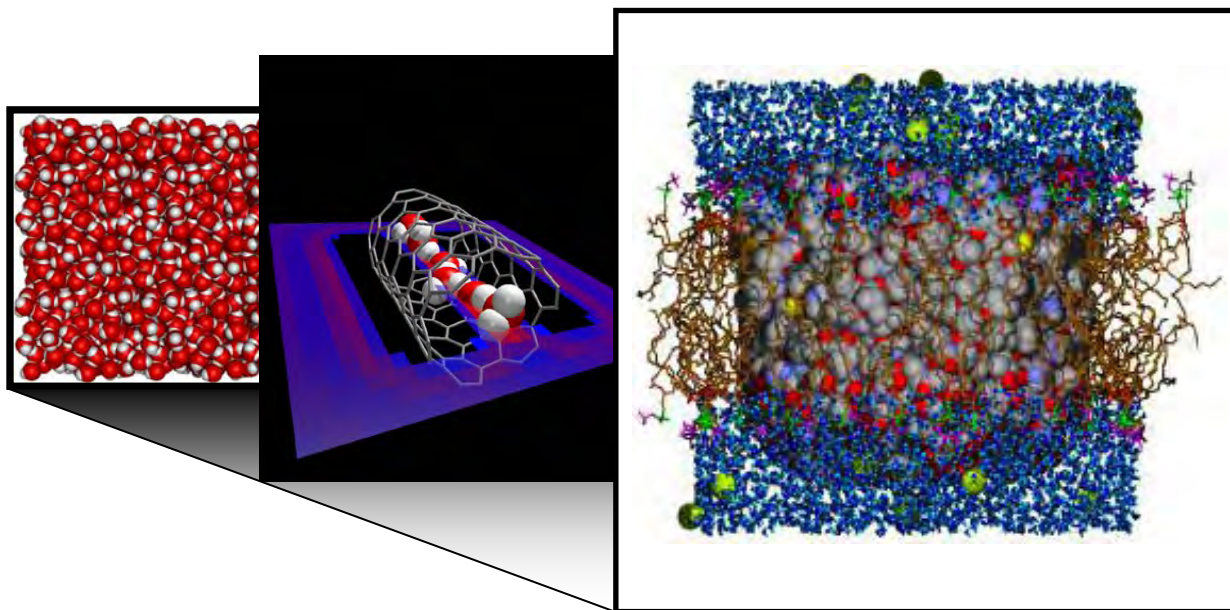


# Water Mediated Proton Conduction: from Nanotubes to Cytochrome c Oxidase

Gerhard Hummer

Laboratory of Chemical Physics, NIDDK

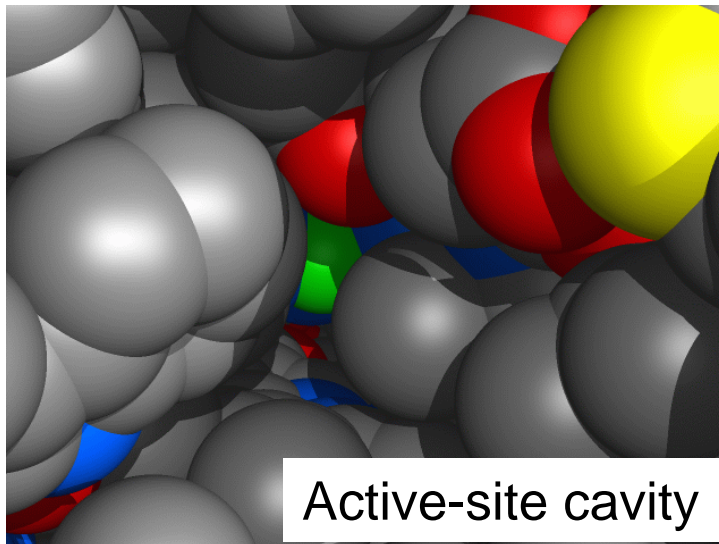
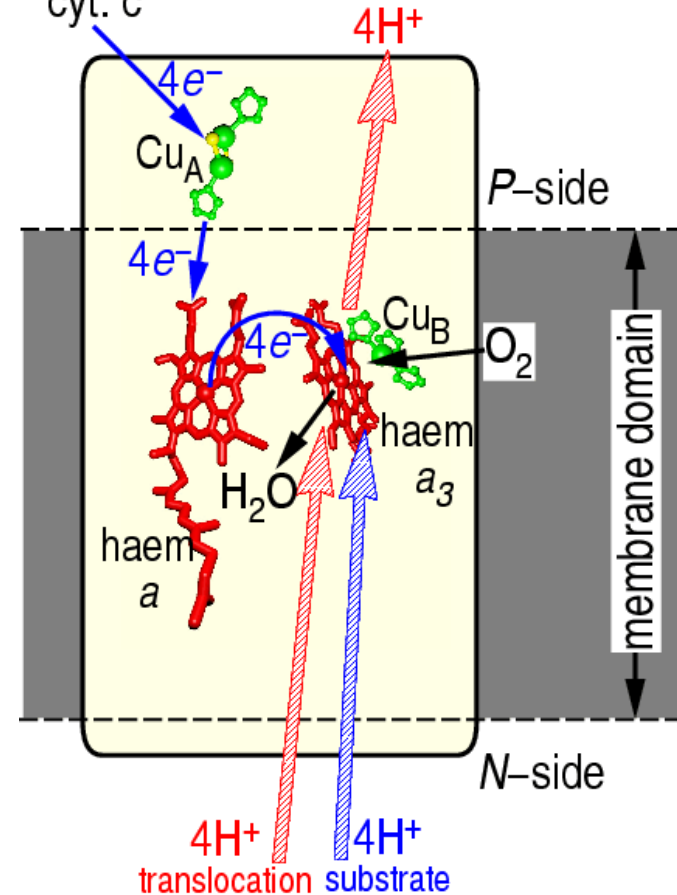
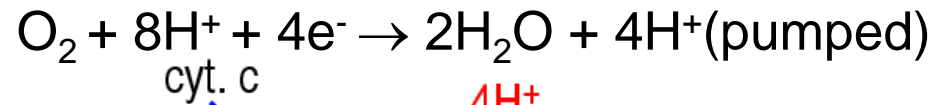
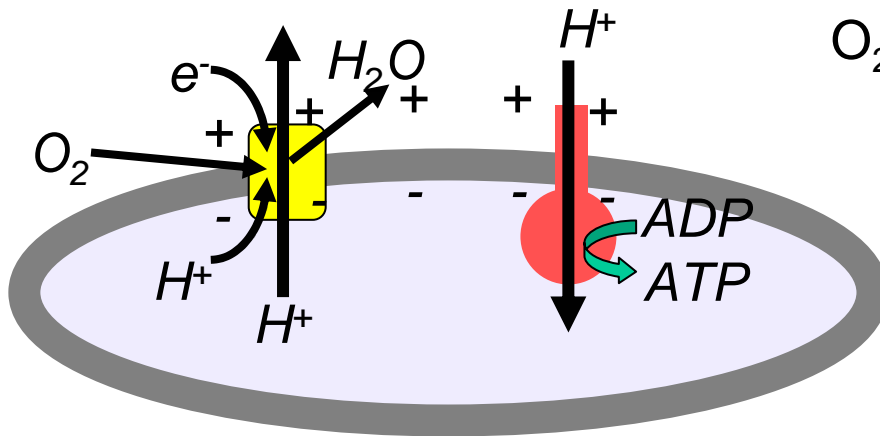
National Institutes of Health, Bethesda, MD 20892, USA



Gerhard.Hummer@nih.gov

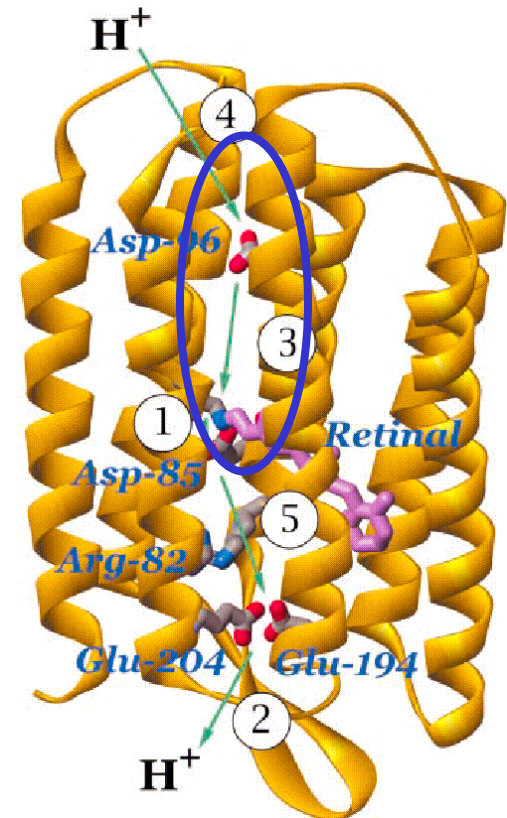
(Department of Health and Human Services)

# Biological "Fuel Cell": Proton Pump Cytochrome c Oxidase



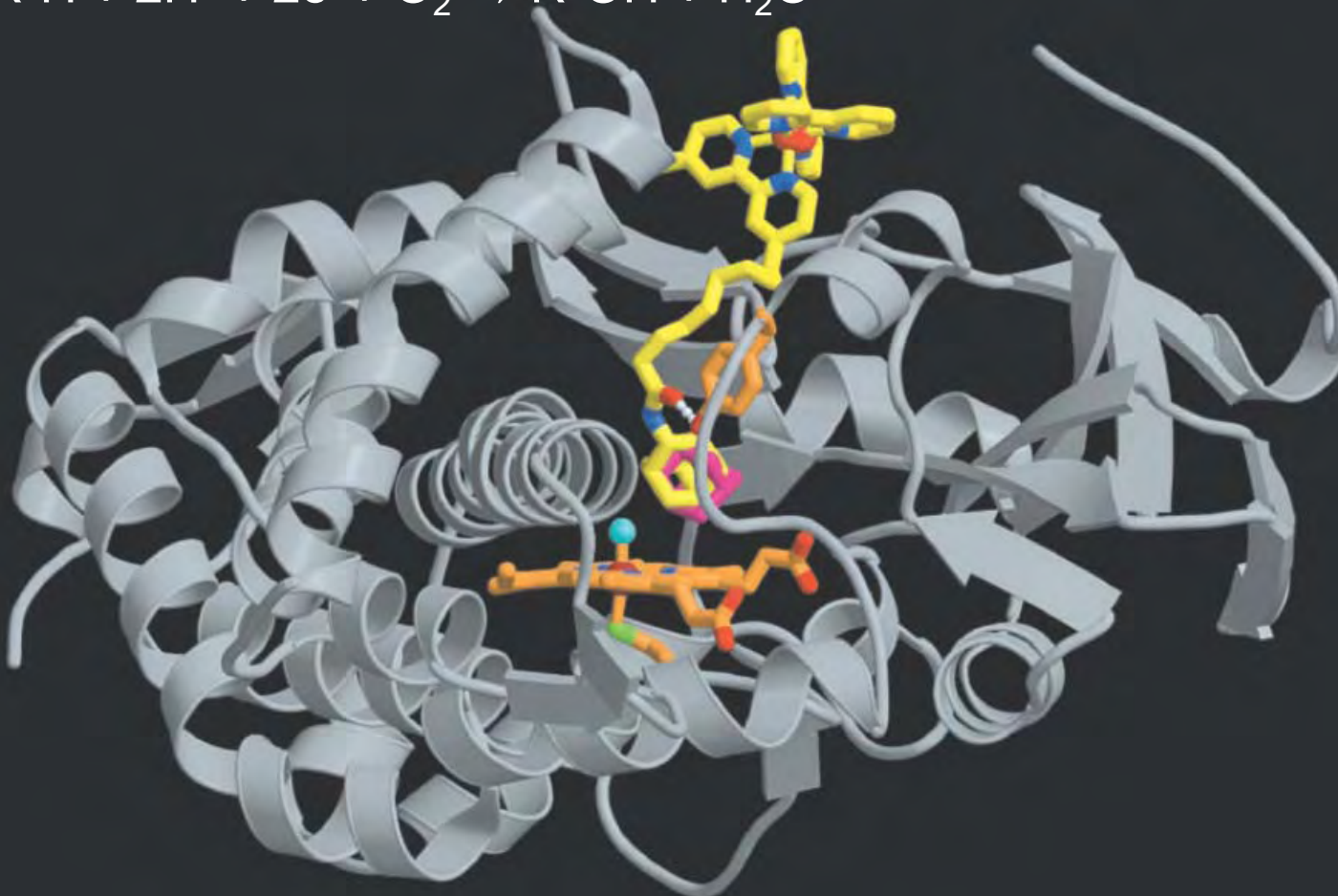
# Bacteriorhodopsin – “Bio-Solar Cell”

- Energy of absorbed photons used to pump protons across membrane
- Hydrophobic proton access channel on cytoplasmic side



(Luecke, Richter and Lanyi, *Science* **289**, 1934, 1998)

# Cytochrome P450: “Bio-Chemistry”



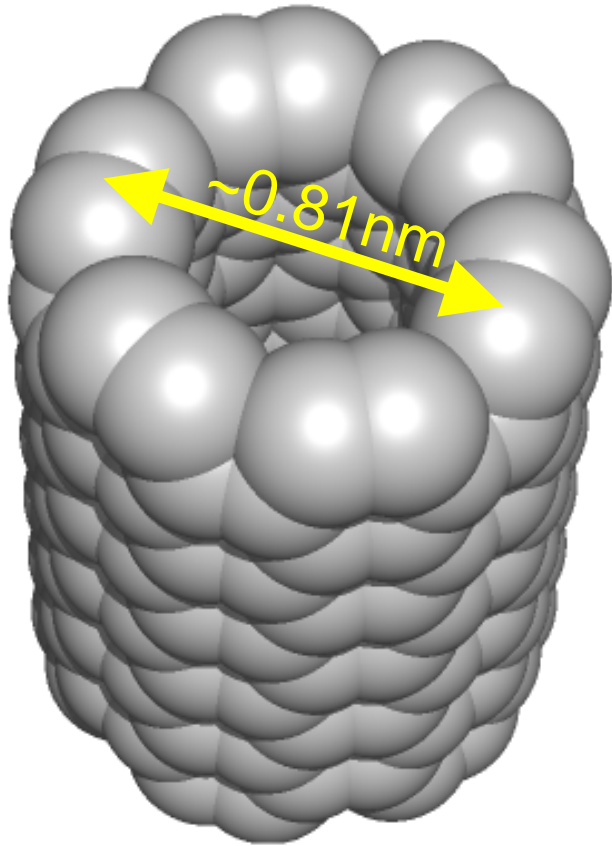
Dmochowski et al., Proc. Natl. Acad. Sci. USA, 96, 12987, 1999)

# Objectives: Role of Water in Biological Proton Transfer



1. Does water fill hydrophobic (i.e., “water repelling”) proton access channels?
2. What are the thermodynamic, dynamic, and structural properties of such molecularly confined water molecules?
3. Can water-filled nonpolar channels provide efficient mediators for proton transfer?
4. Role of protein and solvent dynamics in biological proton transfer

# 1. Does water fill nonpolar channels? Carbon Nanotube as Simplest Nonpolar Molecular Channel

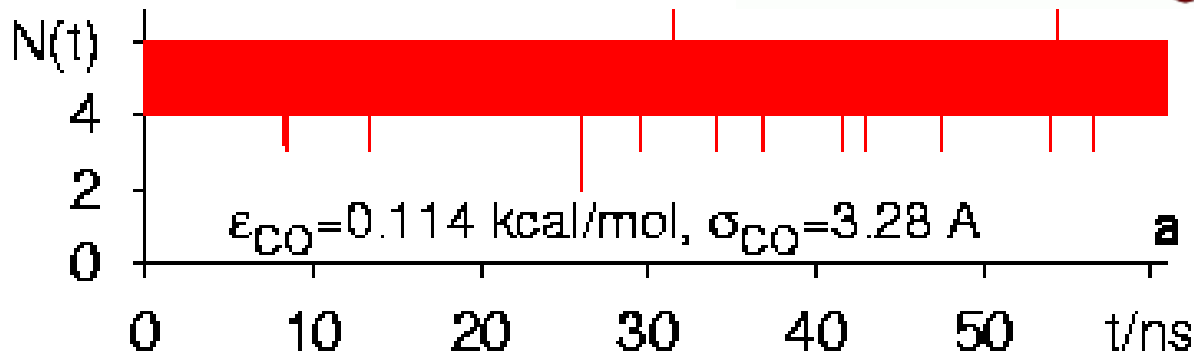
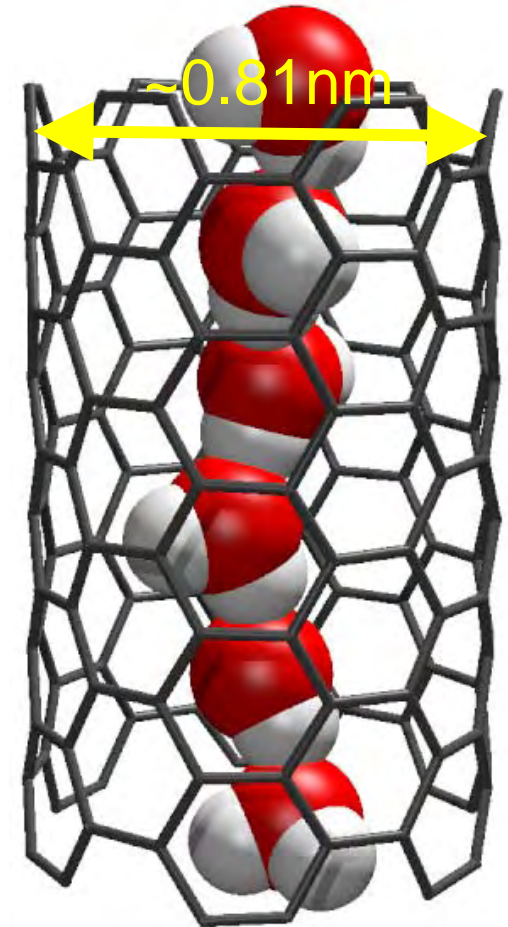
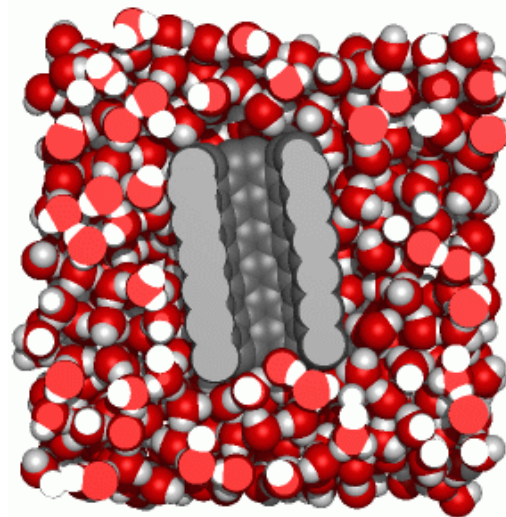


- Fullerene-type cylindrical molecules
- $sp^2$  carbons in 'honeycomb' lattice
- Open or closed ends
- Single or multi-wall structure
- Diameters of  $\sim 1$  nm and larger
- Chemically functionalizable

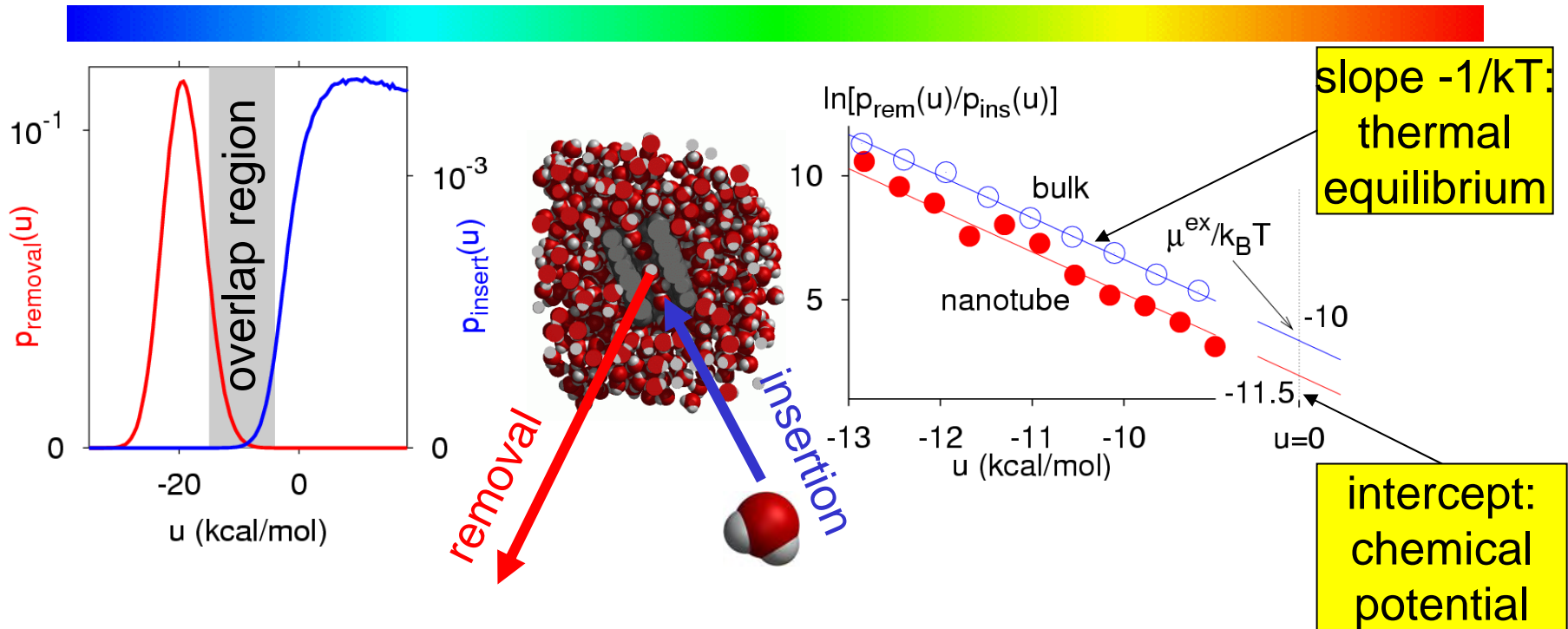
# Molecular Dynamics Simulations of Carbon Nanotube in Water

(Hummer, Rasaiah & Noworyta, *Nature* **414**, 188, 2001)

- Nanotube fills within picoseconds and remains filled for 66 nanoseconds
- Loss of hydrogen-bond energy?
- Loss of entropy because of 1D order?



# Thermal and Chemical Equilibrium between Water in Nanotube and Bulk Phase



## Excess chemical potentials from histogram analysis

- $\mu_{\text{w}}^{\text{ex}} = -6.05 \pm 0.02$  kcal/mol (bulk TIP3P water)
- $\mu_{\text{nt}}^{\text{ex}} = -6.87 \pm 0.07$  kcal/mol (nanotube)
- $-kT \ln(\langle N \rangle / \rho \Delta V) = -0.87$  kcal/mol  $\sim \mu_{\text{nt}}^{\text{ex}} - \mu_{\text{w}}^{\text{ex}}$

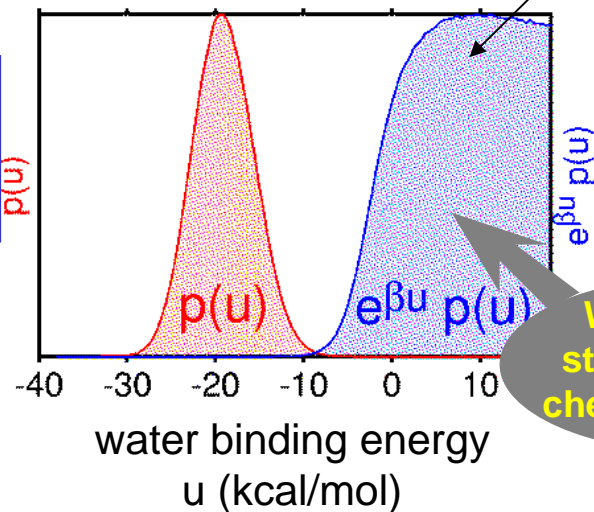
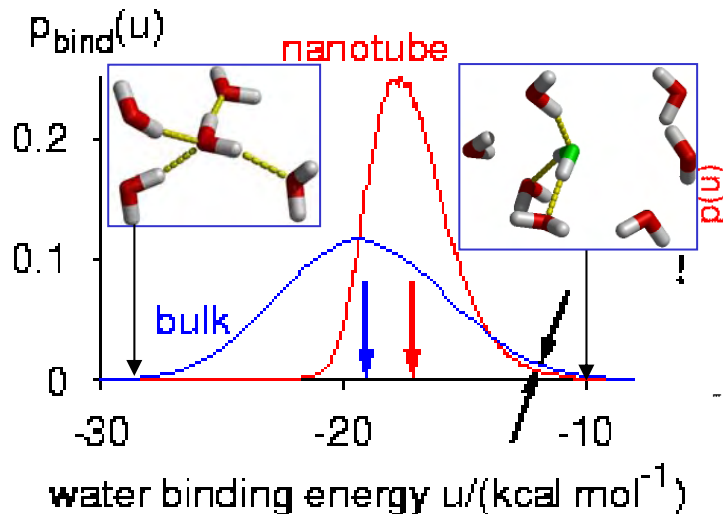
} chemical equilibrium



# Thermodynamics from Binding Energies: High-Energy Tail Determines Vapor Pressure

- Channel shields from fluctuations
  - Degenerate ground state: low population of high energy states

$$e^{\beta\mu^{ex}} = \int e^{\beta u} p(u) du$$



Weakly bound states determine chemical potential

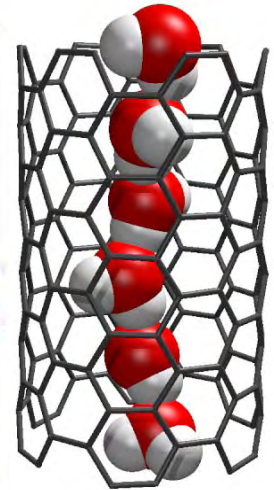
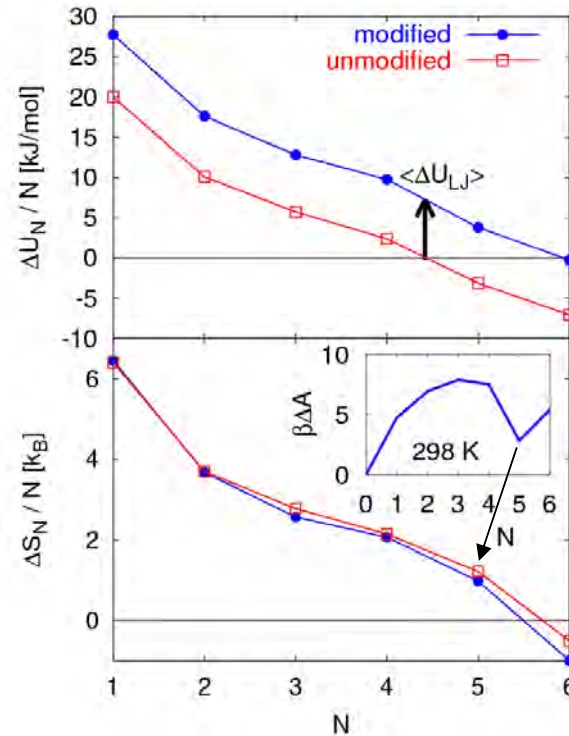
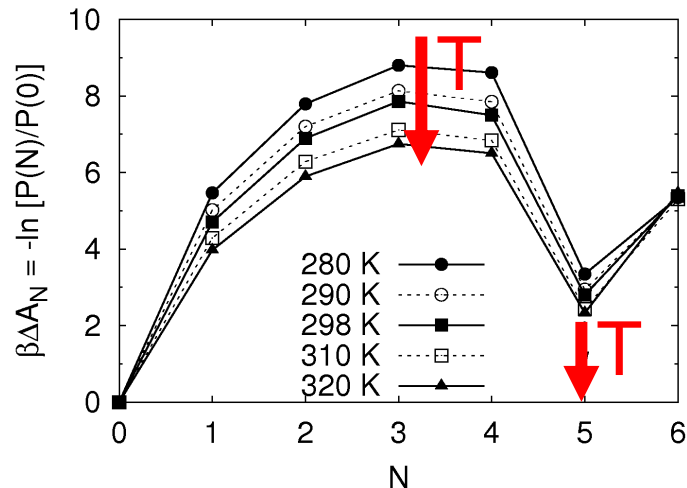
# Thermodynamics of Filling from Grand-Canonical Partition Function for Infinite Periodic Tube

(Vaitheeswaran, Rasaiah, and Hummer, J. Chem. Phys. **121**, 7955, 2004)

- Grand-canonical partition function calculated term-by-term using histogram method

$$\frac{P(N+1)}{P(N)} = \frac{\rho V}{N+1} \langle \exp[-\beta(U_{N+1} - U_N)] \rangle_N$$

- Positive entropy of filled state

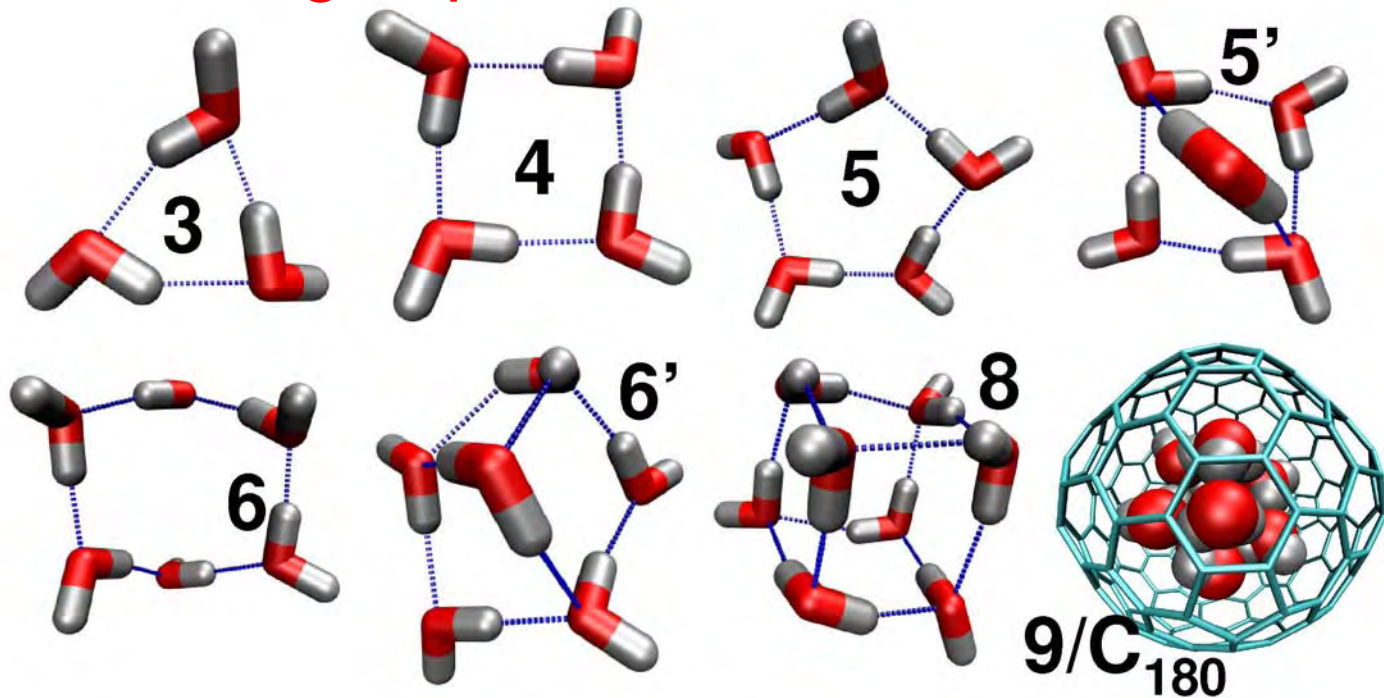


Dangling OH bond  
compensates entropy loss of  
1D ordering

# Water in Nonpolar Cavities

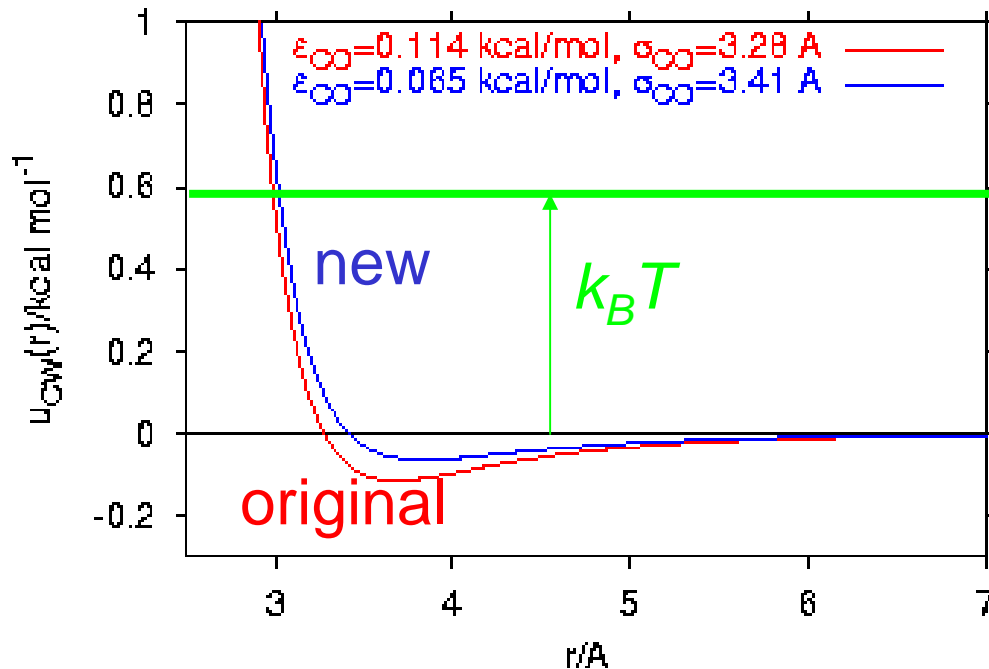
(Vaitheeswaran, Yin, Rasaiah, and Hummer, *Proc. Natl. Acad. Sci. USA* **101**, 17002, 2004)

- Water clusters in weakly polar spherical cavities can be thermodynamically stable and resemble gas-phase clusters

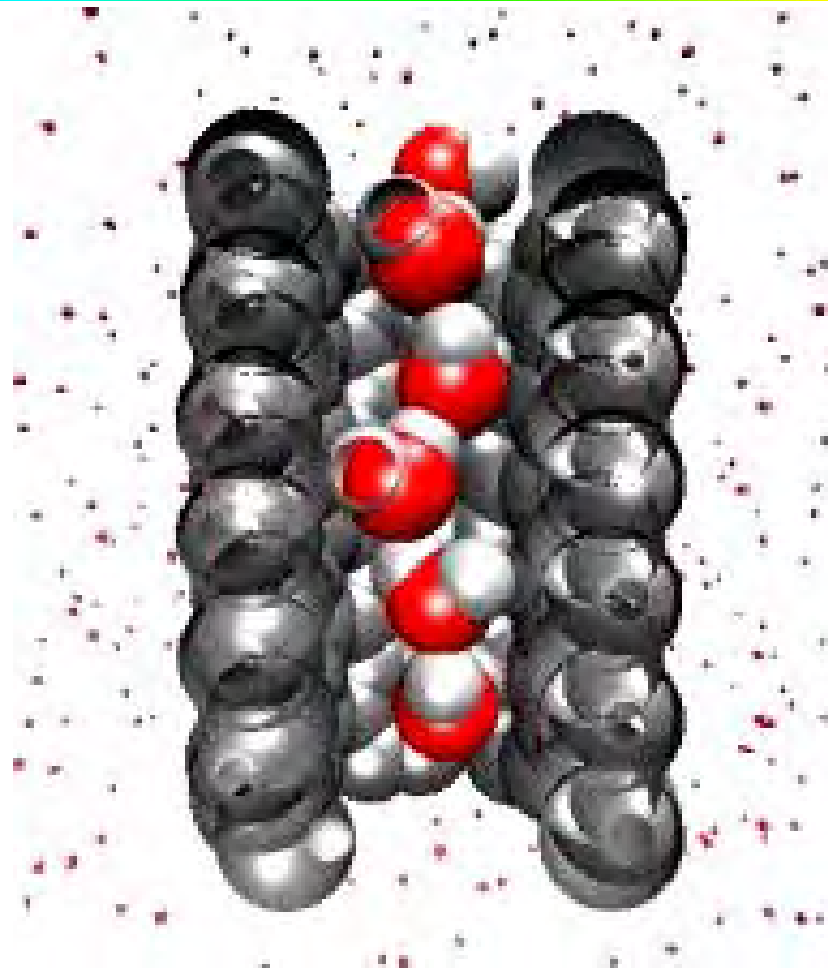


# Effects of Interaction Potentials and Solvent Conditions: Modified Carbon-Water Attractions

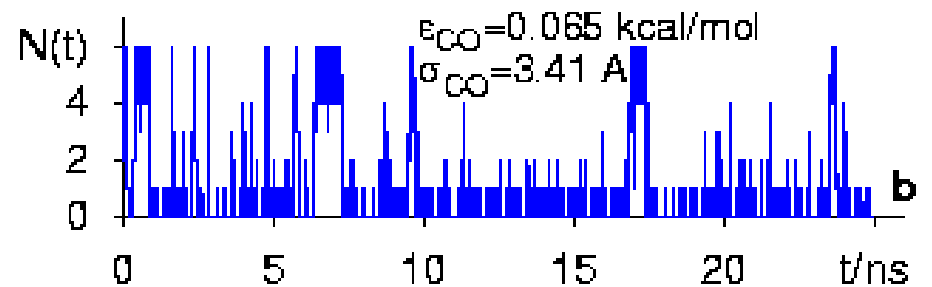
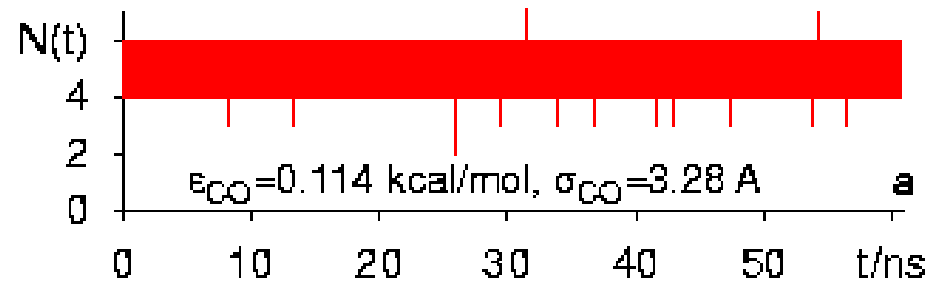
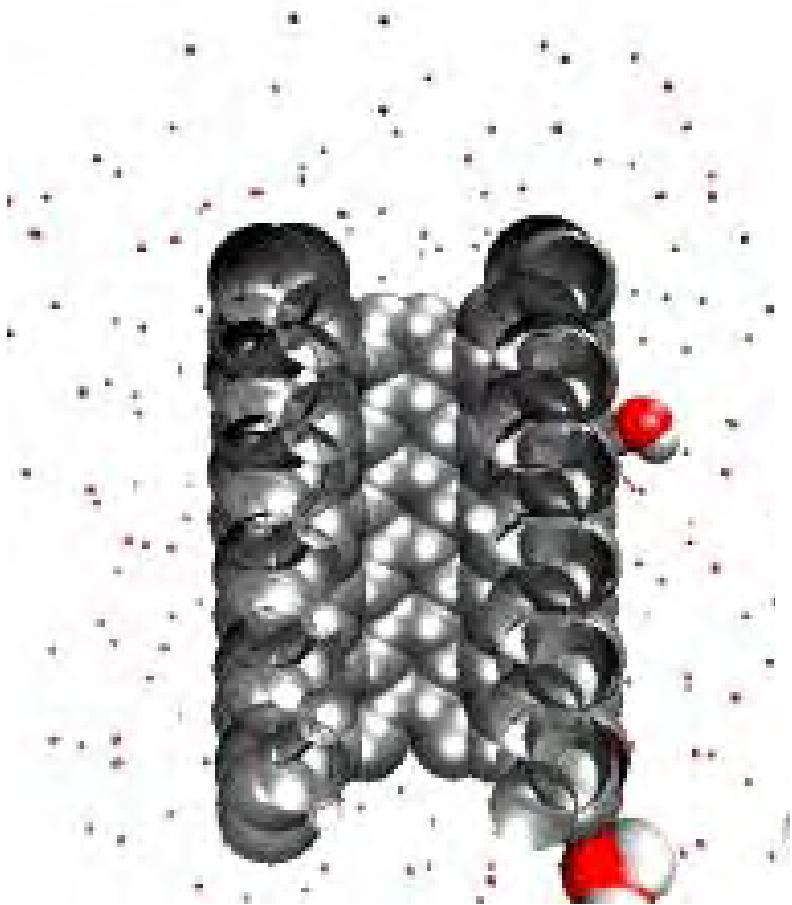
- Modified carbon parameters
  - $\varepsilon_{\text{CO}} = 0.065$  (0.114) kcal/mol
  - $\sigma_{\text{CO}} = 3.41$  (3.28) Å



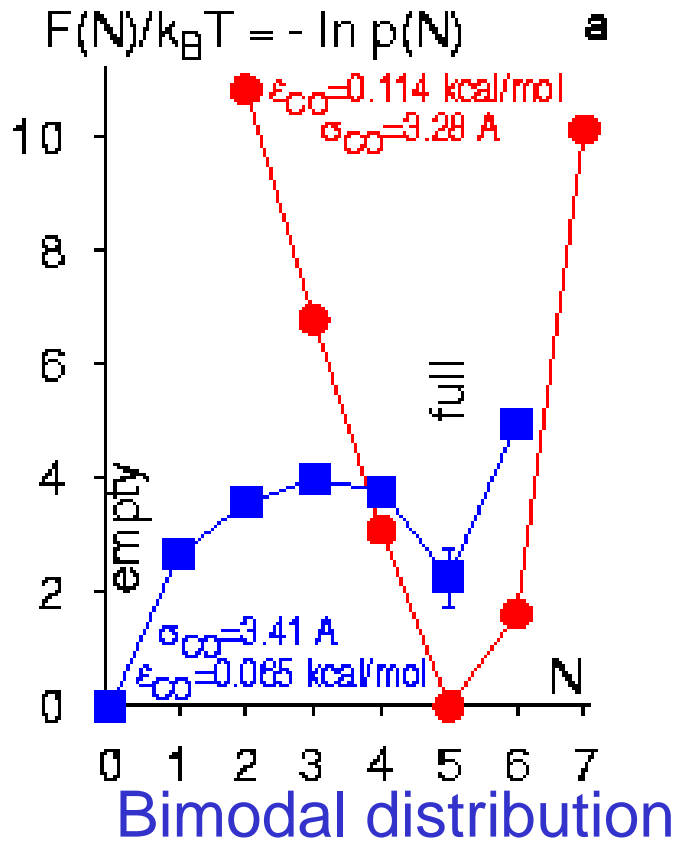
# Emptying Transition



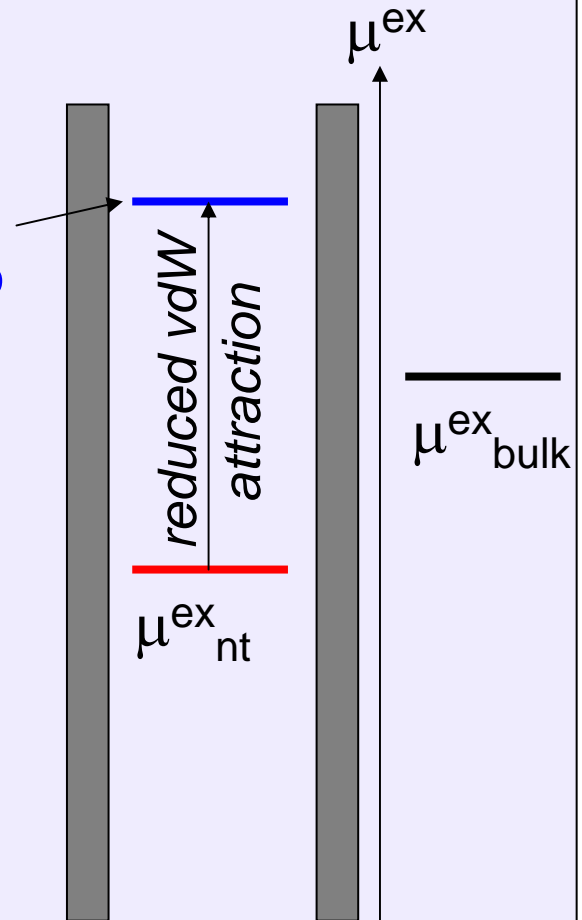
# Filling/Emptying Transitions



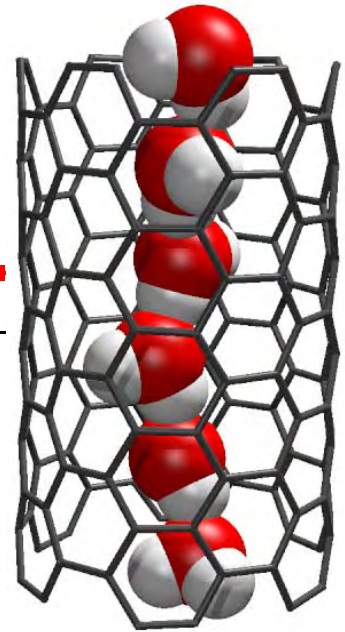
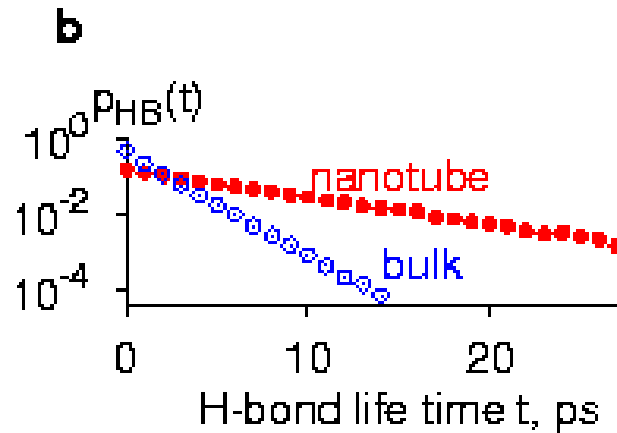
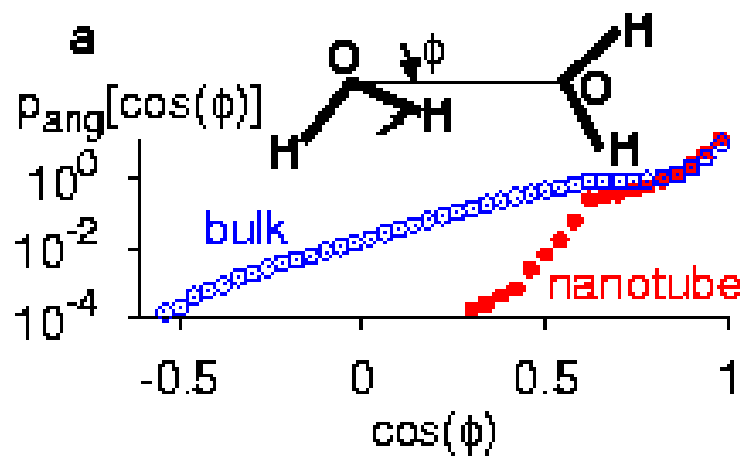
# Change in Potential Parameters/Solvent Conditions Results in Bimodal Occupancy Distribution



Average occupancy  $N \sim \exp(-\beta \Delta \mu^{\text{ex}})$  corresponds to 'unstable' fragmented chain  
 → fluctuations between filled and empty states ('coexistence')



## 2. Properties of 1D Confined Water: Long-Lived and Strongly Oriented Hydrogen Bonds in Narrow Channel



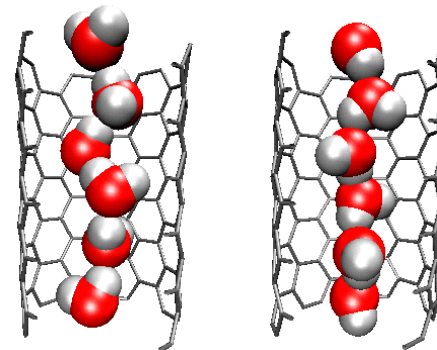
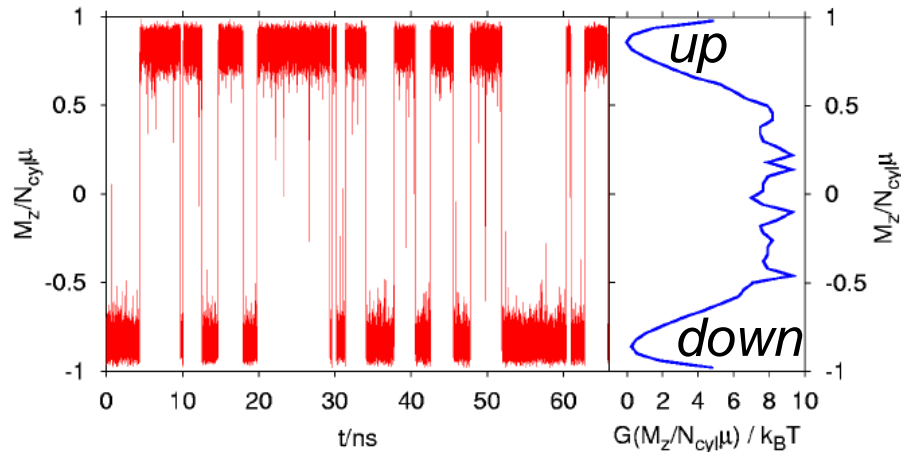
- H-bond angles  $> 30^\circ$ 
  - Water: 37%
  - Nanotube:  $< 15\%$

- H-bond Lifetime
  - Water: 1ps
  - Nanotube: 5ps



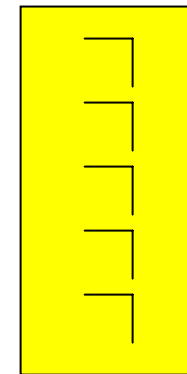
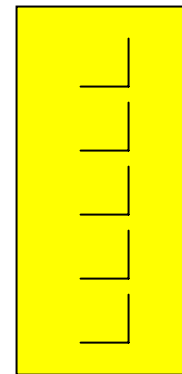
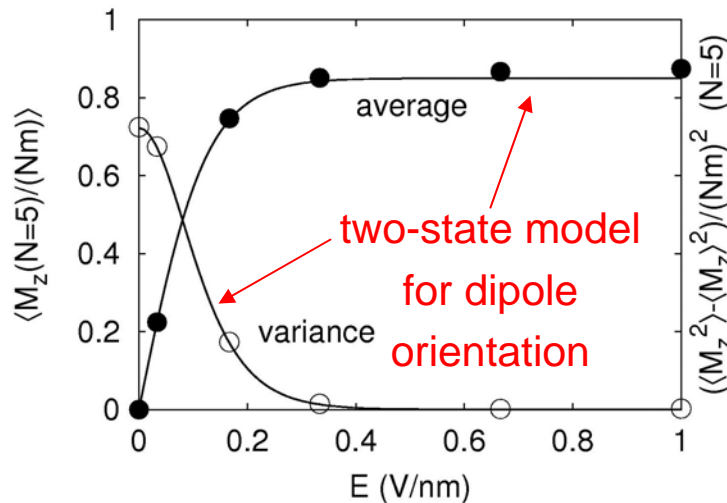
# Collective Dipolar Orientation of Water Chain Governed by Local Electric Field

(Vaitheeswaran, Rasaiah, and Hummer, J. Chem. Phys. **121**, 7955, 2004;  
Best and Hummer, Proc. Natl. Acad. Sci. USA, in press, 2005)



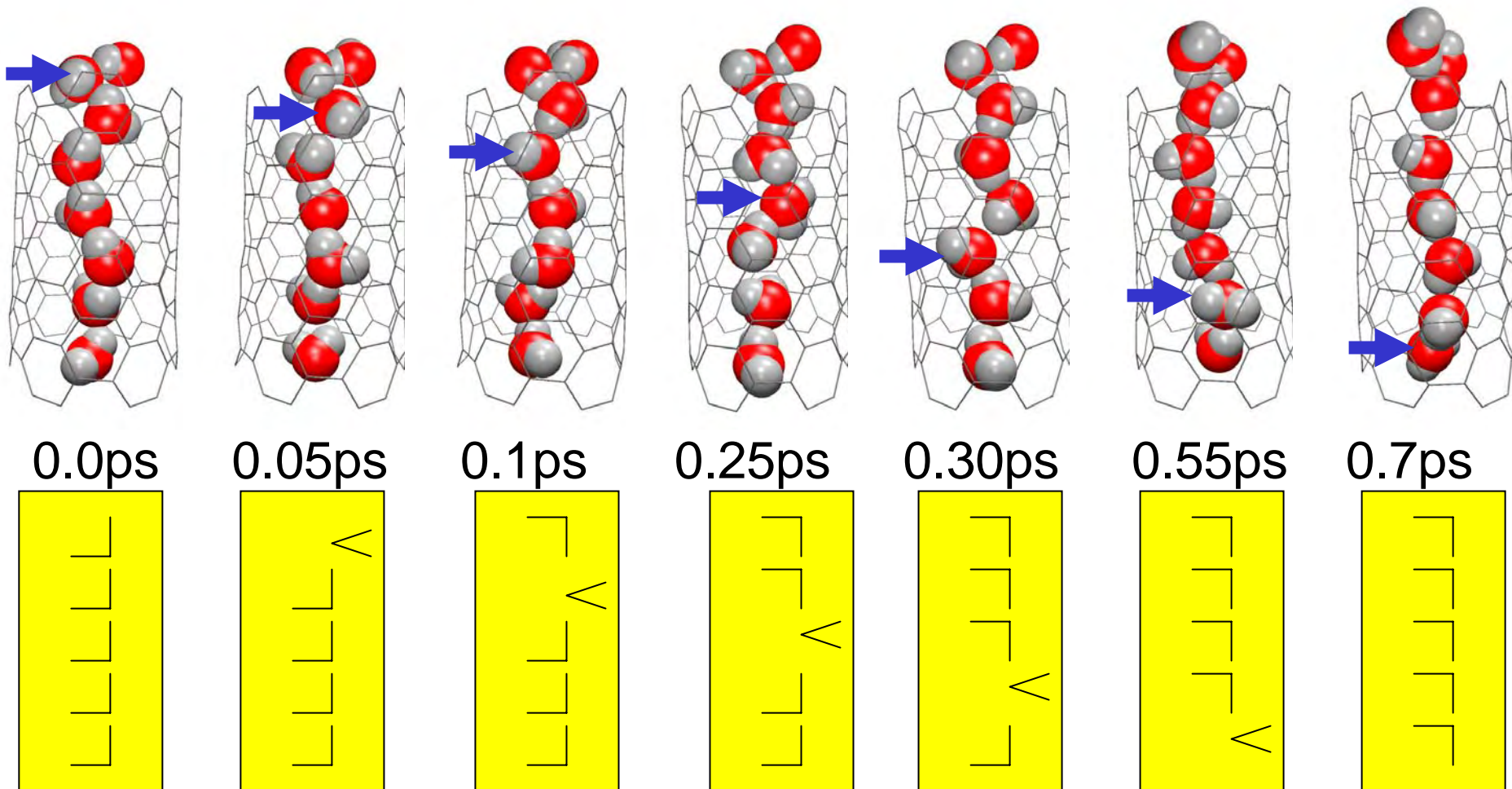
*up*

*down*



# Propagating Hydrogen Bond Defect Reorients Chain

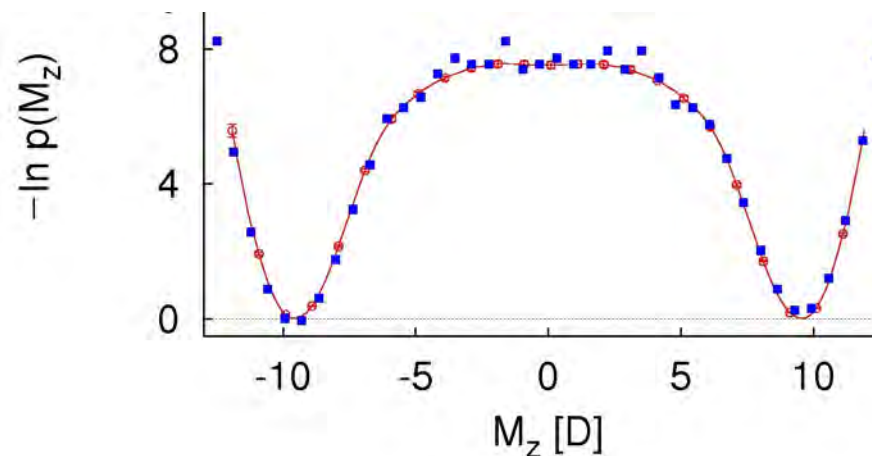
(Best and Hummer, Proc. Natl. Acad. Sci. USA, in press, 2005)



# Rate of Dipolar Reorientation is Slow

- Defect motion is diffusive

- Typically  $\sim 7$  recrossings of  $M_z=0$  dividing surface
- Langevin damping frequency of  $\sim 200 \text{ ps}^{-1}$ , with an average transition path duration of  $\sim 2 \text{ ps}$



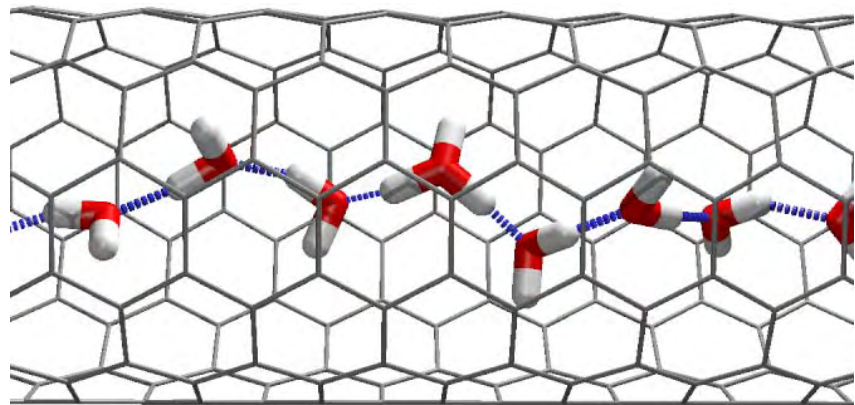
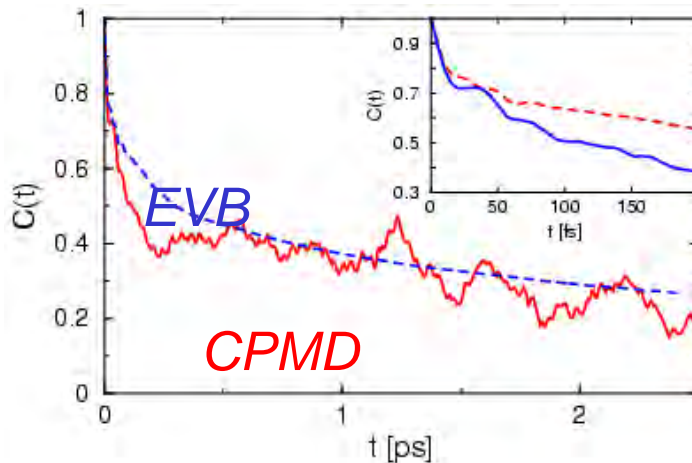
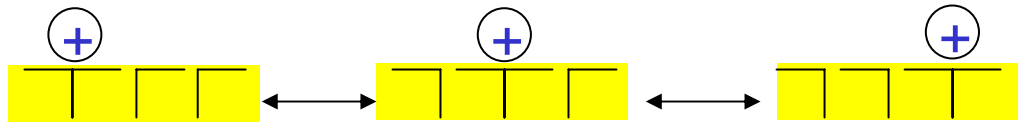
- Rate of dipole reorientation is slow

- $k \sim 1/(2 \text{ ns})$  for solvated tube filled with  $\sim 5 \text{ H}_2\text{O}$
- $k > 1/(20 \text{ ns})$  for tube in low-dielectric environment
- Free energy barrier of  $\sim 8 k_B T$  dominated by electrostatics

# 3. Proton Transport along 1D Water Wires

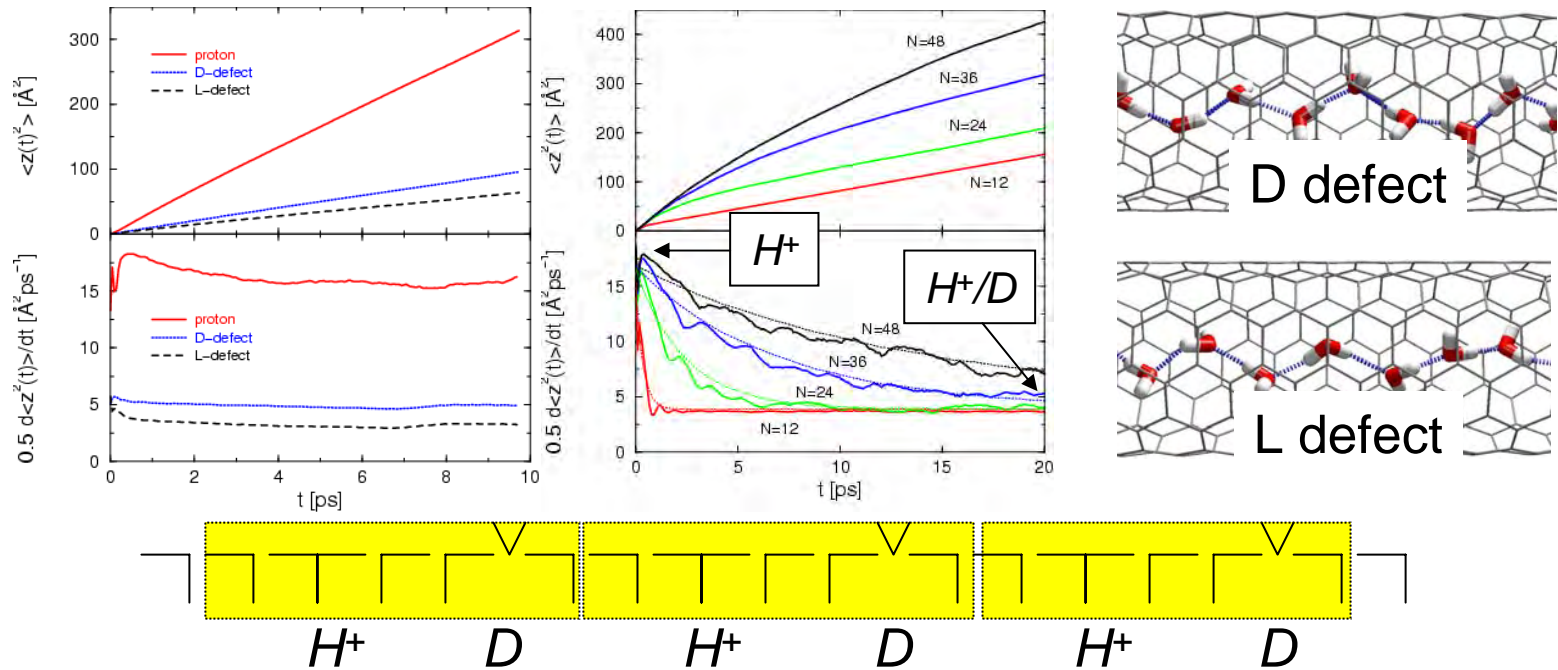
(Dellago, Naor and Hummer, *Phys. Rev. Lett.* **90**, 105902, 2003)

- Molecular dynamics simulations of water and excess proton in nanotube
  - Car-Parrinello dynamics (DFT/BLYP)
  - Empirical-valence-bond model (Warshel and Weiss, *J. Am. Chem. Soc.* **102**, 6218, 1980; Schmitt and Voth, *J. Phys. Chem. B* **102**, 5547, 1999)
  - Grotthuss H<sup>+</sup> relay (de Grotthuss, *C. J. T. Annal. Chim.* **58**, 54, 1806):




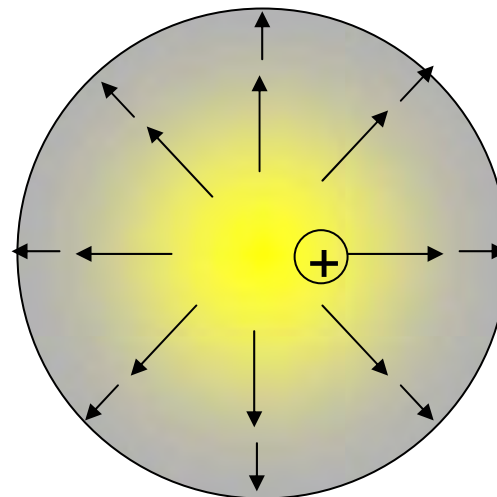
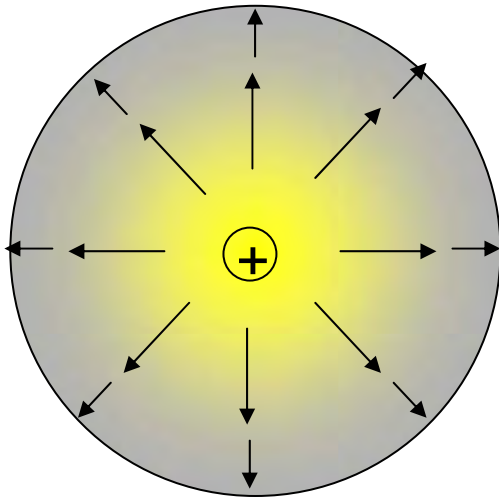
# 1D Proton Transport Coupled to Defect Motion

- Strong  $1/r$  electrostatic coupling between  $H^+$  and H-bond (D) defect in periodic tube (both defects carry positive effective charge):
  - 10-fold reduction of apparent diffusion constant



# 1D vs 3D Proton Conduction

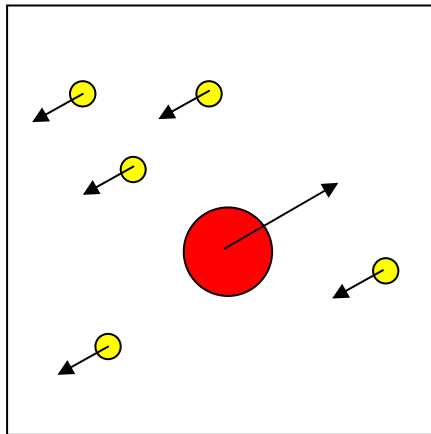
- Proton diffusion approximately 40 times faster than in bulk water:  $D(\text{H}^+) \approx 170 \times 10^{-5} \text{ cm}^2 \text{ s}^{-1}$
- 1D: local 
- 3D: non-local



# System-size dependence of diffusion coefficients

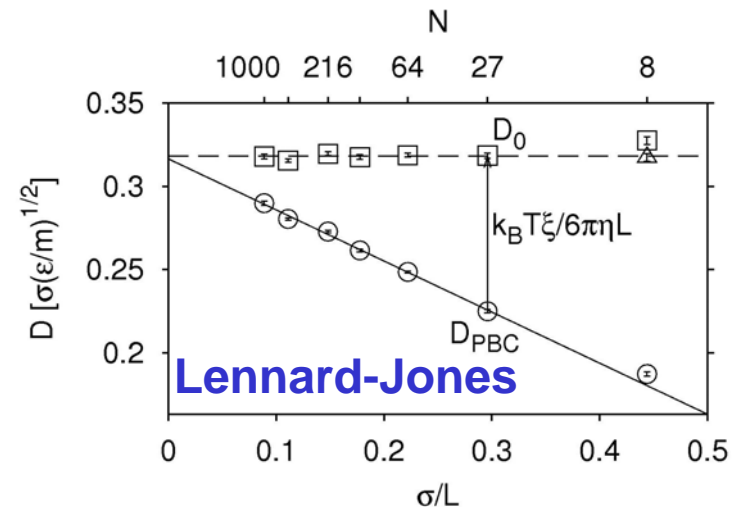
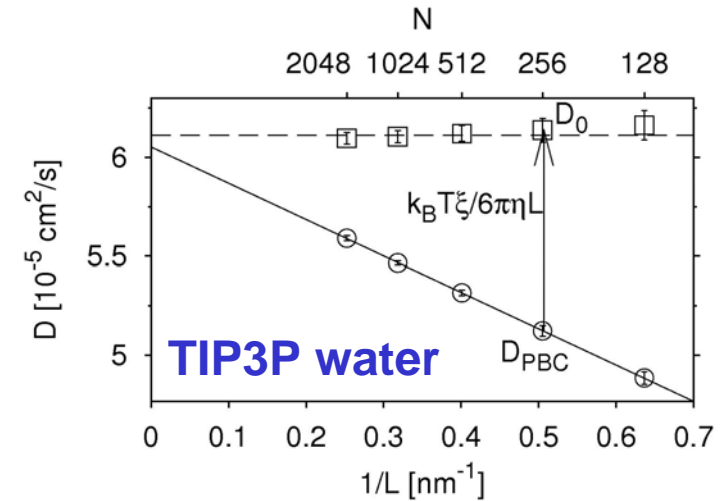
(Yeh and Hummer, *Biophys. J.* **86**, 681, 2004; *J. Phys. Chem. B* **108**, 15873, 2004;  
Dünweg & Kremer, *J. Chem. Phys.* **99**, 6983, 1993)

- Conservation of momentum imposes zero net force



- Hydrodynamic theory

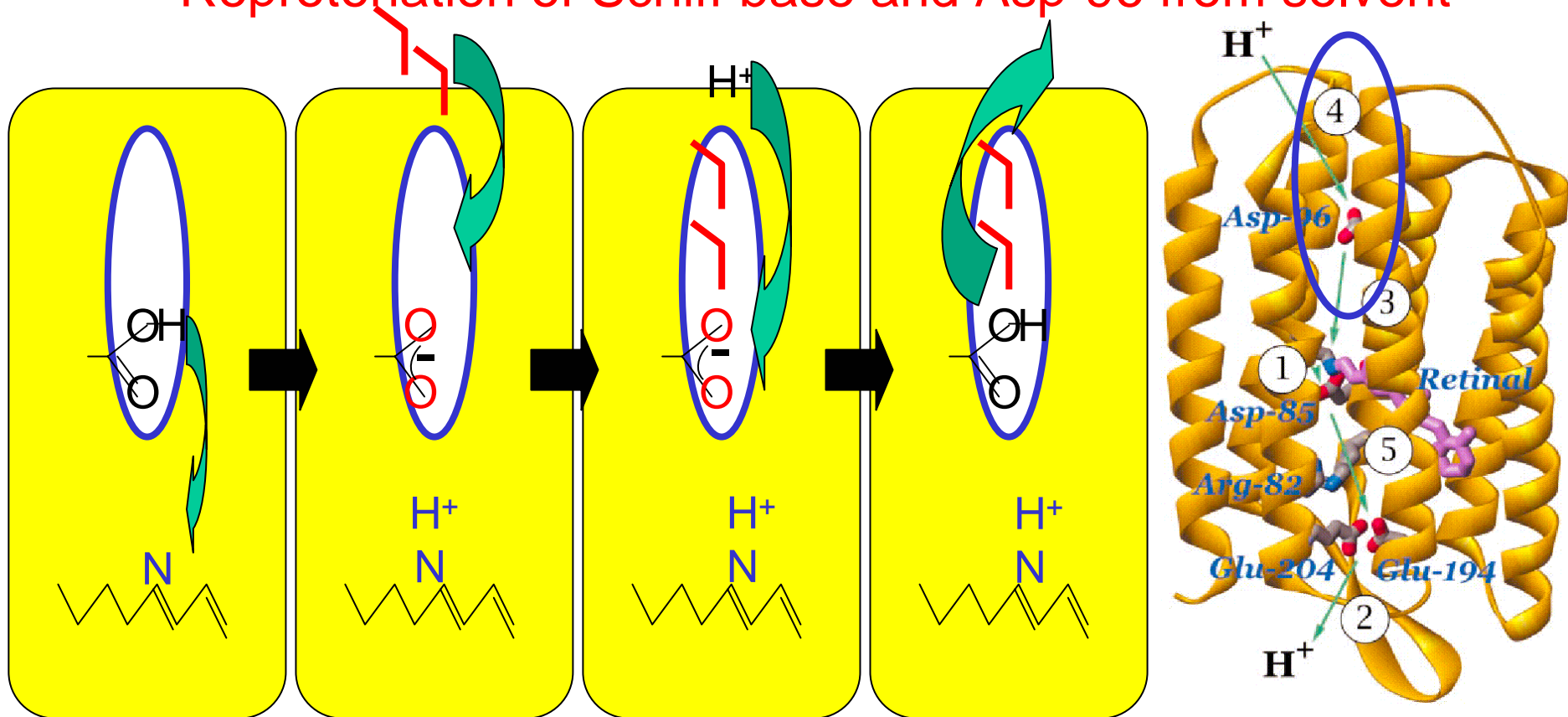
$$D_{\text{app}}(L) = D_0 - \frac{k_B T \xi_{\text{EW}}}{6\pi\eta L}$$



# 3. Water Mediated Proton Transfer in Light-Driven Proton-Pump Bacteriorhodopsin

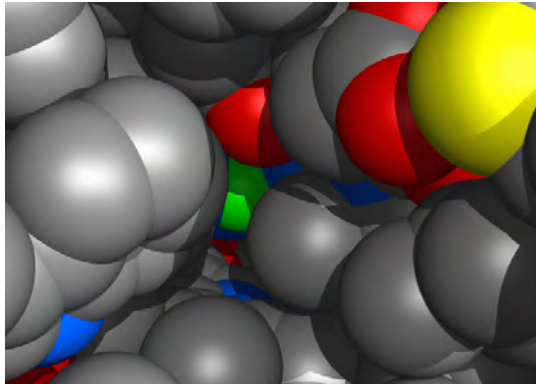
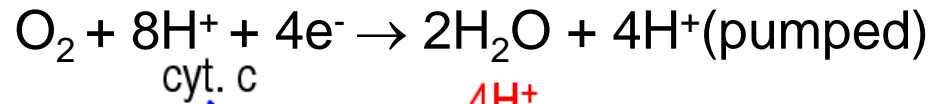
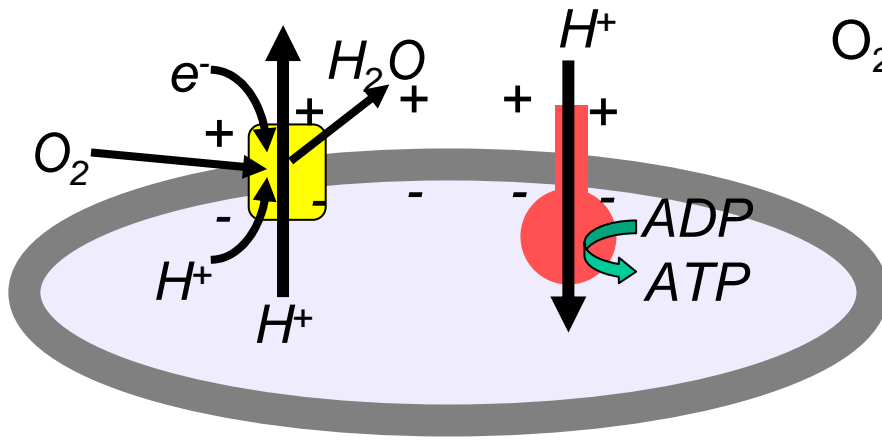
(Hummer, Rasaiah, Noworyta, ICCN Proceedings, 2002)

- **Transient water networks in trapped intermediates** (e.g., Schobert, Brown, Lanyi, J. Mol. Biol. 330, 553, 2003)
- **Reprotonation of Schiff base and Asp-96 from solvent**

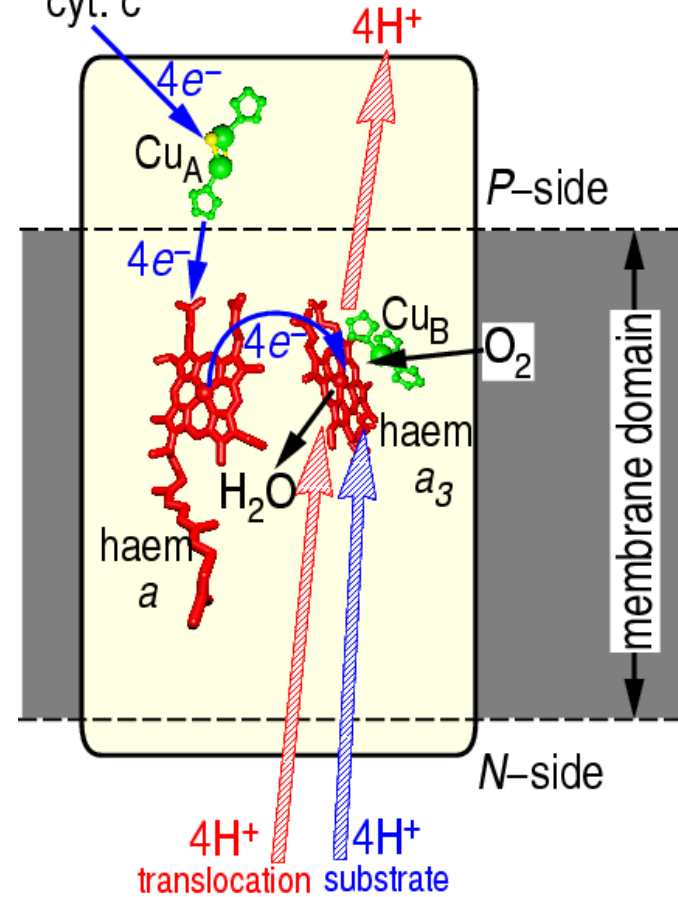




# Cytochrome c Oxidase



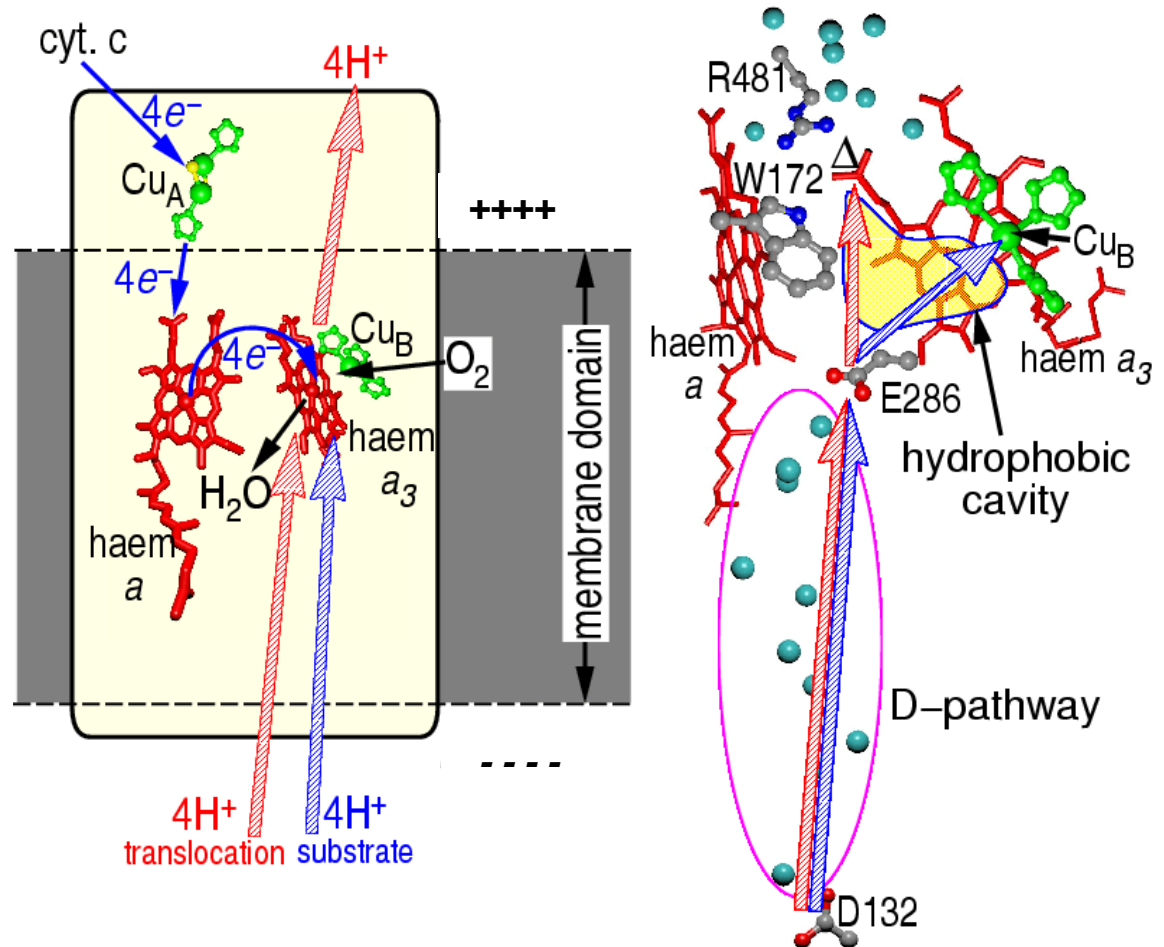
Functional role of water in nonpolar active-site cavity?



# Proton Pumping in Cytochrome C Oxidase

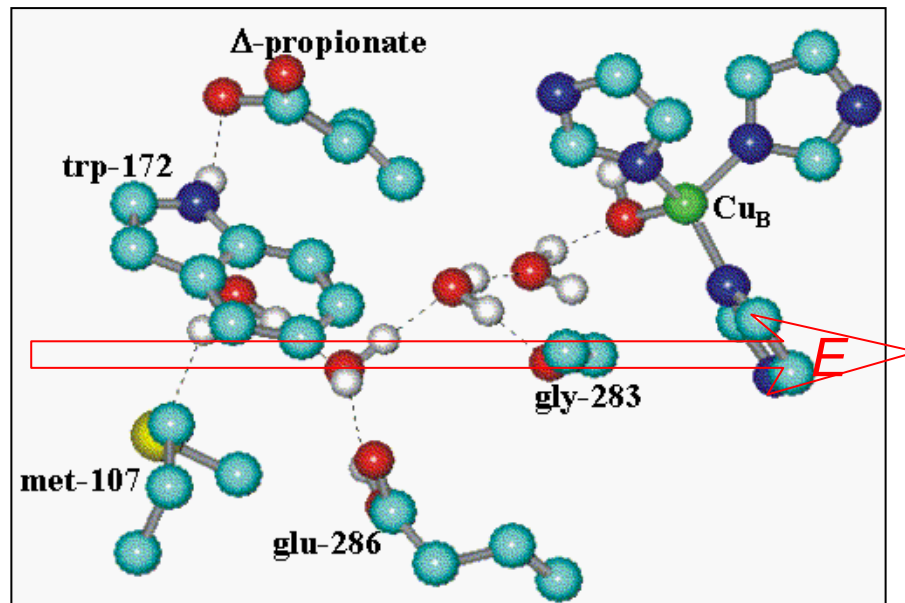
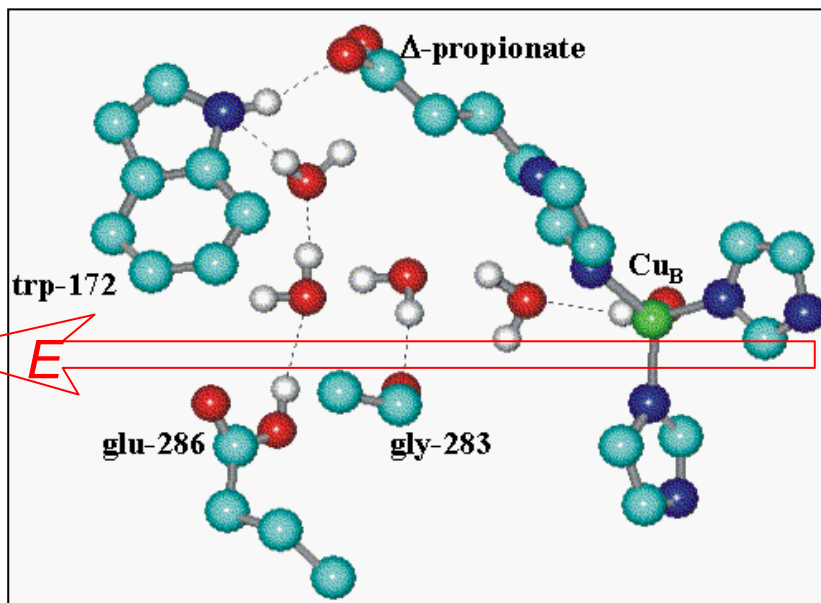
(Wikström, Verkhovsky and Hummer, *Biochim. Biophys. Acta-Bioenerget.* **45238**, 1, 2003)

- Gating of 'chemistry' and 'pumping'
  - Pumped protons (for energy conservation) and chemical protons (for water production) use same pathway
  - Hydrophobic cavity between hemes is possible fork in pathway



# Heme-a/Heme-a<sub>3</sub>/Cu<sub>B</sub> Charge Distribution Switches Water-Chain Orientation

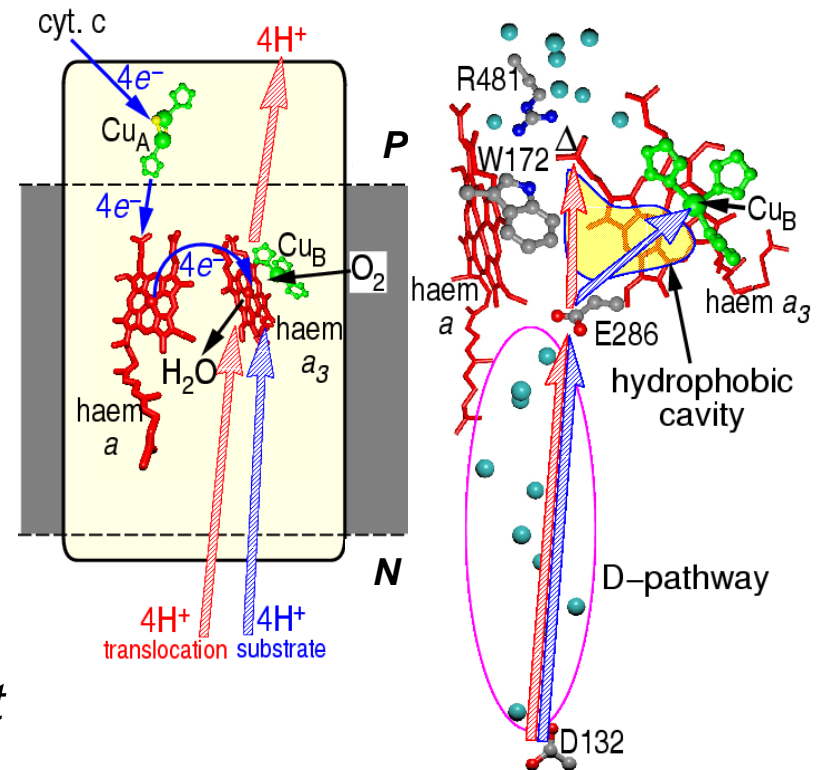
- Reorientation within ~1 ps of electron transfer in molecular dynamics simulations
- Heme-a reduced
- Heme-a<sub>3</sub>/Cu<sub>B</sub> oxidized
- Heme-a oxidized
- Heme-a<sub>3</sub>/Cu<sub>B</sub> reduced



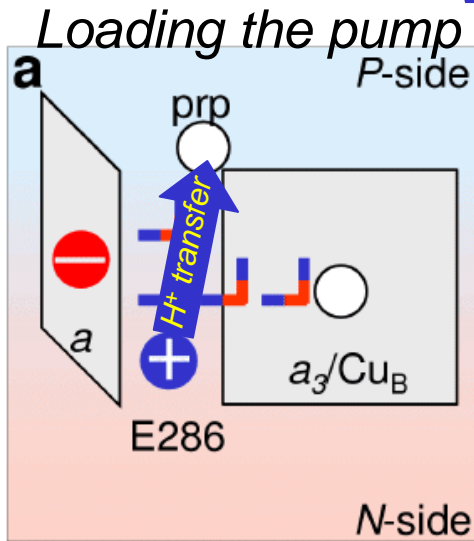
# Proton Pumping in Cytochrome C Oxidase

(Wikström, Verkhovsky and Hummer, *Biochim. Biophys. Acta-Bioenerget.* **45238**, 1, 2003)

- Gating of 'chemistry' and 'pumping'
  - Water in cavity orientated by electric field between hemes a and  $a_3$ / $\text{Cu}_B$
  - Switching between  $\text{H}^+$  paths by water orientation (' $\text{H}^+$  diode')
- Coupling of  $\text{O}_2$  reduction to pumping
  - $\text{H}^+$  transfer from E286 to heme- $a_3$  propionate provides gate ('solvent fluctuation') for electron transfer from heme a to heme- $a_3$ / $\text{Cu}_B$
  - 'Pumped'  $\text{H}^+$  trapped by electron transfer and reprotonation of E286



# Water-Gated Proton Pump



$H^+$  transfer

E286 to propionate

electron transfer

haem a reduction from P-side

water reorientation

E286  $H^+$  uptake from N-side

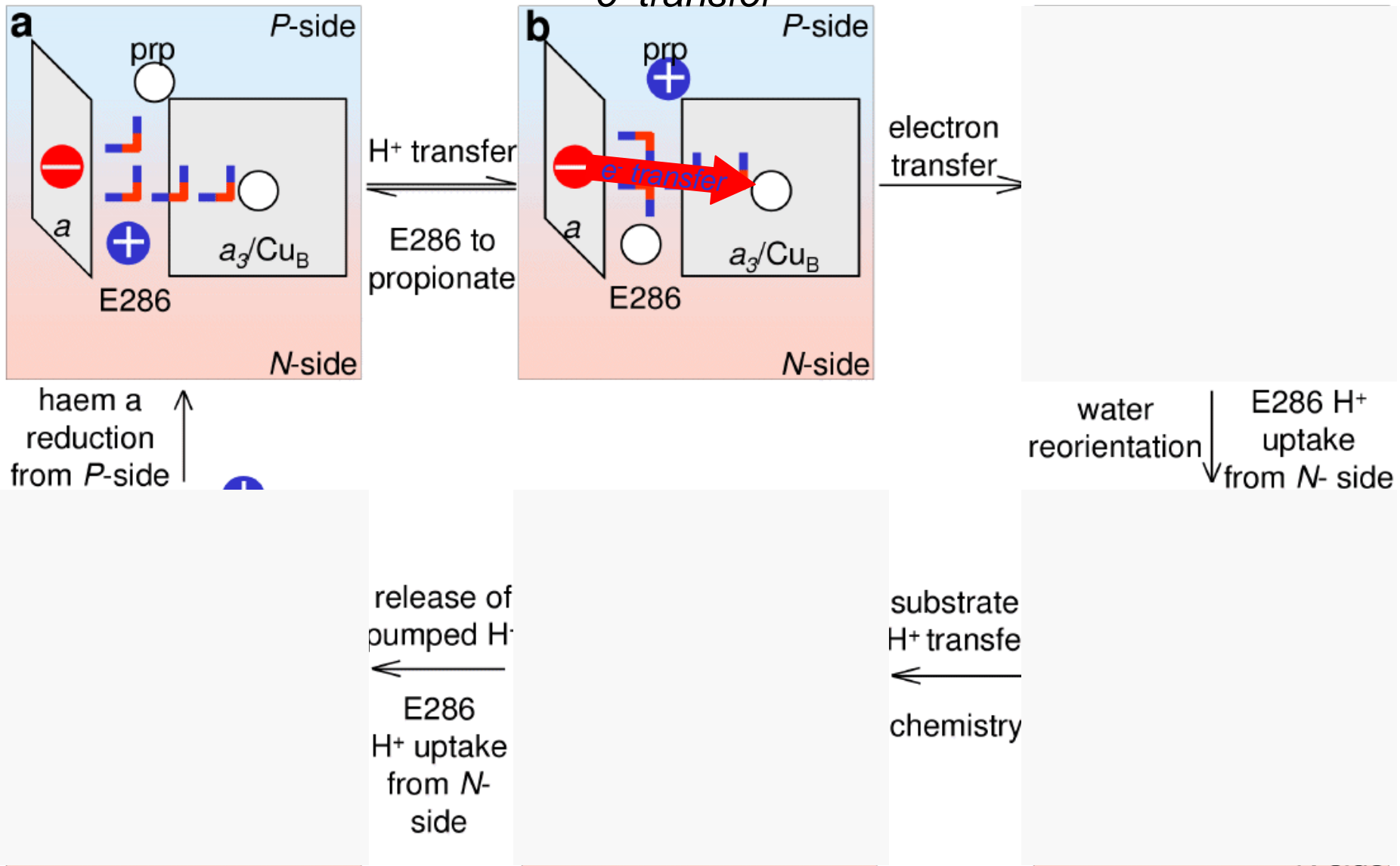
release of pumped  $H^+$

E286  $H^+$  uptake from N-side

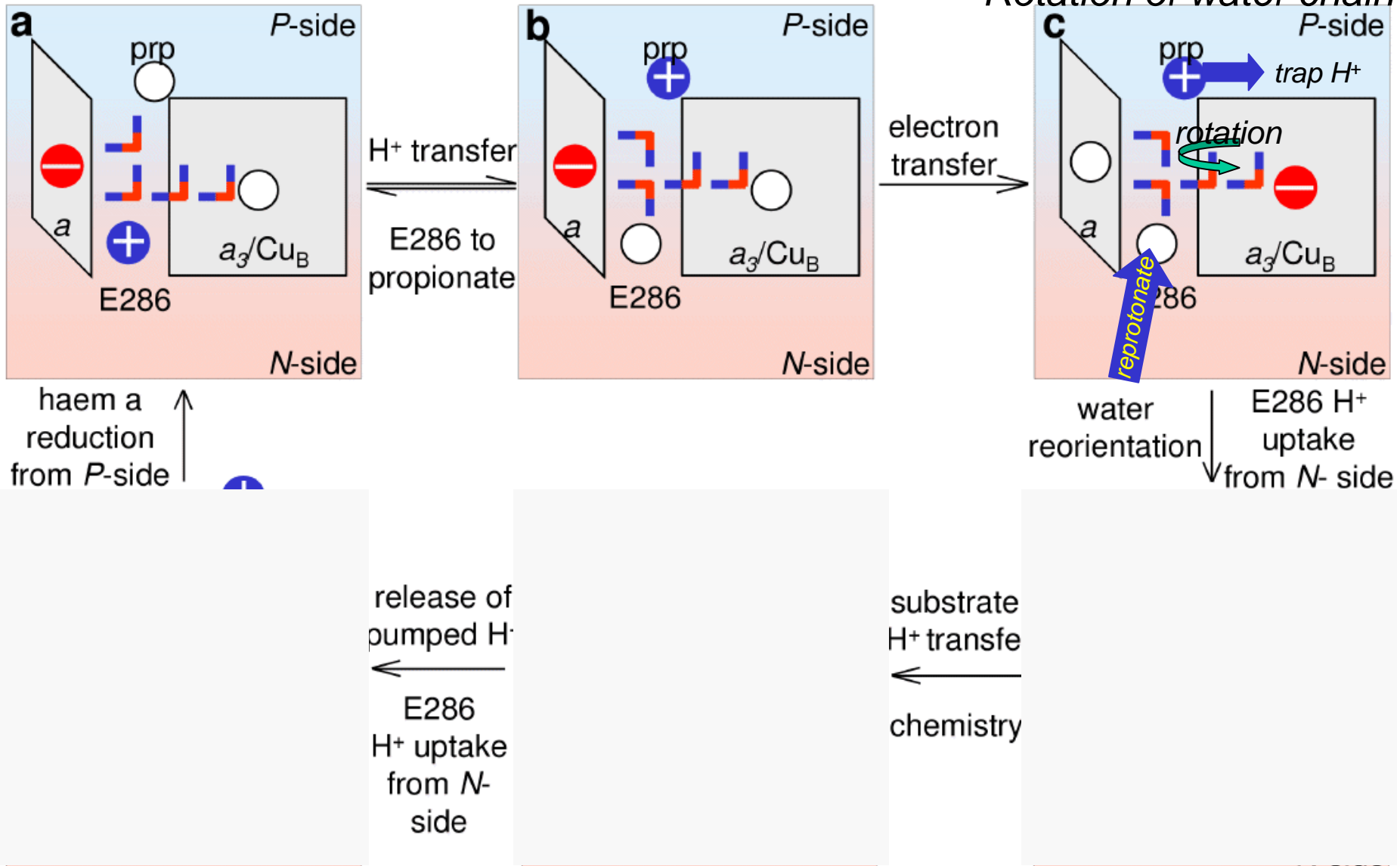
substrate  $H^+$  transfer

chemistry

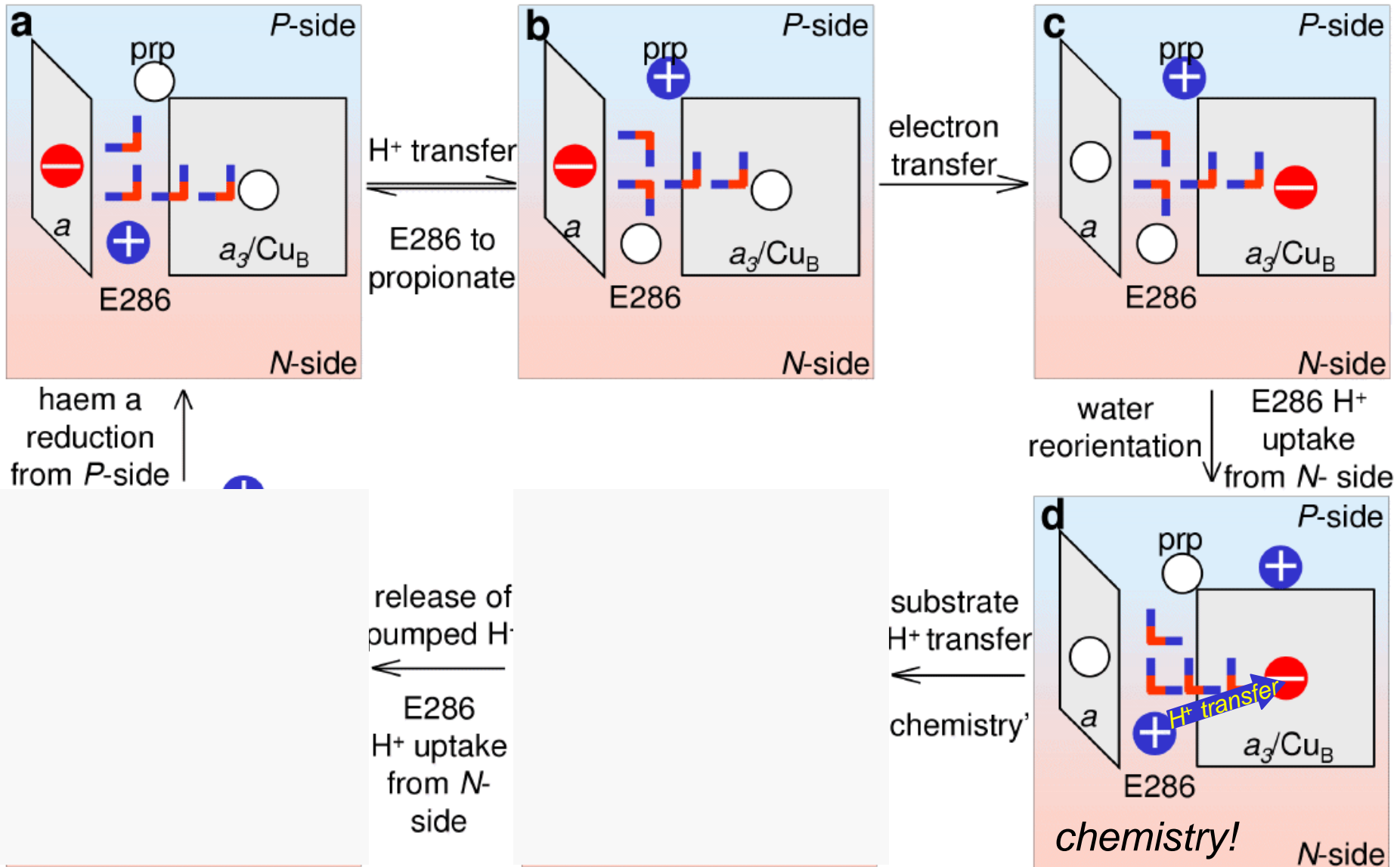
# Water-Gated Proton Pump



# Water-Gated Proton Pump

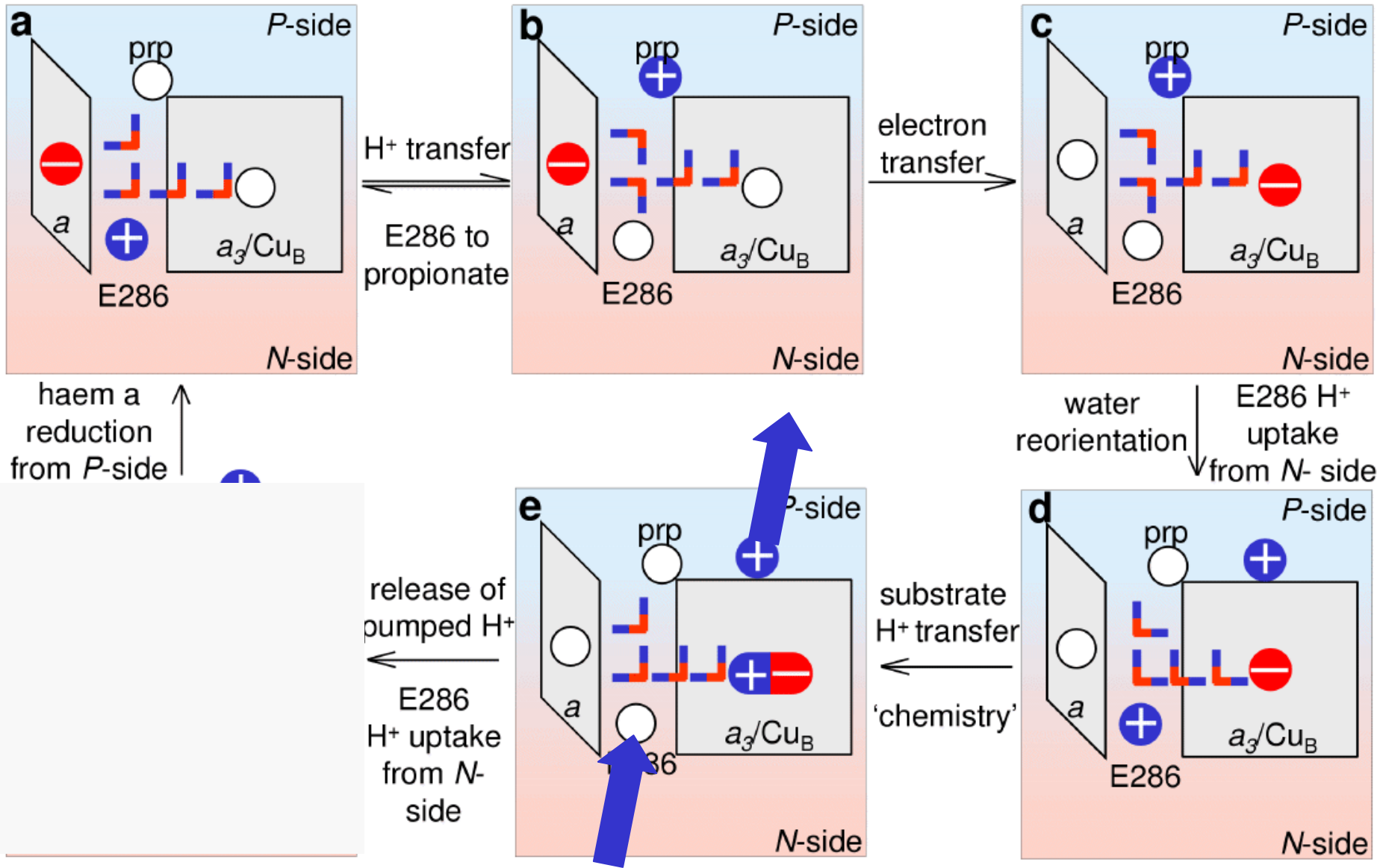


# Water-Gated Proton Pump

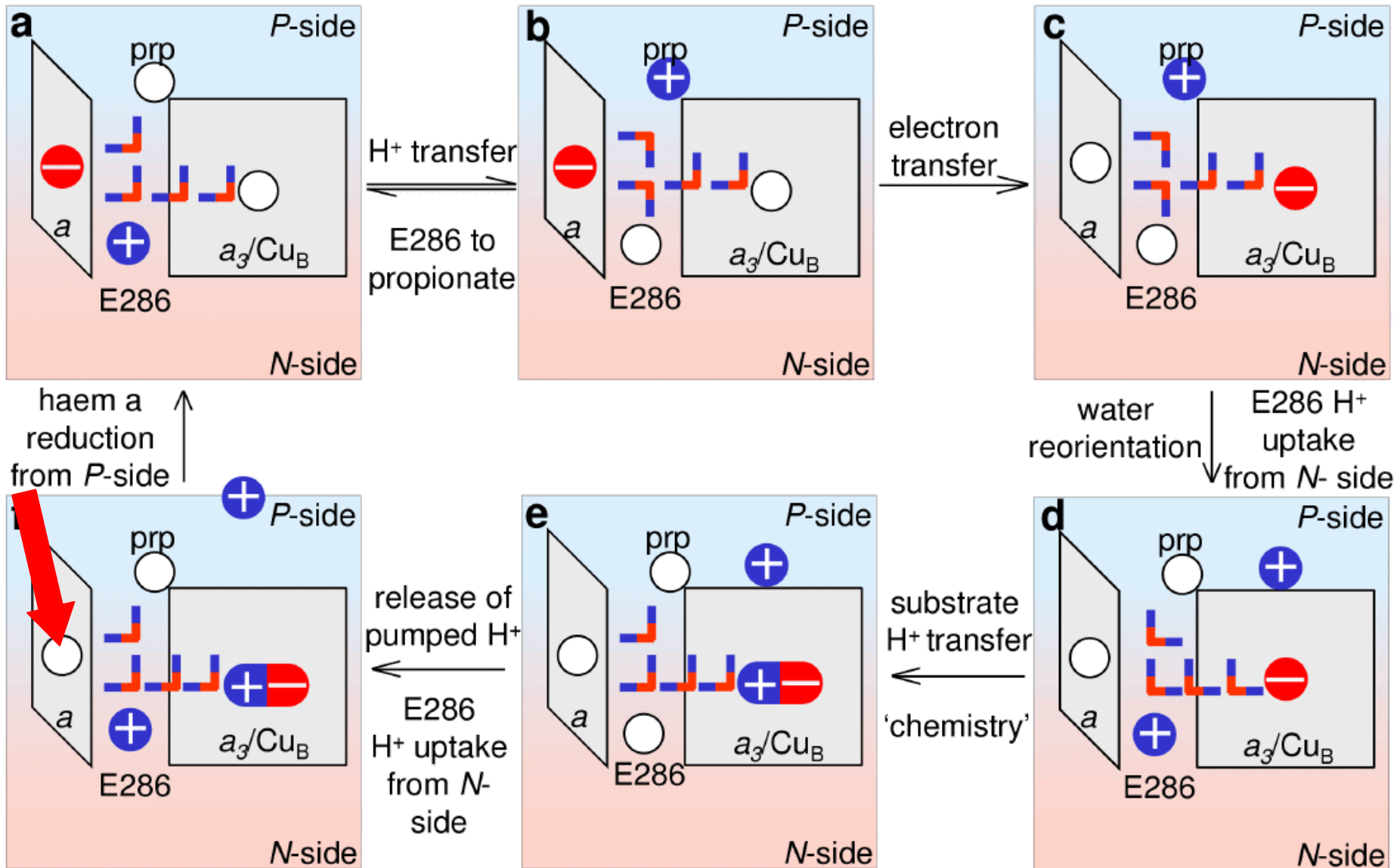




# Water-Gated Proton Pump

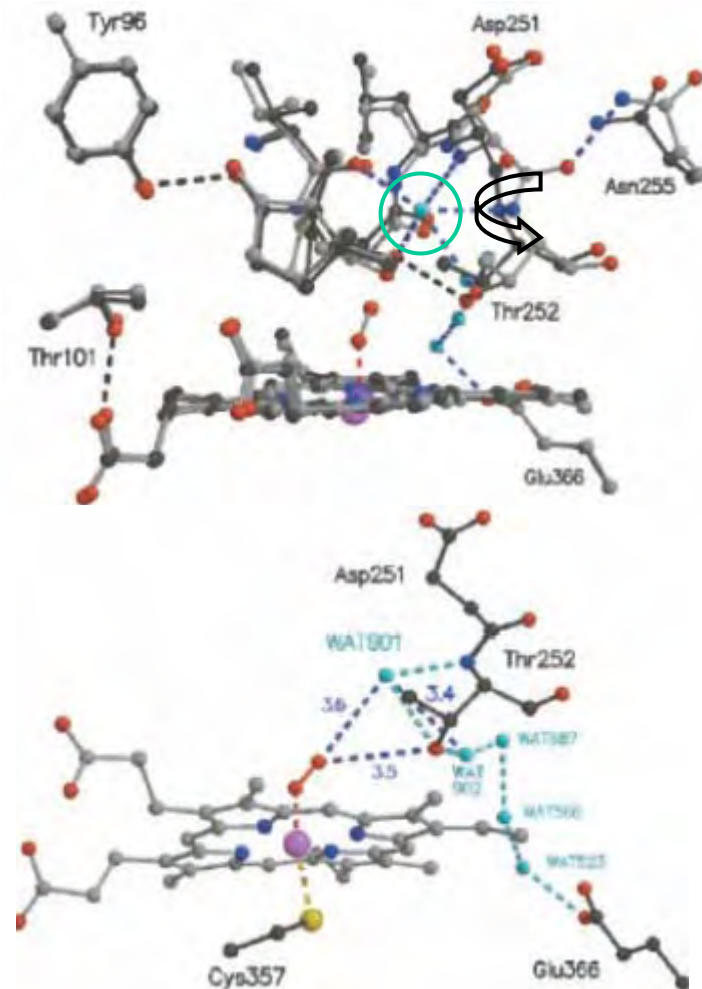


# Water-Gated Proton Pump



# 4. Role of Protein Dynamics in Biological Proton Transfer: Water Penetration and Side Chain Isomerization in Cytochrome P450cam

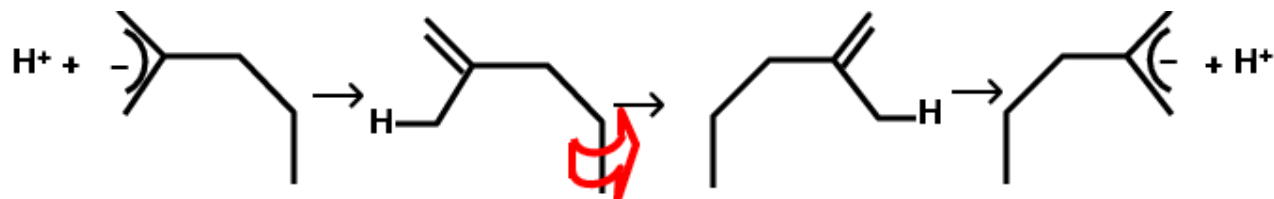
- Cryo-trapped intermediate with dioxygen bound
  - Exposure of amide group to previously empty non-polar cavity induces water filling (Schlichting et al, *Science* **287**, 1615, 2000)



# Network Model of Proton Transfer in Proteins

(Taraphder and Hummer, *J. Am. Chem. Soc.* **125**, 3931, 2003)

- **H<sup>+</sup> transfer via H bonds and shuttles of ionizable side-chains:**  $\text{H}^+ + \text{AH} \dots \text{OH} \dots \text{B}^- \rightarrow \text{HA} \dots \text{HO} \dots \text{HB}$

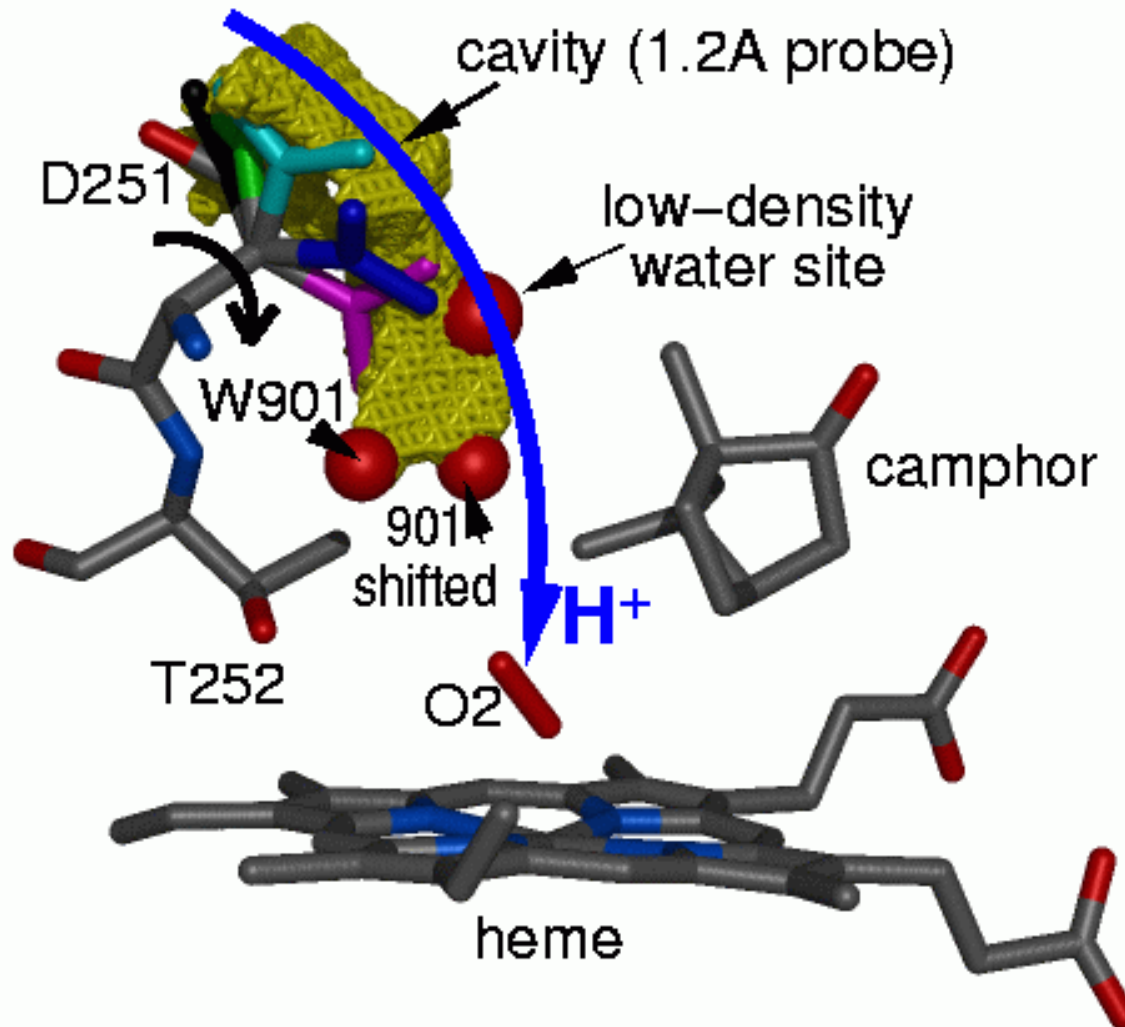


- **Recursive network analysis of H<sup>+</sup> relay groups**
  - Sample fluctuations in side-chain orientations and hydration to collect possible H<sup>+</sup> paths
  - Rank paths by using “steric” action

$$p(i \rightarrow j) = \exp(-\beta \Delta E_{ij}) / \sum_k \exp(-\beta \Delta E_{ik})$$

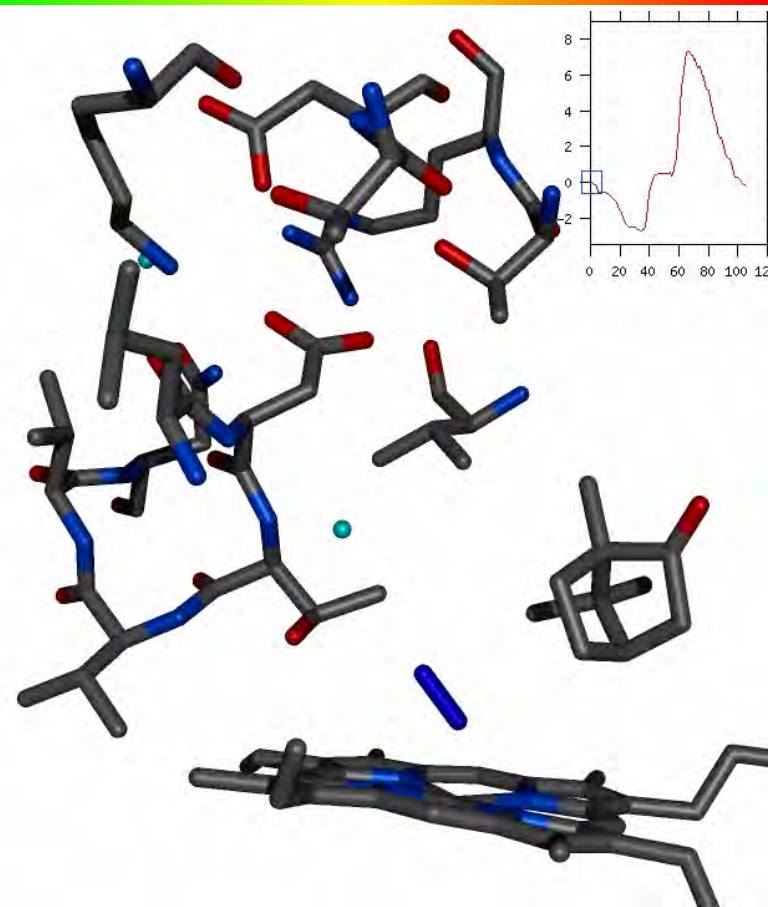
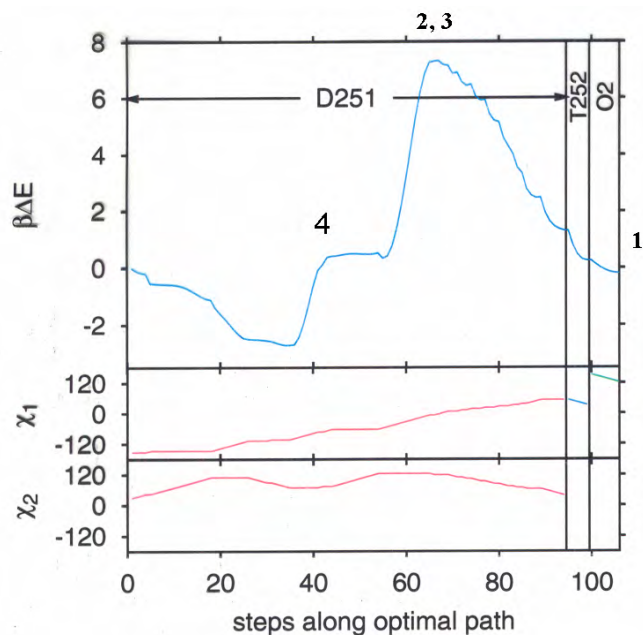
$$p(i_1 \rightarrow i_2 \rightarrow \dots \rightarrow i_n) = \prod p(i_k \rightarrow i_{k+1}) \equiv \exp(-S)$$

# Proton shuttle through concerted water penetration and side chain motion



# Energetics of Asp-251 Shuttle in P450cam

- Exhaustive search of side-chain conformers
- Sterically optimal path for Asp-251 isomerization



## Conclusions: Water in Nonpolar Channels



- Water can favorably occupy nonpolar channels, despite loss of hydrogen bonds
- Channels protect from fluctuations
  - Narrow distribution of energies
  - Unbound states rarely populated
  - Increased life time of hydrogen bonds with rare defects
  - Long life-time of water-chain orientation

## Conclusions: Drying



- **Water occupancy in nanotube channel extremely sensitive to attractive interactions**
  - Difficult to predict whether filling of narrow channels occurs under ambient conditions, but small perturbations to near-ambient conditions (polarity,  $T$ ,  $p$ , osmolality, etc.) can tune filling
- **Sharp two-state transitions between empty and filled states**
  - Intermediate states are rarely populated because of fragmented hydrogen bonds



# Proton Transfer in Proteins



- **Proton wires ‘on demand’**
  - Increase in local polarity can trigger water’ influx to establish protonic connectivity
- **High ‘delivery speed’**
  - High mobility of a *single* proton along ordered water chain inside hydrophobic pore (40x bulk!)
- **Unidirectional wires (‘diode’)**
  - Hydrogen-bond orientation controlled by electrostatics
- **High ‘fidelity’**
  - Only single proton delivered without reorientation

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