dow Membrane: Complexity, Cooperativity, and Connectivity



S.J. Paddison  
University of Alabama

J. A. Elliott  
University of Cambridge

**UAH**  
The University of Alabama in Huntsville



# Recent Reviews

S.J. Paddison, “First principles modeling of sulfonic acid-based ionomer membranes”, in *Handbook of Fuel Cells – Fundamentals, Technology and Applications*, edited by W. Vielstich, H. Gasteiger, A. Lamm, Volume 3: *Fuel Cell Technology and Applications*, J. Wiley and Sons, Chichester, Chapter 31 (2003).

S.J. Paddison, “Proton conduction mechanisms in Polymer Electrolyte Membranes at low degrees of hydration”, *Annual Review of Materials Research*, **33**, 289-319 (2003).

K. D. Kreuer, S.J. Paddison, E. Spohr, and M. Schuster “Transport in Proton Conductors for Fuel Cell Applications: Simulations, Elementary Reactions, and Phenomenology”, *Chemical Reviews*, **104**, 4637 (2004).

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# Collaboration

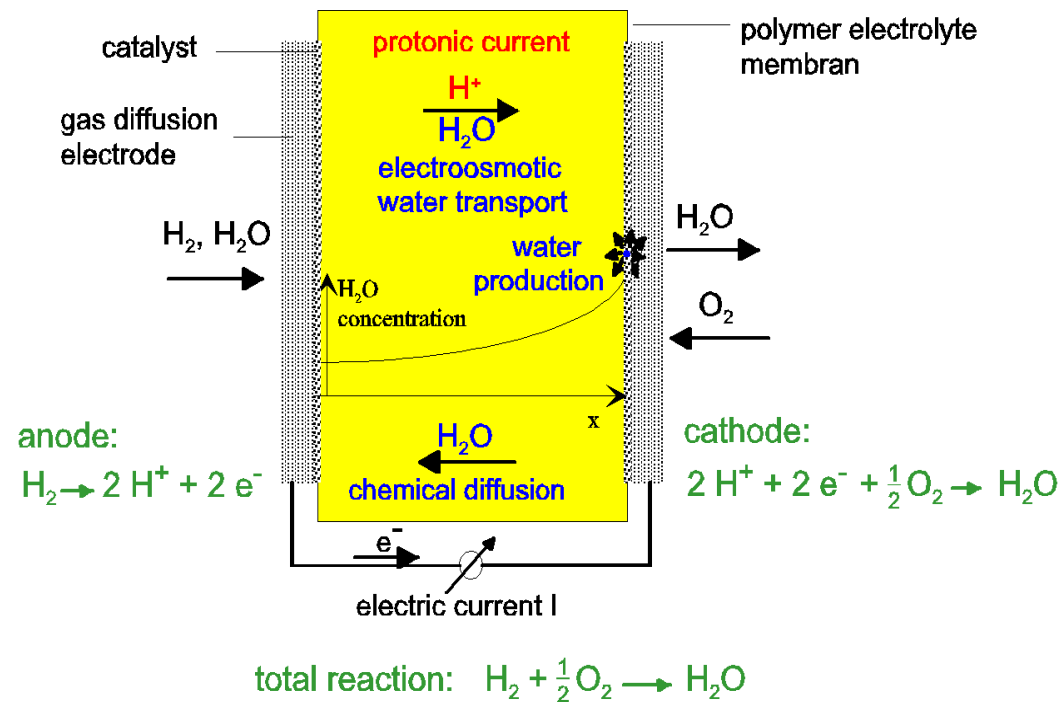
## Past

- T. A. Zawodzinski Jr., MST-11, LANL – CWRU
- L. R. Pratt, T-12, LANL
- M. Eikerling, MST-11, LANL – SFU
- T. K. Mattsson, SSC, SNL

## Present

- K-D. Kreuer, Max Planck Institute, Stuttgart, GERMANY
  - R. Paul, The University of Calgary, CANADA
  - J. A. Elliott, The University of Cambridge, UK
-

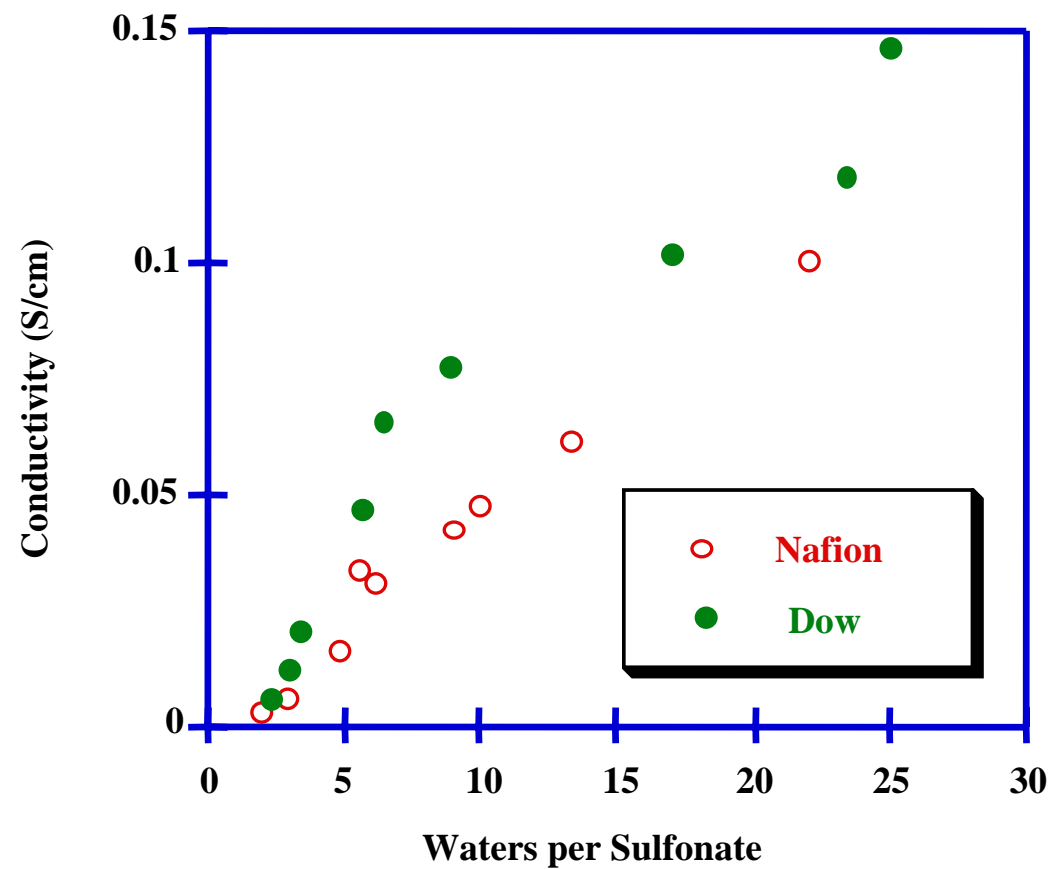
# Polymer electrolyte membrane (PEM) fuel cell



# Modeling Goals

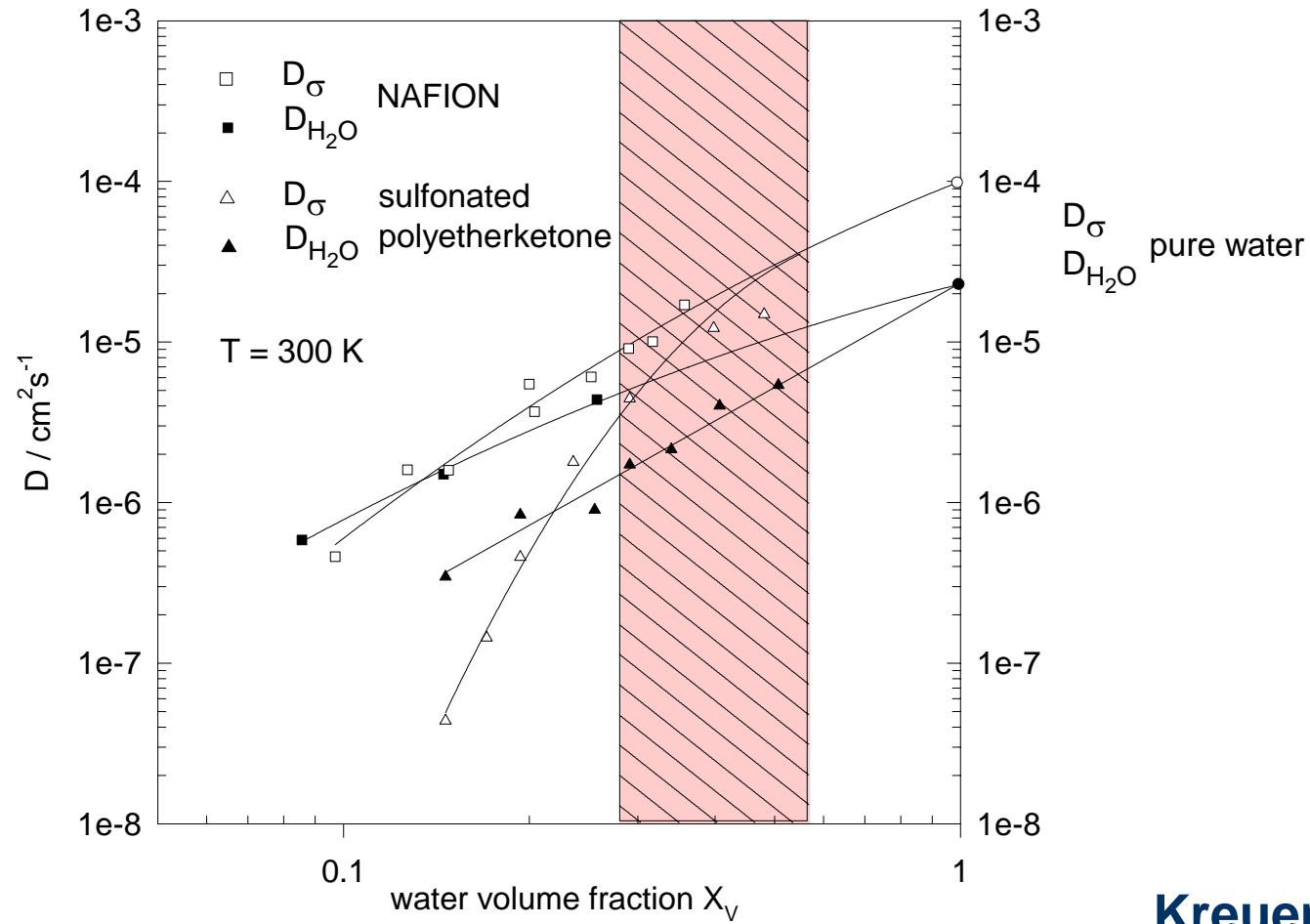
- (1) To obtain a molecular-level understanding of transport mechanism(s) in polymer electrolyte membranes.**
  - (2) To connect/correlate this information with function/properties of the materials.**
  - (3) To design, in collaboration with synthetic and experimental characterization efforts, improved materials.**
-

# Provocation:



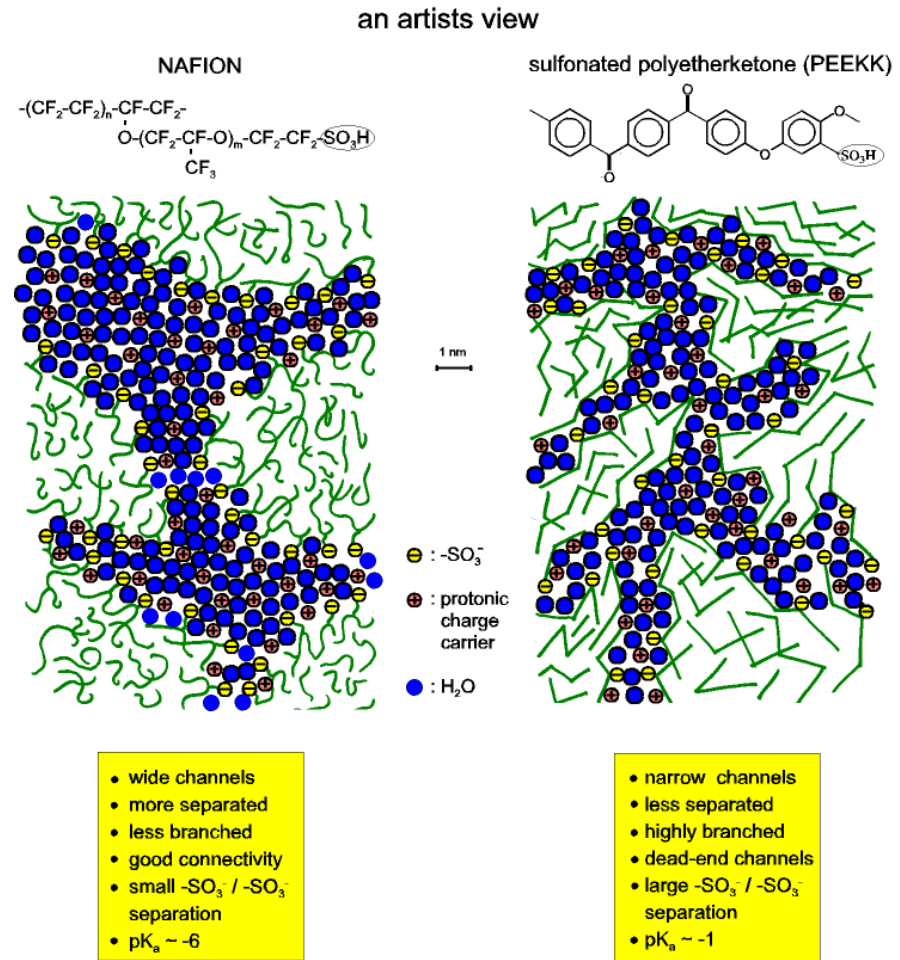
Zawodzinski, LANL

# Provocation:



Kreuer, MPI

# Morphology:



- model dependent

- measurement dependent



# Conduction:

(1) **Complexity:** proton dissociation; transfer; transport - diffusion

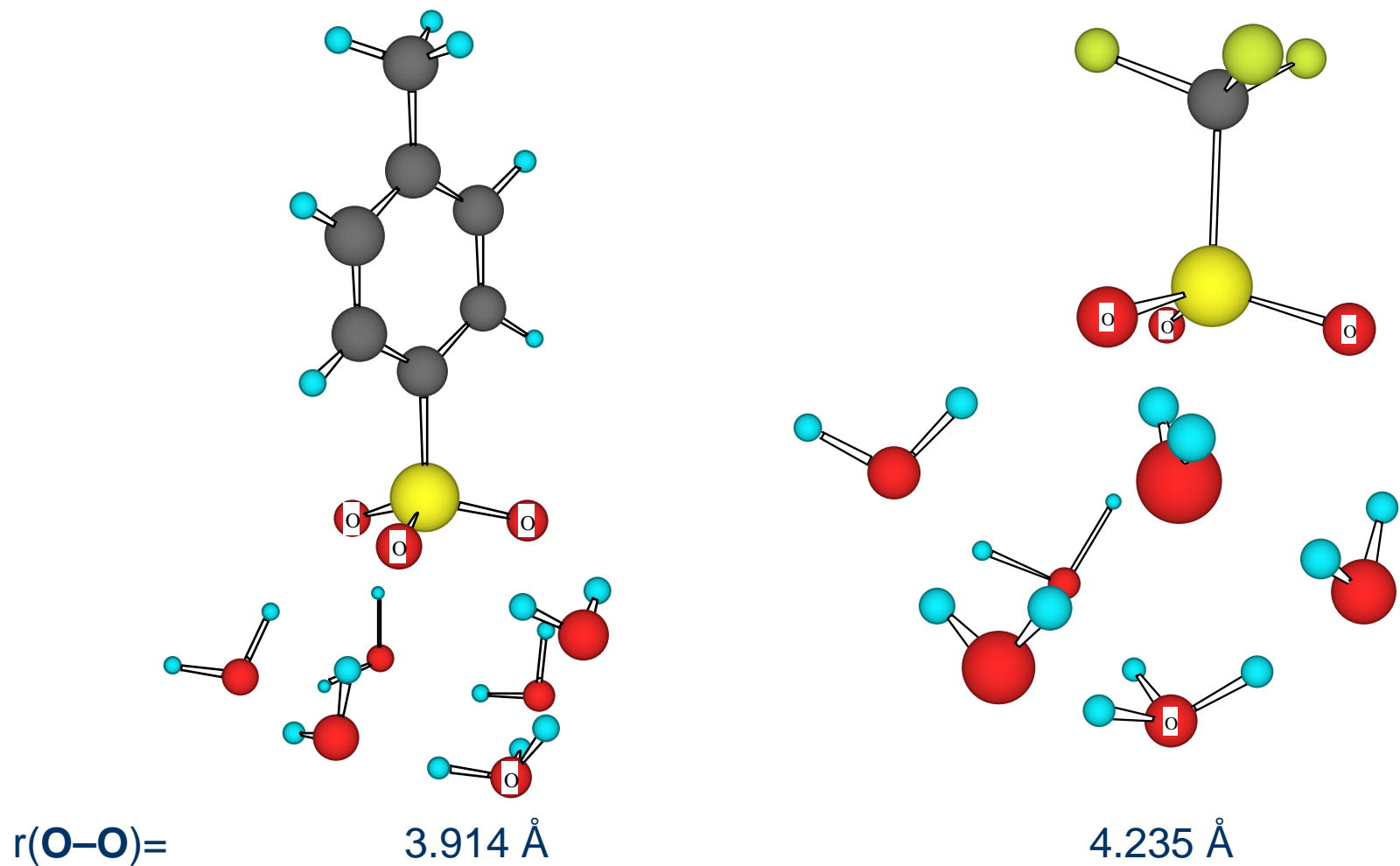
(2) **Connectivity:** hydrogen bonding: water to anionic sites; water to water; domain to domain

(3) **Cooperativity:** flexibility of polymeric groups, motion of polymeric side chains, flux of water

All depend on: polymer chemistry, degree of hydration, temperature, and presence of 'other' species.

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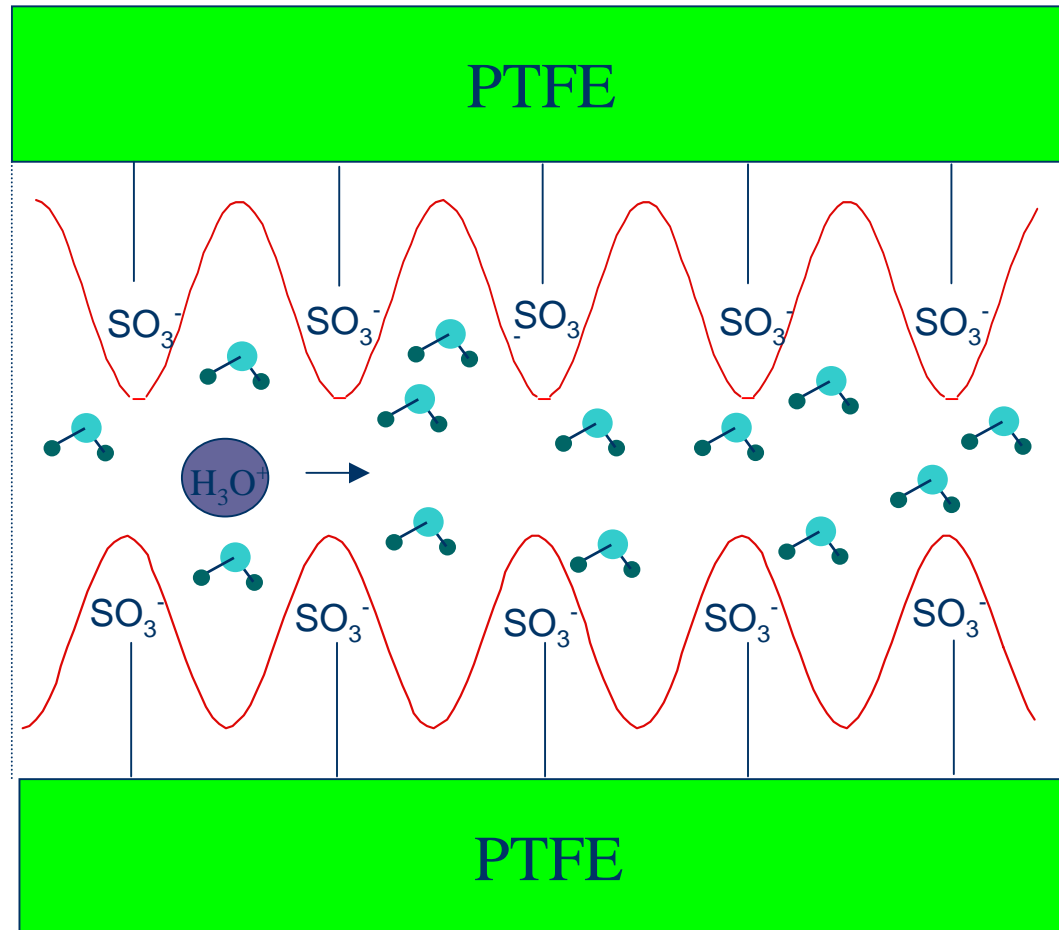
# Complexity: local chemistry specific separation



B3LYP/6-31G\*\*

S.J. Paddison *J. New Materials for Electrochem. Sys.* **4**, 197 (2001).

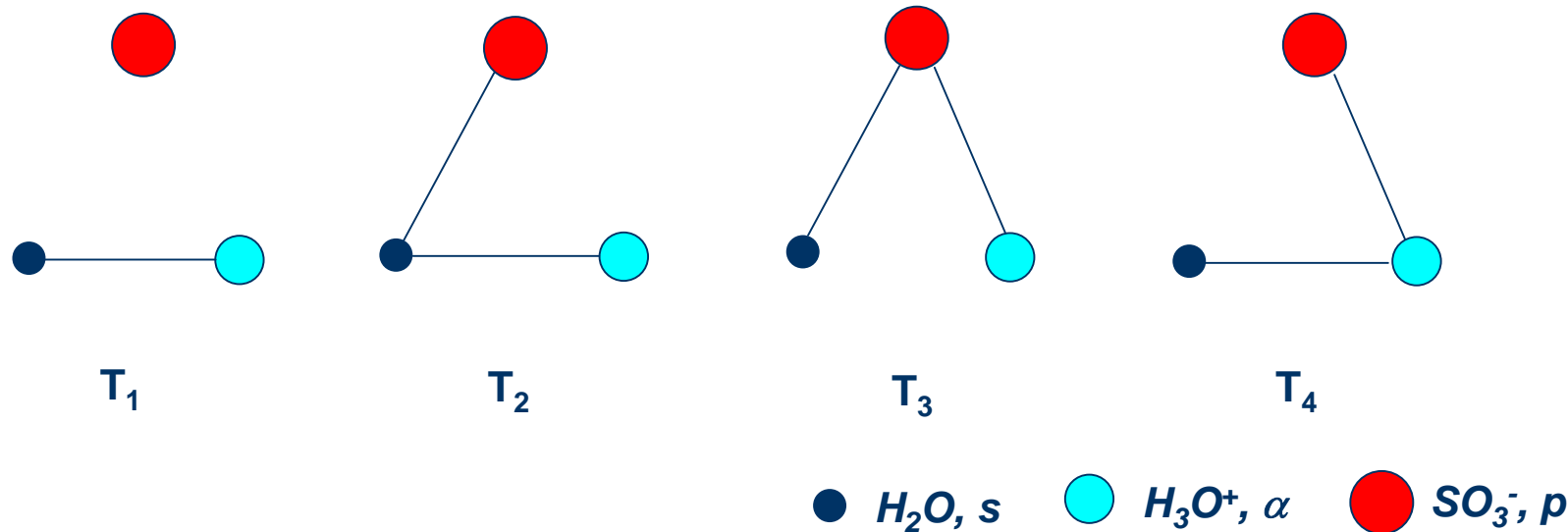
# Complexity: proton diffusion



S.J. Paddison, R. Paul, and T.A. Zawodzinski, in *Proton Conducting Membrane Fuel Cells II*, S. Gottesfeld and T.F. Fuller, Editors, **PV 98-27**, 106-120, The Electrochemical Society Proceedings Series, Pennington, NJ (1999).

# Complexity: proton diffusion

"Friction Coefficient" 
$$= \beta \int_0^\infty dt \langle \vec{F}_{\alpha s} e^{-iL_0 t} \vec{F}_{\alpha s} \rangle_0 + \beta \int_0^\infty dt \langle \vec{F}_{\alpha s} e^{-iL_0 t} \vec{F}_{ps} \rangle_0 + \beta \int_0^\infty dt \langle \vec{F}_{\alpha p} e^{-iL_0 t} \vec{F}_{ps} \rangle_0 + \beta \int_0^\infty dt \langle \vec{F}_{\alpha p} e^{-iL_0 t} \vec{F}_{\alpha s} \rangle_0$$

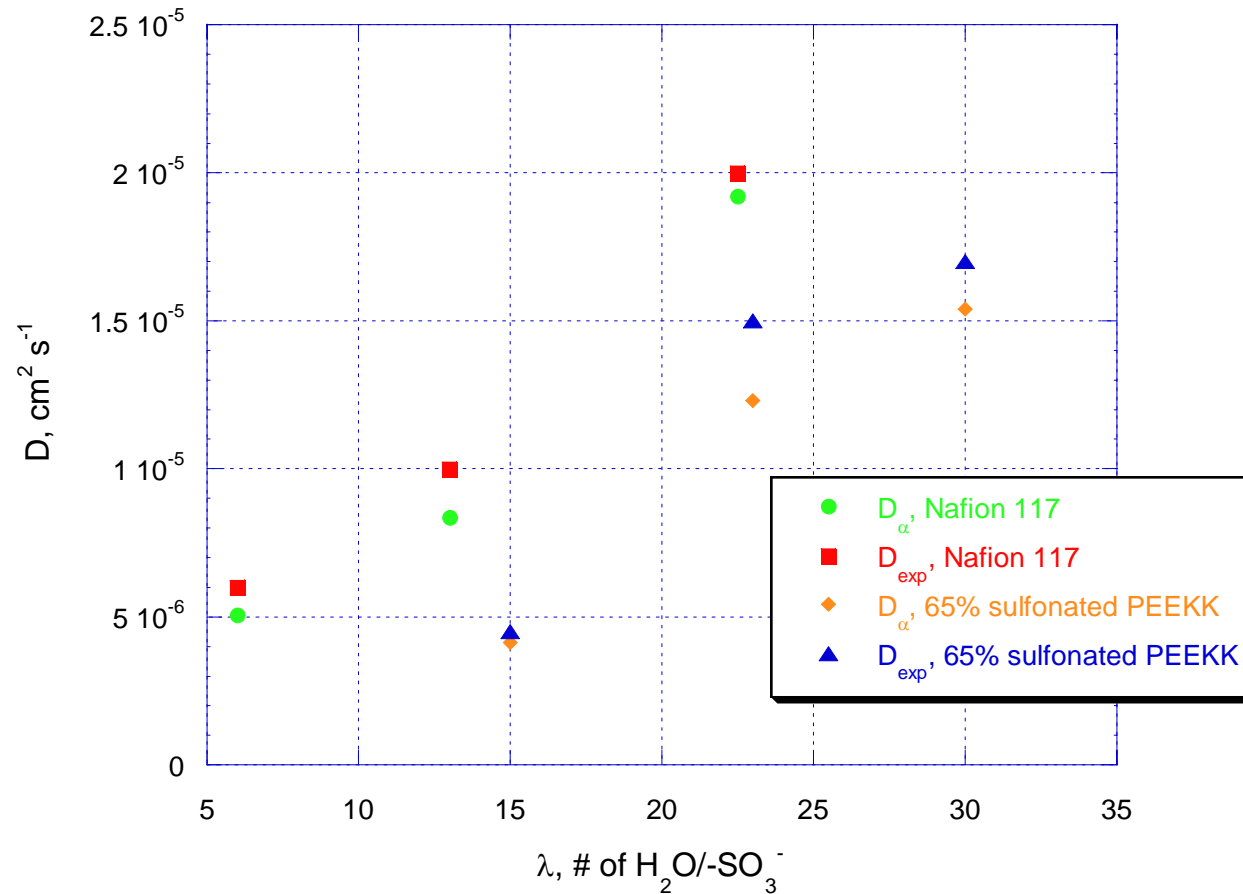


$$\zeta = \zeta^{(0)} + \zeta^{(c)}$$

Einstein Relation  $\Rightarrow D_\alpha = \frac{kT}{\zeta_\alpha}$

S.J. Paddison, R. Paul, and T.A. Zawodzinski Jr., *J. Electrochem. Soc.*, **147**, 617 (2000).

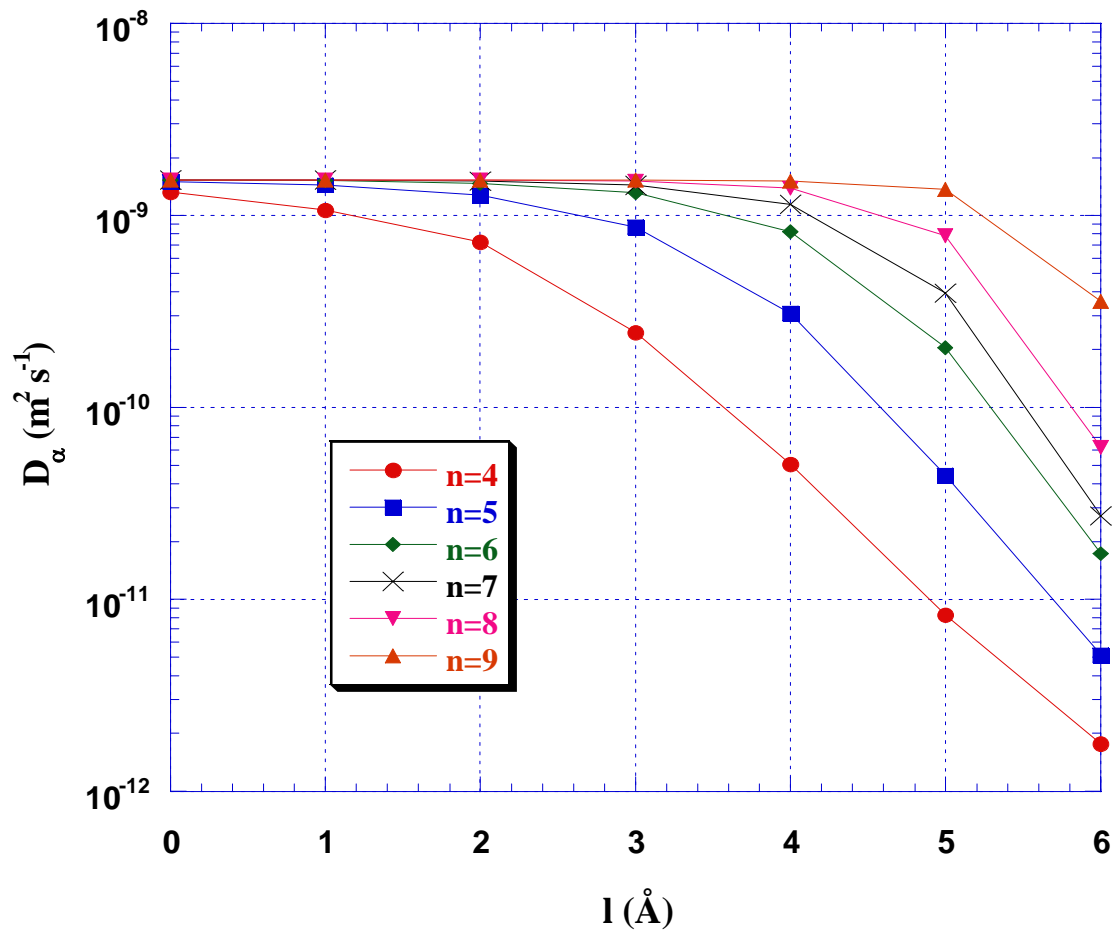
# Complexity: proton diffusion



S. J. Paddison, *Handbook of Fuel Cells – Fundamentals, Technology and Applications*, W. Vielstich, A. Lamm, and H. Gasteiger, Editors-in-Chief, Chapter 31, pp. 396-411, J. Wiley and Sons Ltd, Chichester (2003).

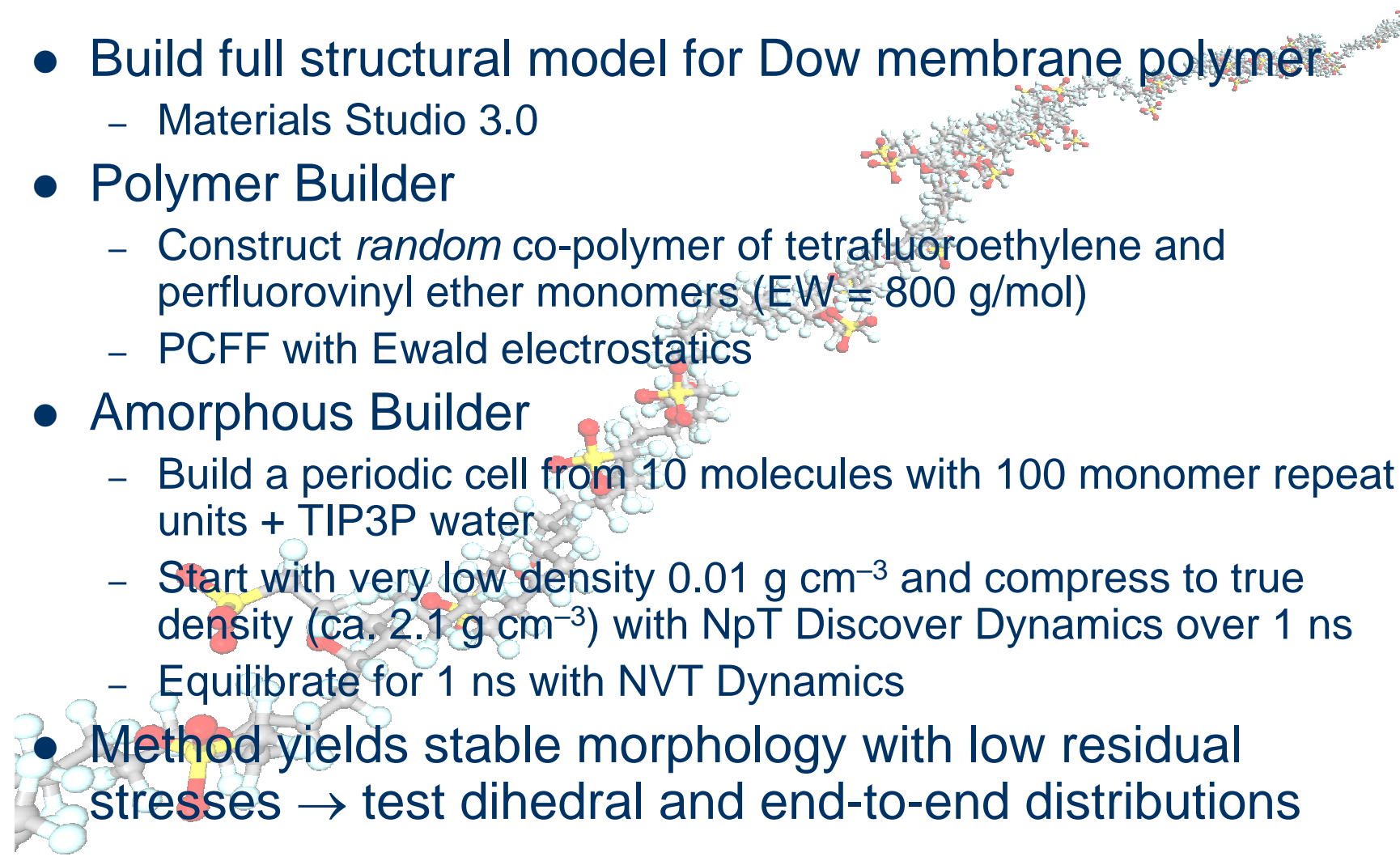
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# Complexity: proton diffusion



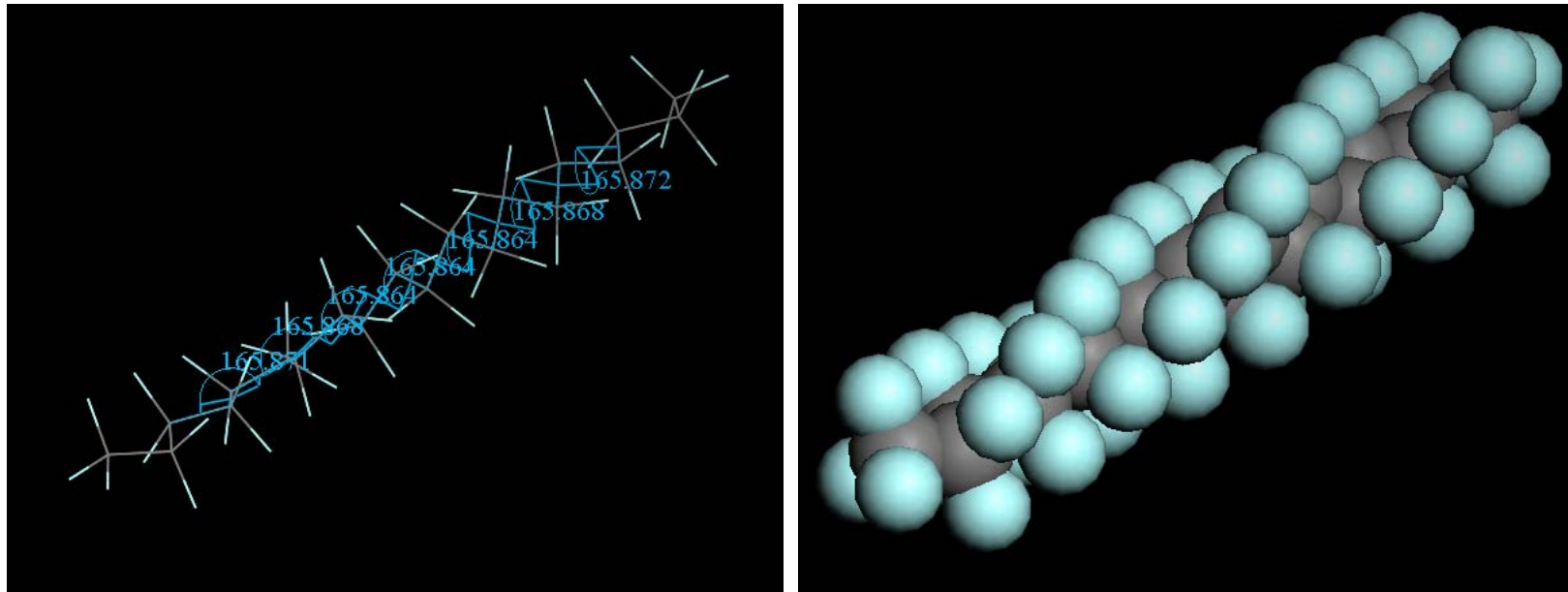
S. J. Paddison and R. Paul, *J. Chem. Phys.*, **115**, 7753 (2001).

# Molecular mechanics modelling of Dow polymer

- Build full structural model for Dow membrane polymer
    - Materials Studio 3.0
  - Polymer Builder
    - Construct *random* co-polymer of tetrafluoroethylene and perfluorovinyl ether monomers (EW = 800 g/mol)
    - PCFF with Ewald electrostatics
  - Amorphous Builder
    - Build a periodic cell from 10 molecules with 100 monomer repeat units + TIP3P water
    - Start with very low density  $0.01 \text{ g cm}^{-3}$  and compress to true density (ca.  $2.1 \text{ g cm}^{-3}$ ) with NpT Discover Dynamics over 1 ns
    - Equilibrate for 1 ns with NVT Dynamics
  - Method yields stable morphology with low residual stresses → test dihedral and end-to-end distributions
- 

# Perfluoroalkane dihedral distribution

- Fluorines induce a helical pitch in backbone ( $\phi = 165^\circ$ ) for an unsubstituted, isolated oligomeric chain

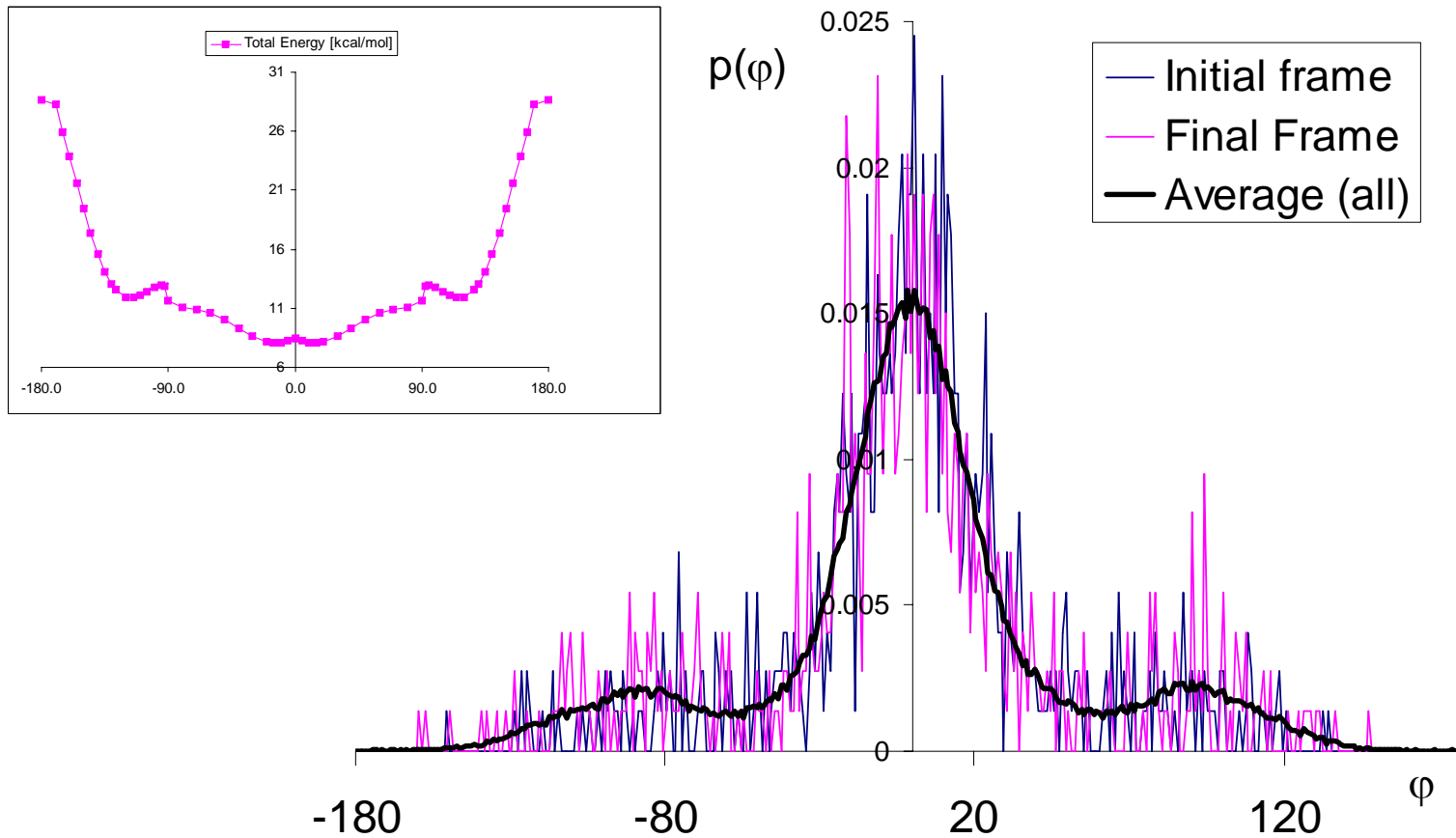


- In PTFE, *trans* and *gauche* states are known to ‘split’
-



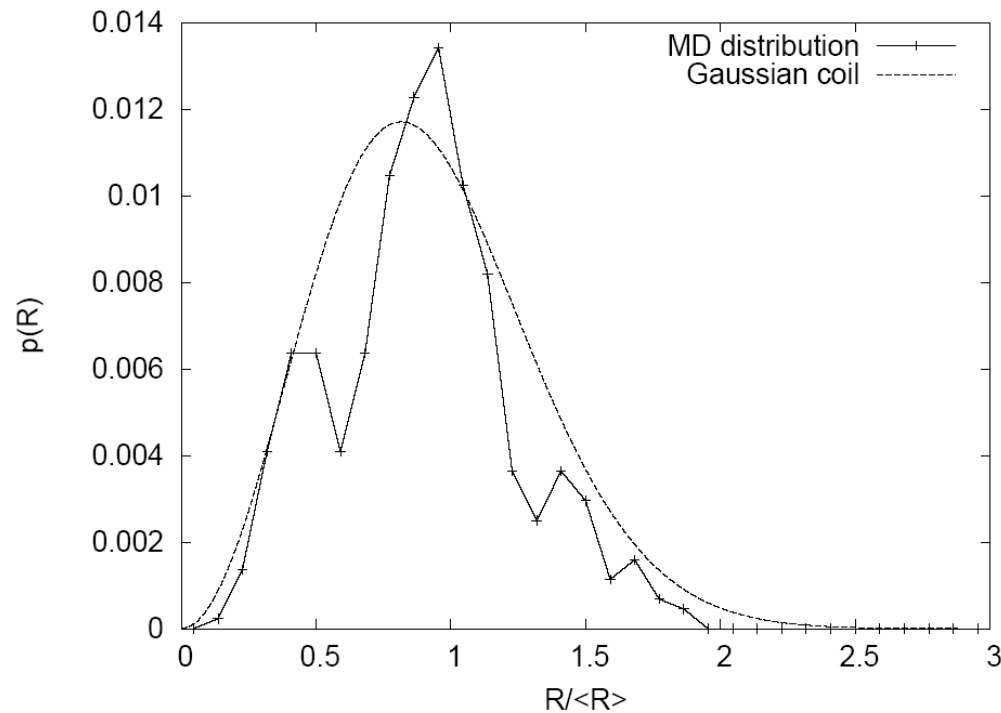
# Perfluoroalkane dihedral distribution

- Dihedral angle distribution from MD simulations



# Perfluoroalkane end-to-end distributions

- For Gaussian coils,



$$p(r_{ij}) = \left( \frac{3}{2\pi \langle r_{ij}^2 \rangle} \right)^{3/2} \exp\left( -\frac{3r_{ij}^2}{2\langle r_{ij}^2 \rangle} \right)$$

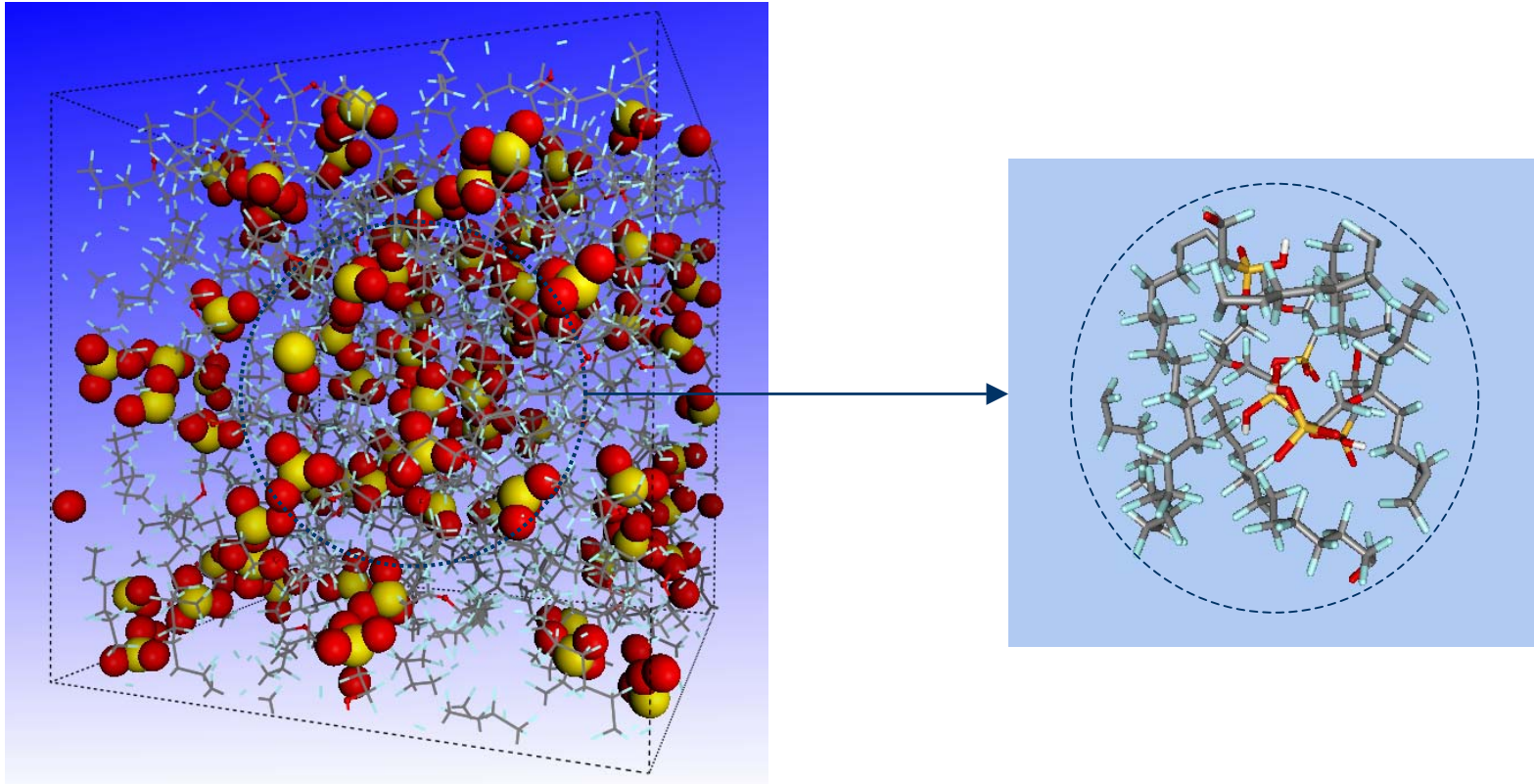
$$C_\infty[\text{PTFE @ 300 K}] \approx 11$$

$$\therefore \sqrt{\langle R^2 \rangle} \approx 8.5 \text{ nm for } N = 100$$

$$\text{c.f. } \sqrt{\langle R^2 \rangle} = 9.8 \text{ nm from MD}$$

- Chain trajectories are reasonably well relaxed
-

# Dow membrane – multi-scale modeling



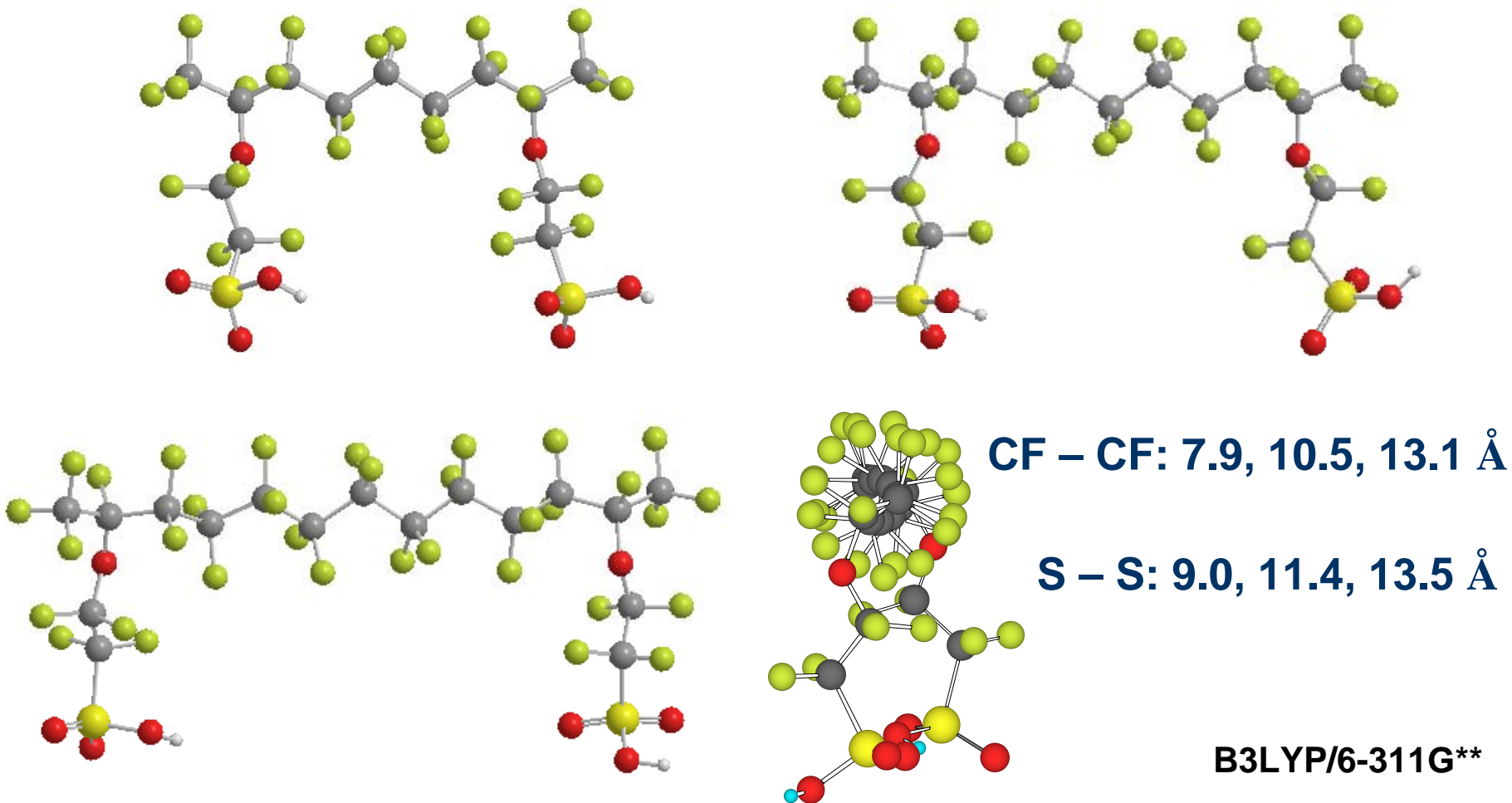
- predict morphology to understand proton transport

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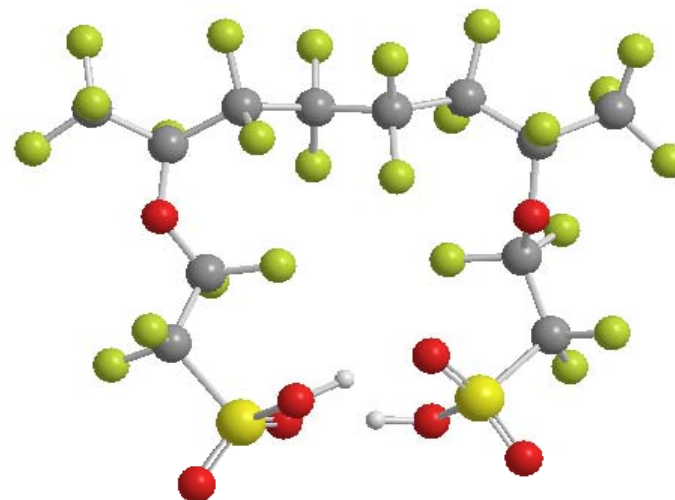
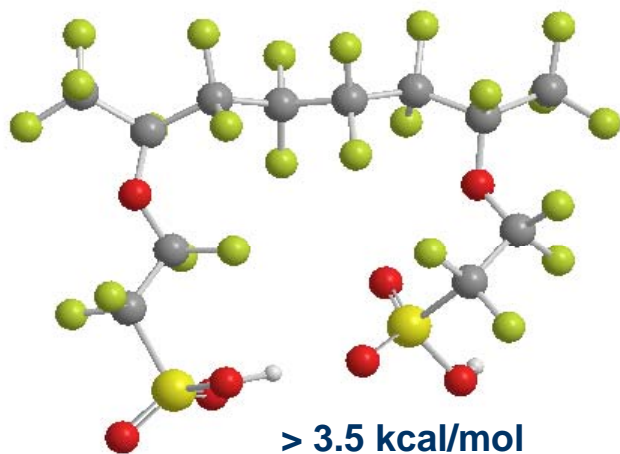
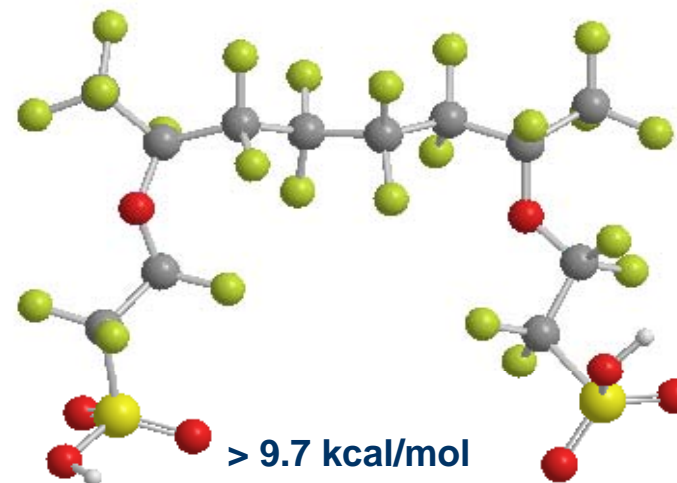
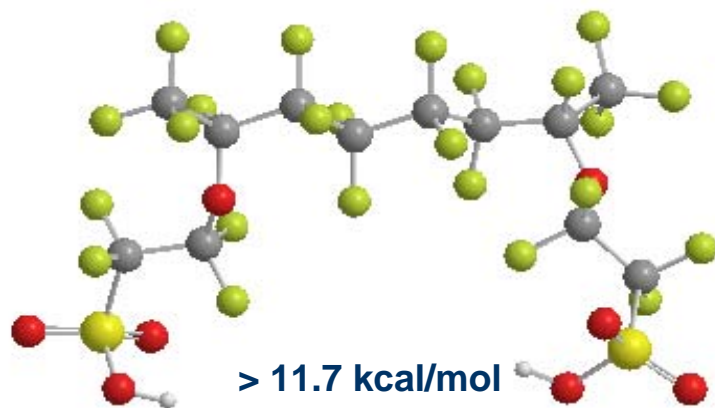
# Dow membrane – molecular modeling

- (1) How does side-chain separation affect **connectivity** of neighboring sulfonic acid groups?
  - (2) How does side-chain separation affect amount of water required to affect proton transfer and separation (i.e. **complexity**)?
  - (3) Does side chain separation influence side chain and/or backbone conformation (i.e. **cooperativity**)?
-

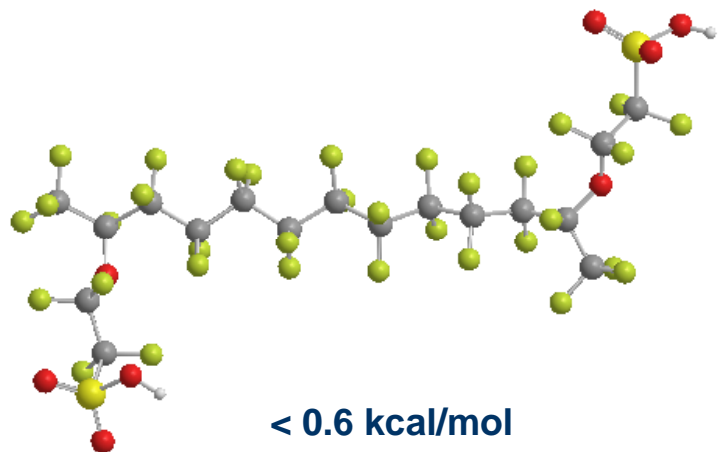
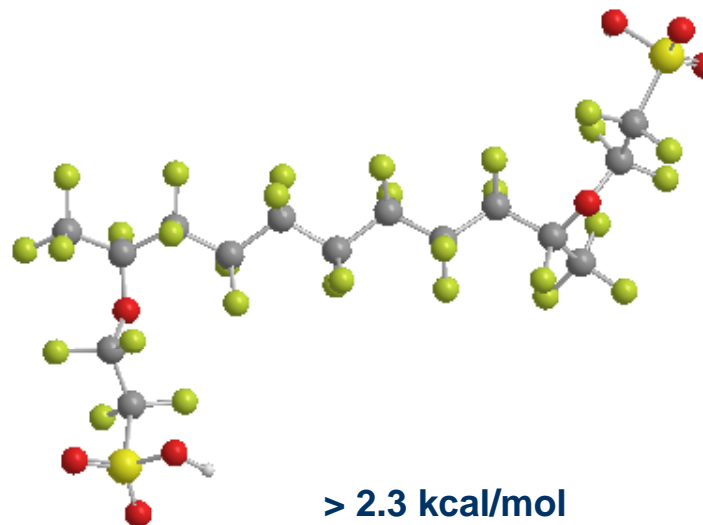
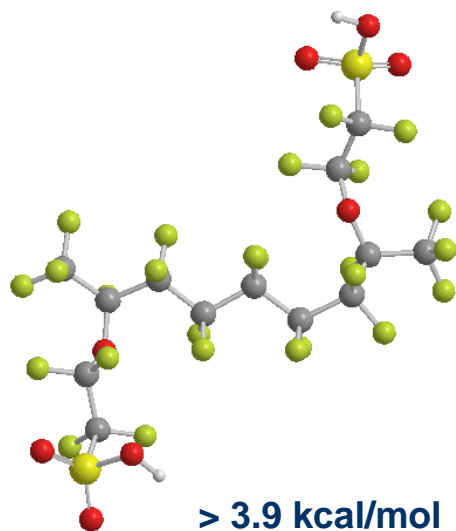
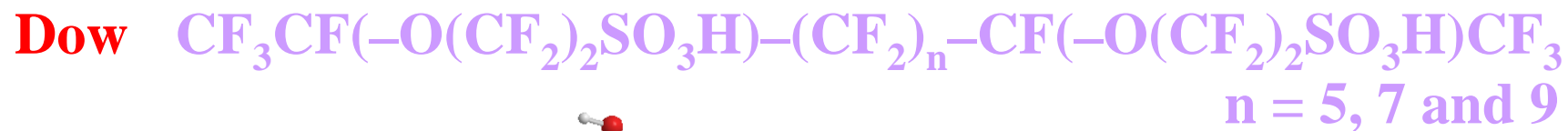
# Connectivity: ?



# Connectivity: ?



# Cooperativity: ?



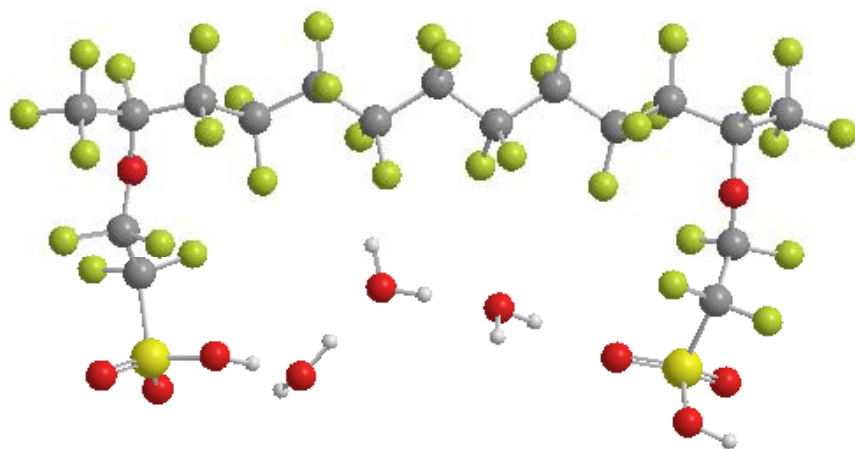
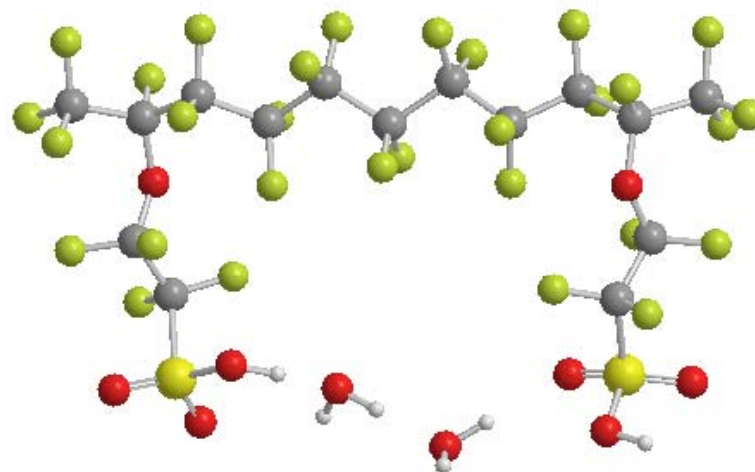
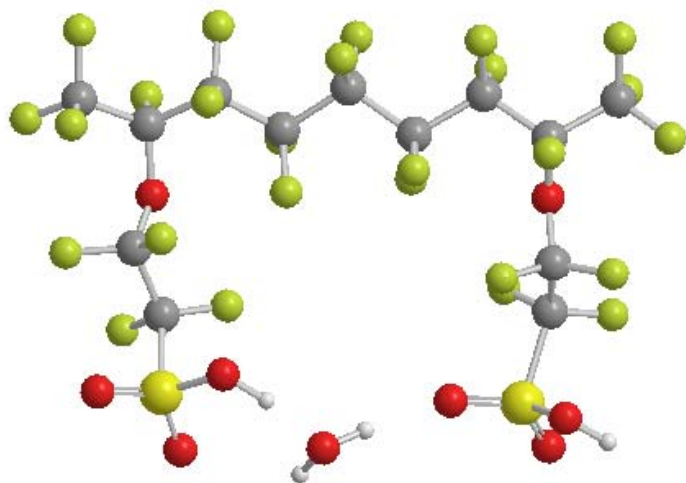
**CF – CF: 7.2, 10.5, 13.1 Å**

**S – S: 13.8, 16.6, 18.2 Å**

**B3LYP/6-311G\*\***



# Connectivity: water hydrogen bonding



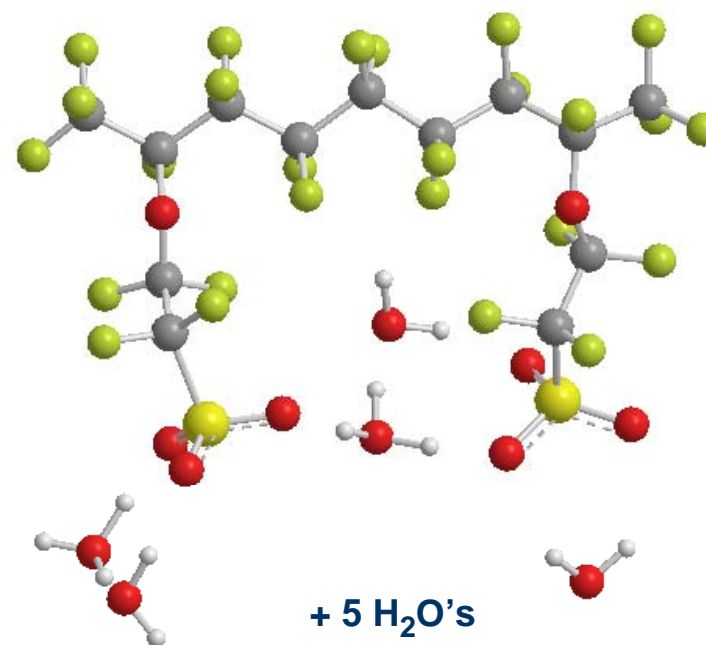
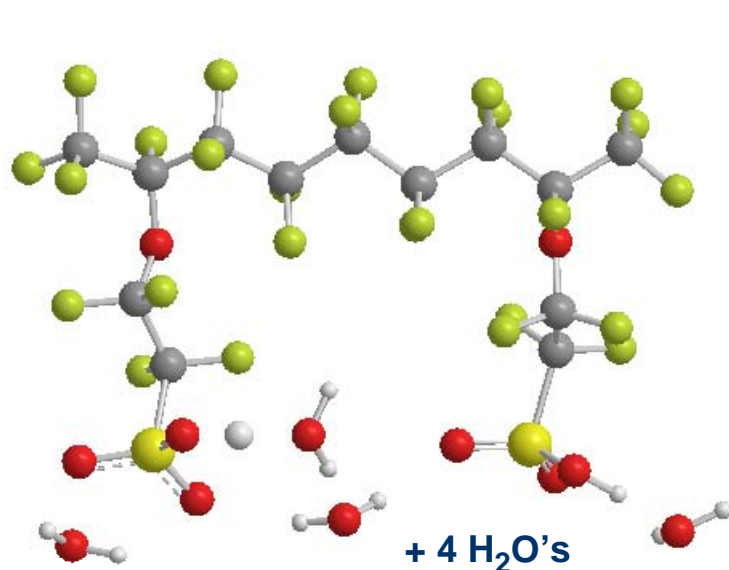
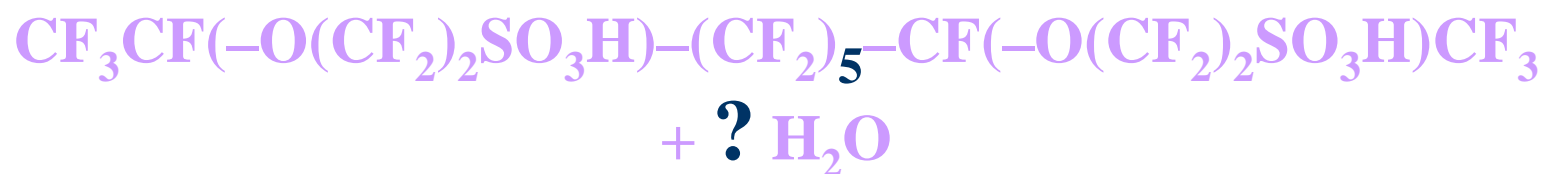
CF – CF: 7.9, 10.5, 13.1 Å

S – S: 7.2, 9.4, 11.5 Å

B3LYP/6-311G\*\*



# Complexity: proton dissociation

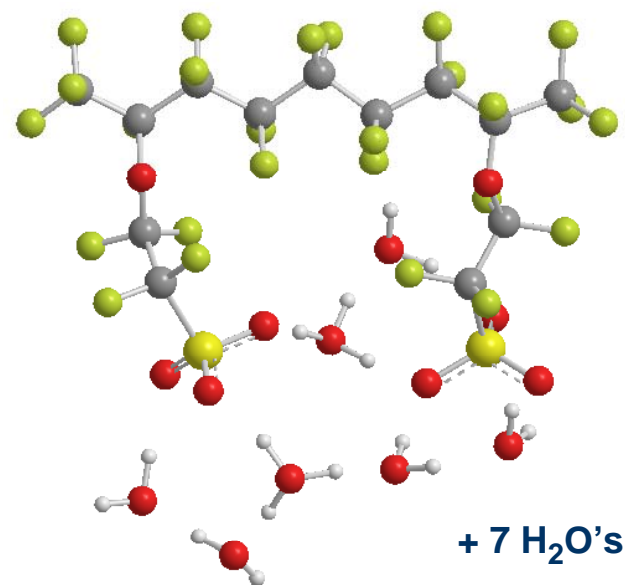
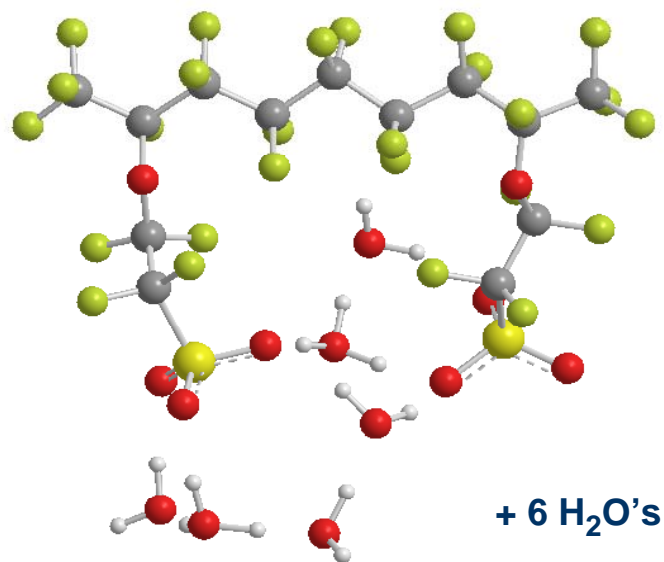
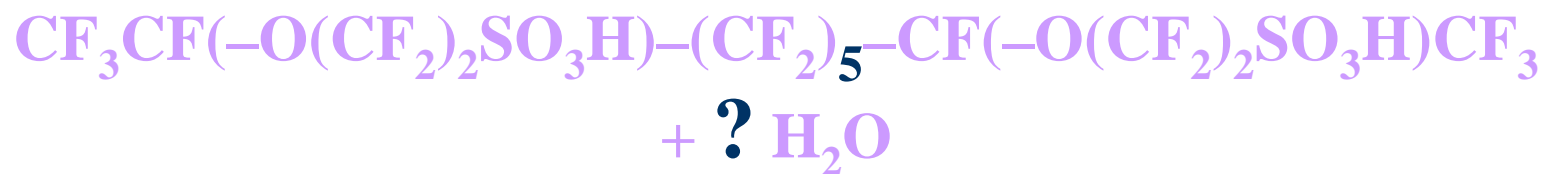


CF – CF: 7.9, 7.6 Å

S – S: 7.5, 7.0 Å

B3LYP/6-311G\*\*

# Complexity: proton separation

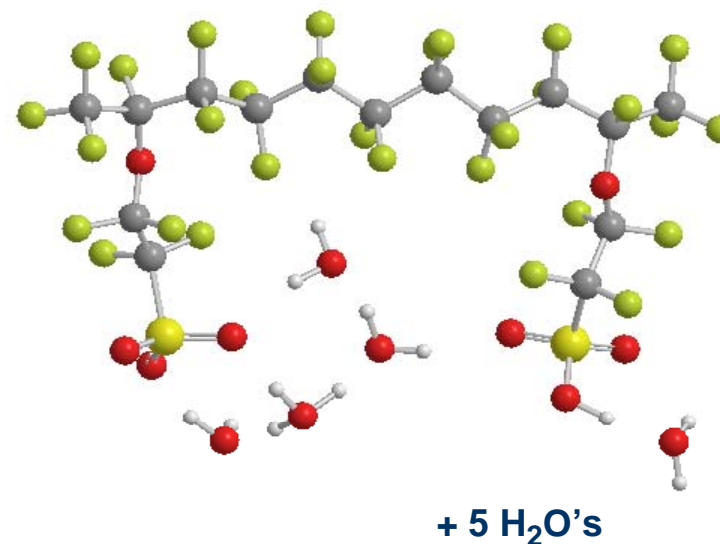
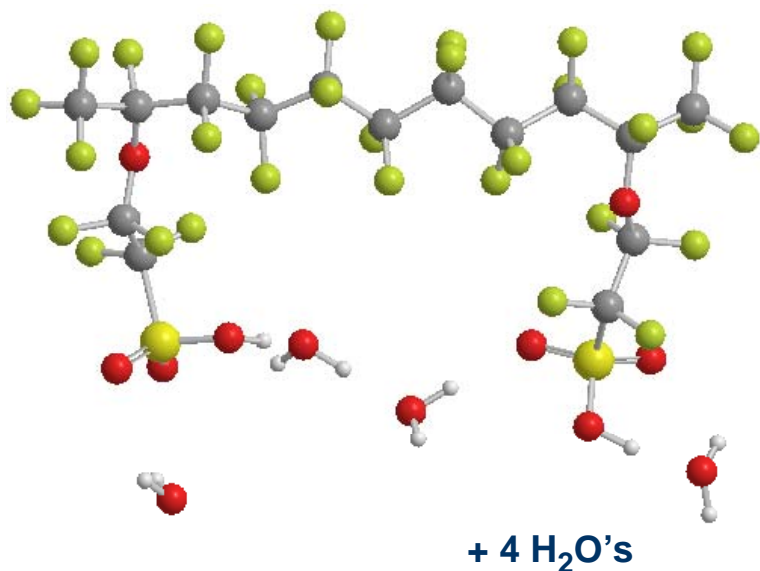
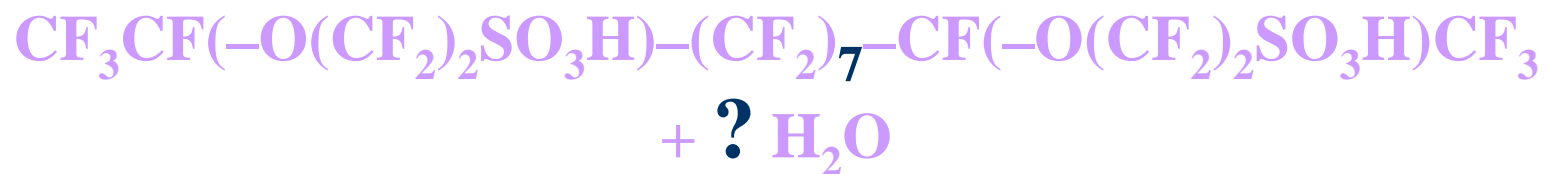


CF – CF: 7.8, 7.8 Å

S – S: 6.5, 6.3 Å

B3LYP/6-311G\*\*

# Complexity: proton dissociation

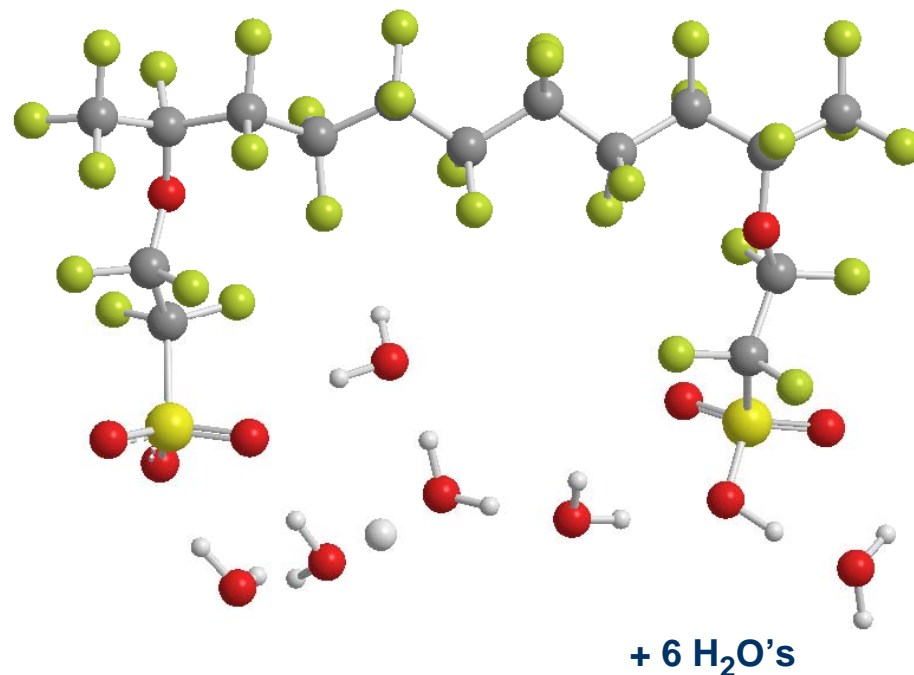
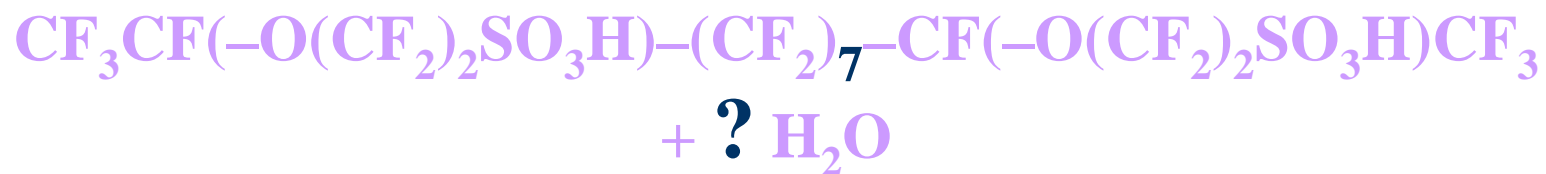


CF – CF: 10.5, 10.5 Å

S – S: 9.2, 9.0 Å

B3LYP/6-311G\*\*

# Complexity: proton dissociation



CF – CF: 10.5 Å

S – S: 10.2 Å

B3LYP/6-311G\*\*

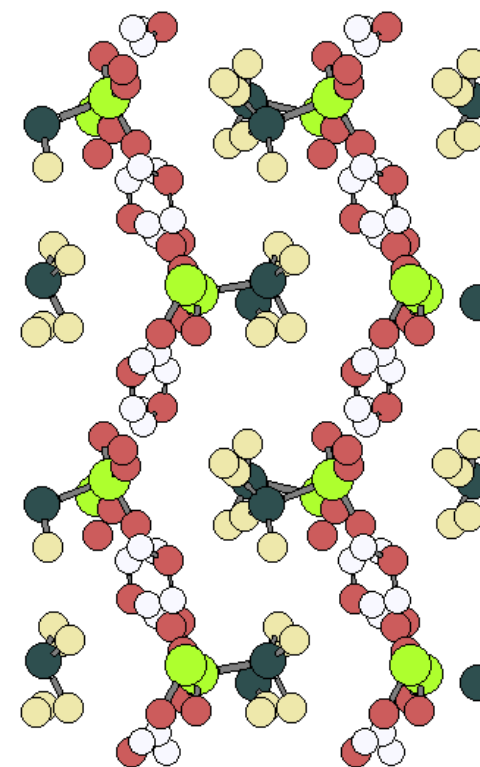
# Complexity: conduction under minimal hydration

## Triflic Acid Monohydrate Solid

J.B. Spencer and J.-O. Lundgren, *Acta Cryst.*, **B29**, 1923 (1973).

$4 \times (\text{CF}_3\text{SO}_3\text{H} \cdot \text{H}_2\text{O})$ :  $a=5.9634$ ,  $b=9.975$ ,  $c=9.708 \text{ \AA}$ ,  $\beta=98.661^\circ$

with  $\kappa = 0.96281 \text{ Sm}^{-1}$  @ 309.15 K, diffusion of a proton  $\Rightarrow$



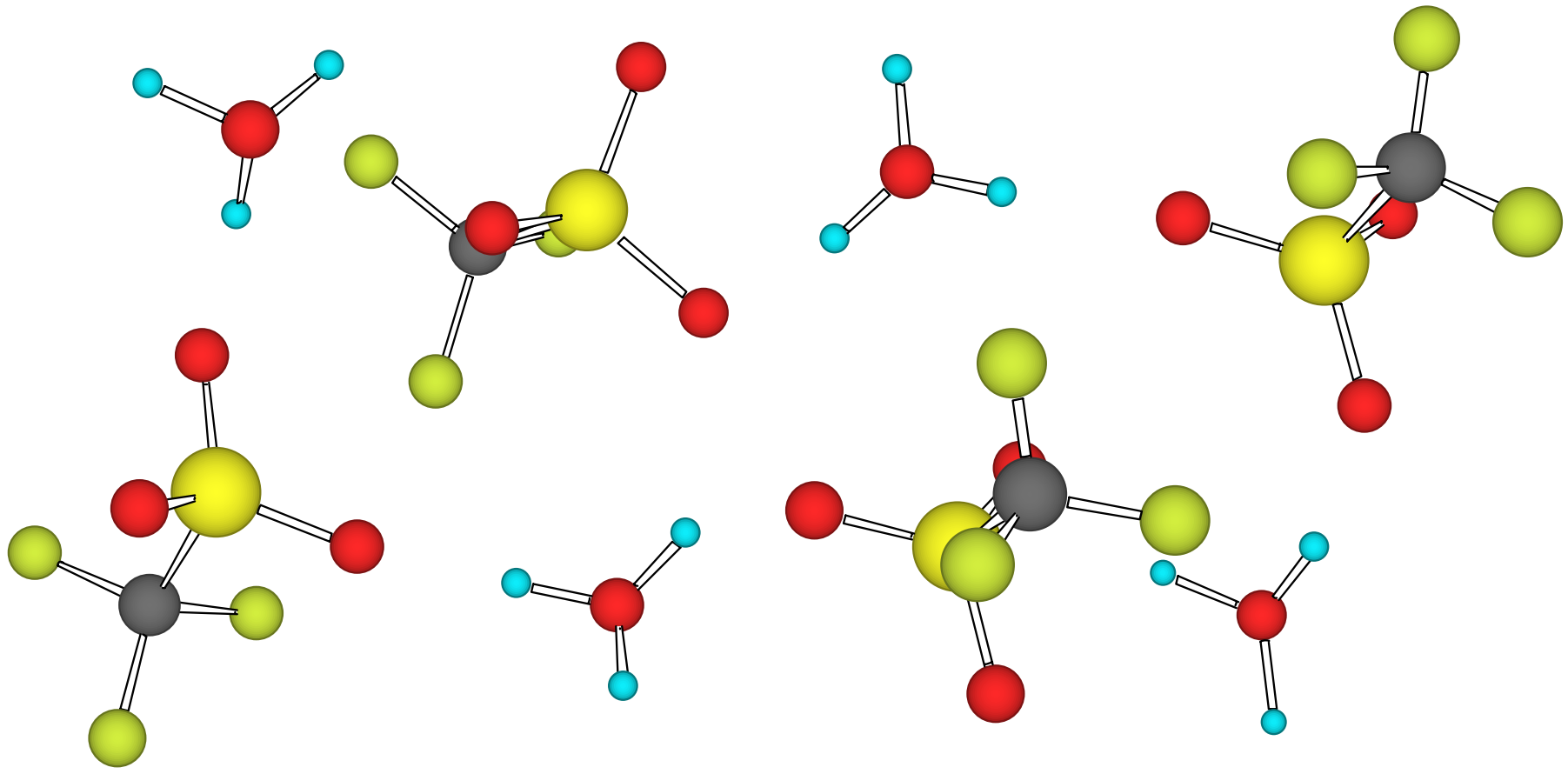
**AIMD**

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M. Eikerling, S.J. Paddison, L. R. Pratt, and T.A. Zawodzinski Jr., *Chem. Phys. Lett.* **368**, 108 (2003).

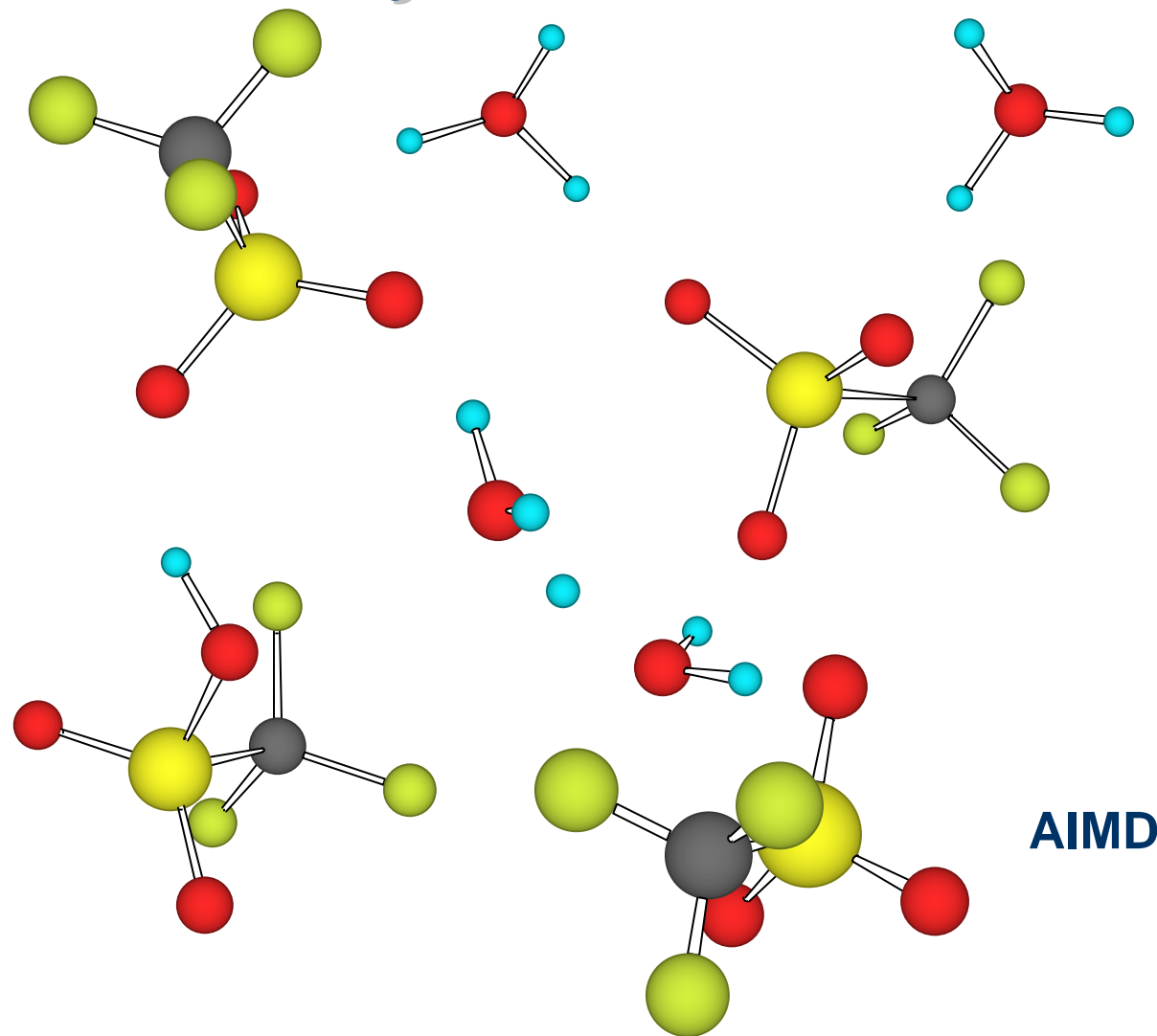
# Trifluoromethanesulfonic acid monohydrate

- expanded unit cell



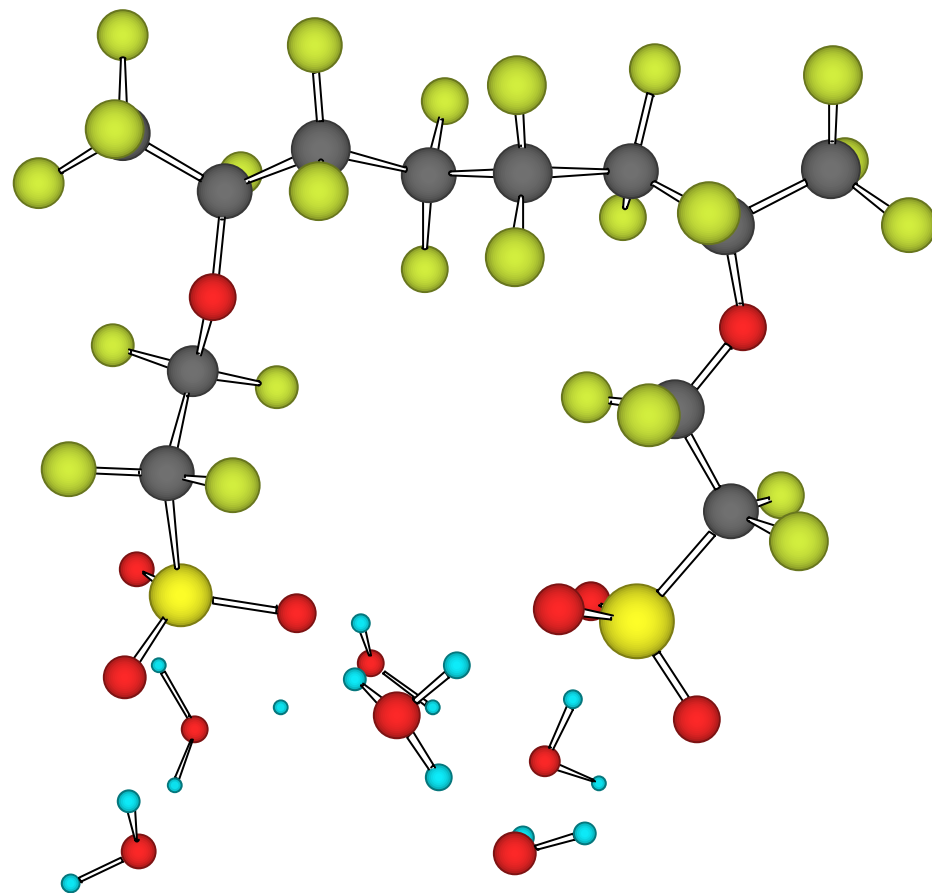
# Trifluoromethanesulfonic acid monohydrate

• defect state



$$\Delta G_f = 0.2 \text{ eV}$$

# Dow Membrane with two side chains + 6 H<sub>2</sub>O



B3LYP/6-31G\*\*

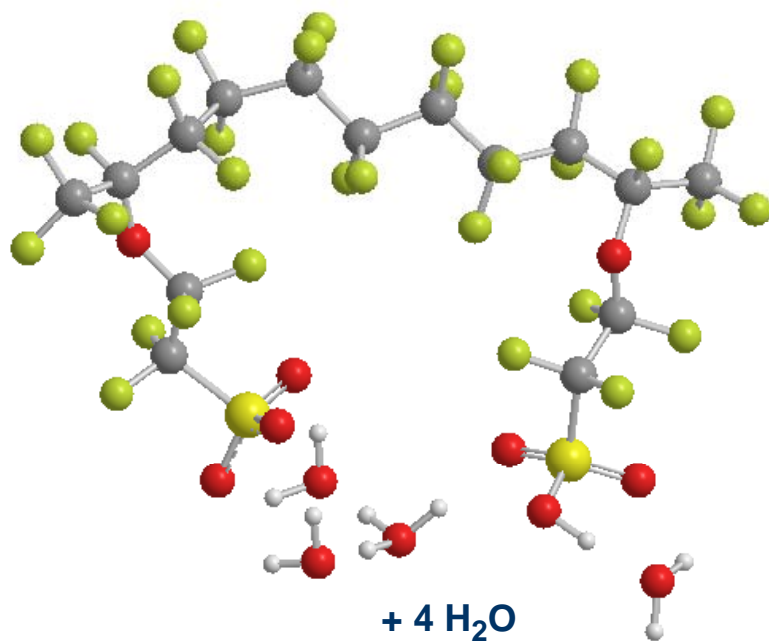
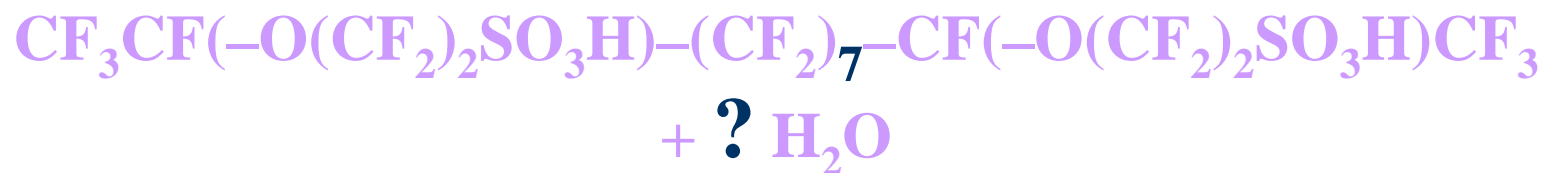
Acidic protons: H<sub>3</sub>O<sup>+</sup> & H<sub>5</sub>O<sub>2</sub><sup>+</sup>

S.J. Paddison, "Proton conduction mechanisms in Polymer Electrolyte Membranes at low degrees of hydration", Volume 33, *Annual Review of Materials Research*, 289-319 (2003).

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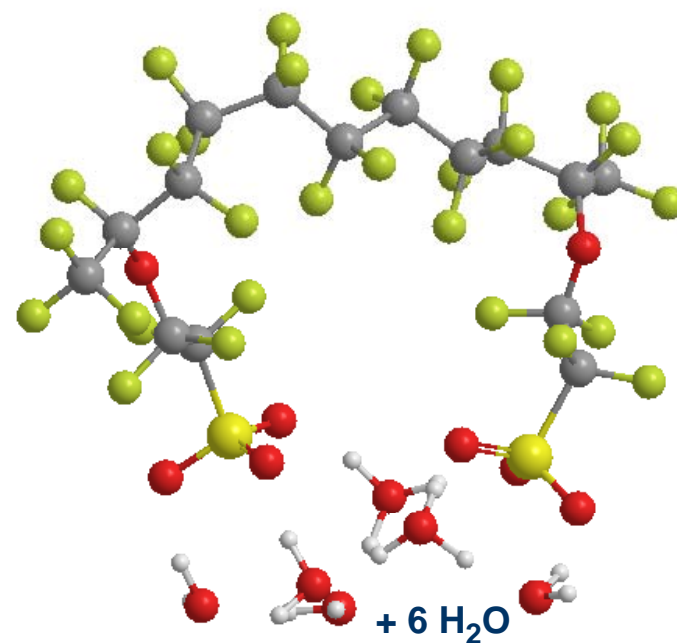


# Complexity & cooperativity: proton dissociation



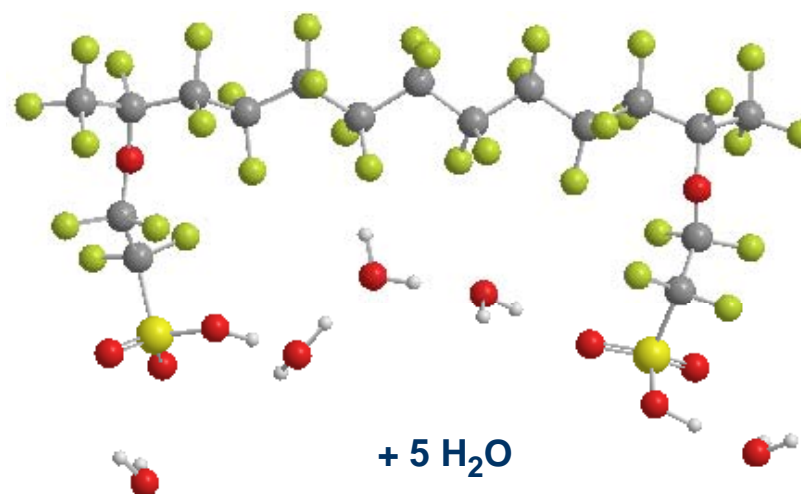
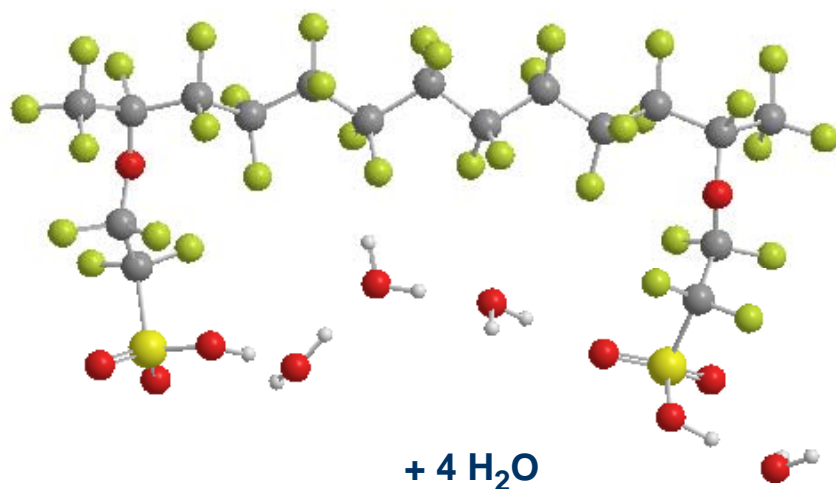
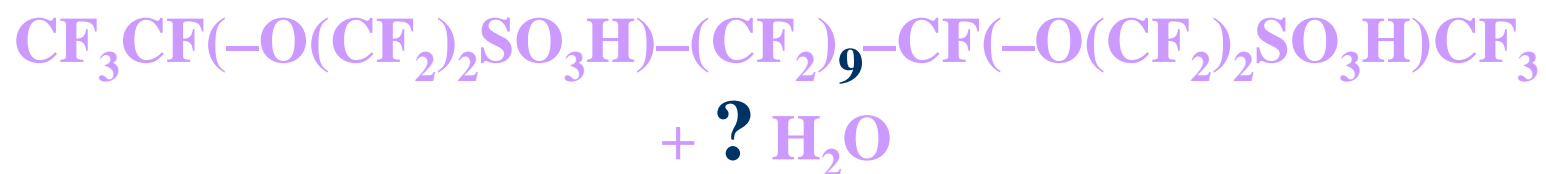
CF – CF: 9.7, 9.4 Å

S – S: 6.1, 5.8 Å



B3LYP/6-311G\*\*

# Complexity: proton dissociation

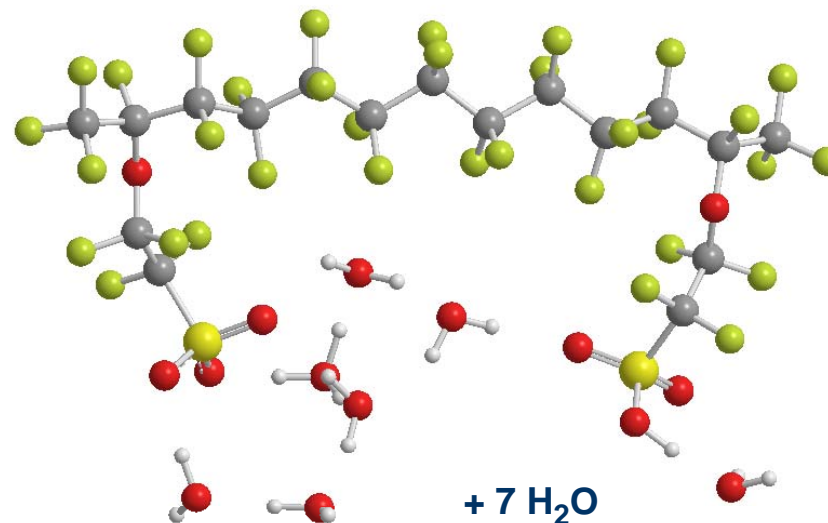
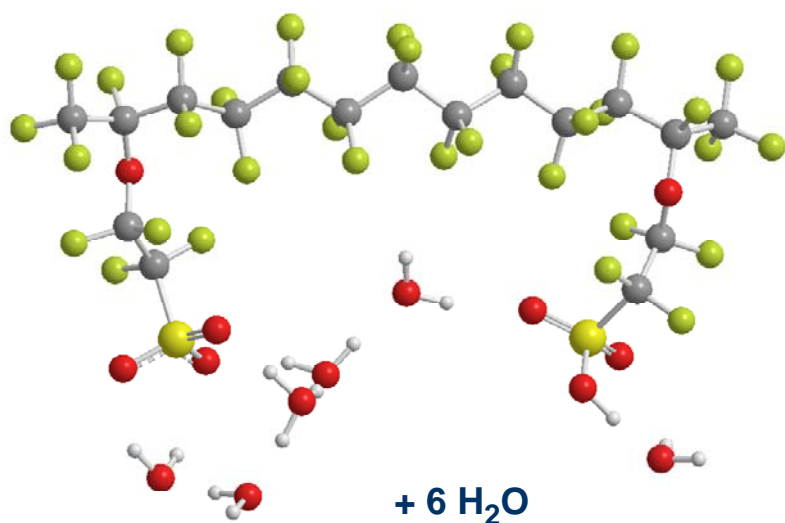
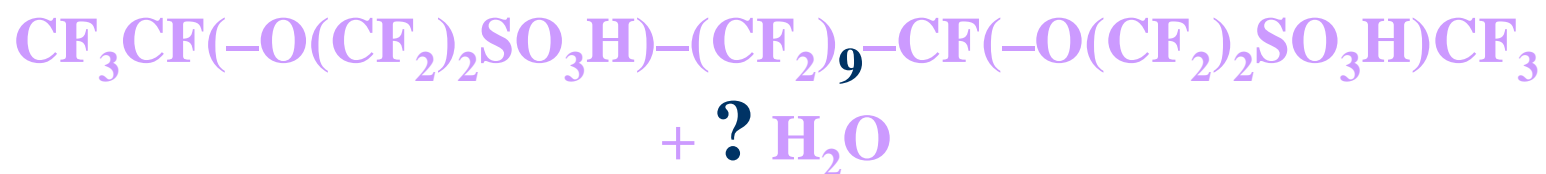


CF – CF: 13.1, 13.1 Å

S – S: 11.5, 11.4 Å

B3LYP/6-311G\*\*

# Complexity: proton dissociation



CF – CF: 13.0, 13.0 Å

S – S: 9.7, 9.6 Å

B3LYP/6-311G\*\*

# Summary

- The extent of separation of the side chains affects the **connectivity** of the sulfonic acid groups via a hydrogen bond network with the first hydration shell water.
  - Proton dissociation (i.e. **complexity**) is affected by the separation of the sulfonic acid groups.
    - influenced by conformational change in the backbone and/or side chains (**cooperativity**)
  - The molecular results provide a 'base-line' set of results for which the effects of distinct: acidic groups, side chain length and polymer chemistry may be examined.
-